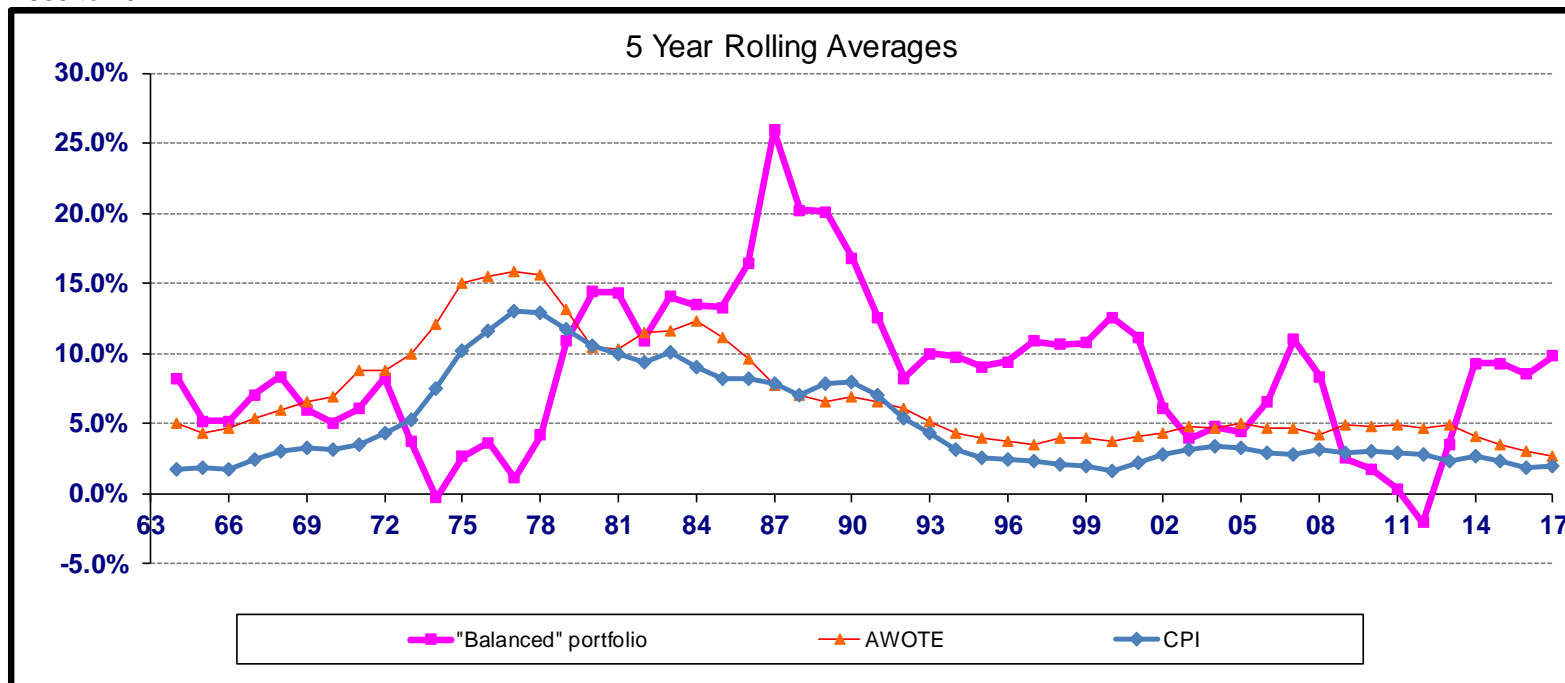


Australian Investment Performance 1959 to 2017 (and Investment Assumptions for Stochastic Models)

Colin Grenfell and **Thomas Sneddon**

Australian Investment Performance 1959 to 2017 (and Investment Assumptions for Stochastic Models)

1959 to 2017



Historical 5-year (ending 30/6/64 to 30/6/17) compound average annual returns and rates

Source: *Austmod*, net of tax and fees

Presentation

Why?

What?

How? ... briefly

Results ... some of the 82 charts

... just 2 of 30 tables

*(with focus on features and
concepts, rather than values)*

Acknowledgments

Why?

Demand versus supply gap

- in Australia
- for many sectors
- often for commercial reasons
- particularly, data for long term assumptions and
- little documented assumption methodology

Demand “pull”

- Actuaries use investment assumptions in all practice areas
- For premium or contribution rate calculations
- For valuations, capital assessments, investment strategy calculations, etc
- For benefit and other projections

Supply “push”

Valuable 58-year database:

- EFG investment system (1965 to 2009)
- Published indices and rates (8-58 years)

We're keen to see Australian actuaries make greater use of:

- Stochastic models
- Historical simulations
- Auto-correlations
- Economic cycles

What content ?

- (1) Australian investment **performance**
30 June 1959 to 30 June 2017
(annual data, quarterly intervals)
- (2) Investment **assumptions** (realistic) for
stochastic (and deterministic) models

What sectors?

GROWTH SECURITIES

S	Australian shares
I	International shares (unhedged)
H	International shares (hedged)
Q	Property trusts
P	Direct property

INTEREST INCOME

F	Australian fixed interest
J	International fixed interest (hedged)
G	Government semis (0 to 3 yrs)
N	Inflation-linked bonds (0 + yrs)
L	Loans (floating rate) / Credit
C	Cash

FINANCIAL INDICATORS

X	CP <u>I</u> ndex (annual increase)
W	AW <u>O</u> TE (annual increase)
B	90-day <u>b</u> ill rates (<u>mid-year</u>)
D	10-year bond <u>r</u> ate (<u>mid-year</u>)

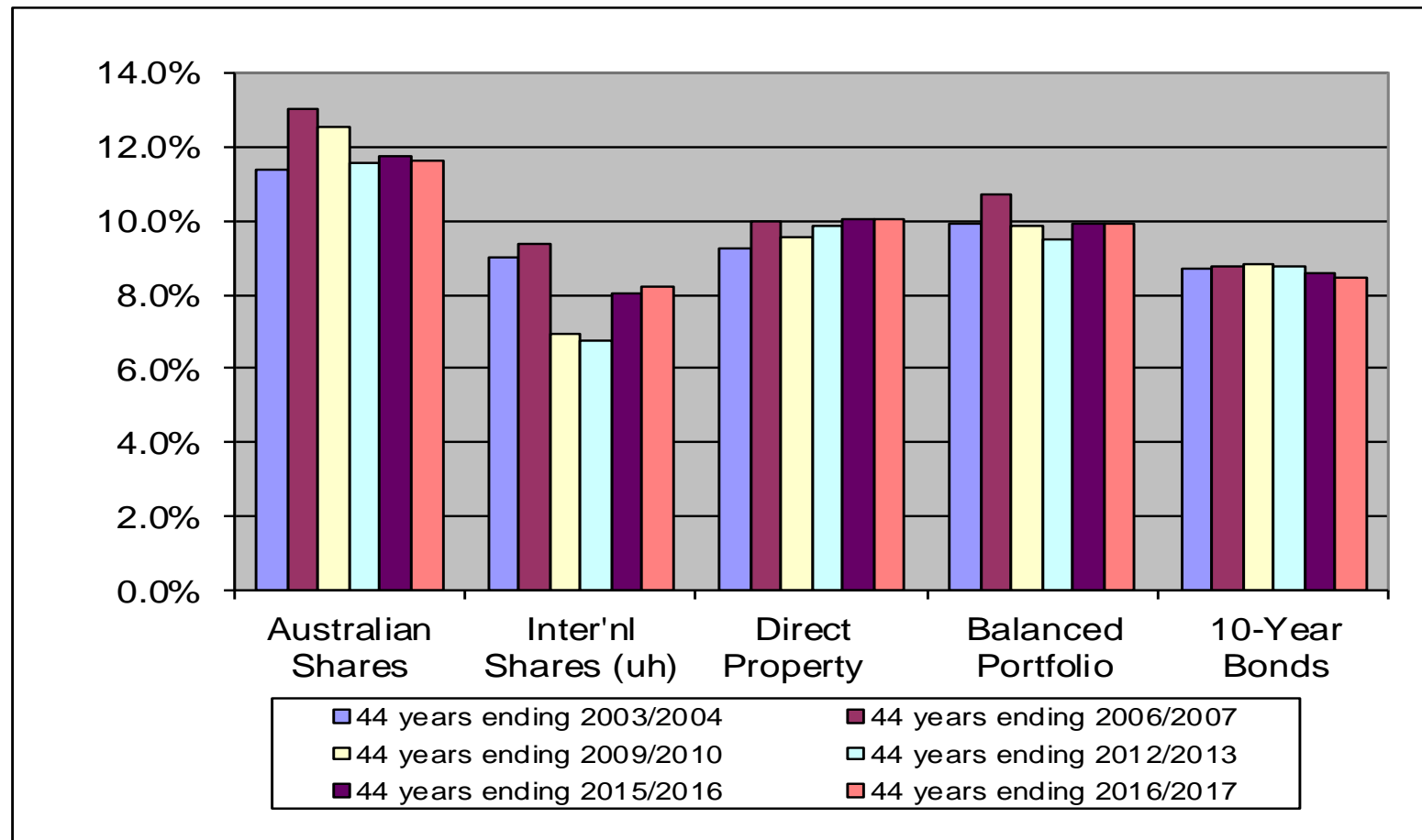
Section 3 details
Section 4 backdating

What results?

- Risk margins (over 10-year bond rates)
- Coefficients of variation (of rates)
- Skewness (of **forces**)
- Kurtosis (of **forces**)
- Cross-correlations (of **forces**)
rank and standard
- Auto-correlations (of **forces**)

- Arithmetic means (44 years)
- Compound means (44 and 40 yrs)
- Standard deviations (44 years)
- “Balanced” and “Capital stable”
- Gross/net of superannuation **tax**
- Gross/net of wholesale passive **fees**

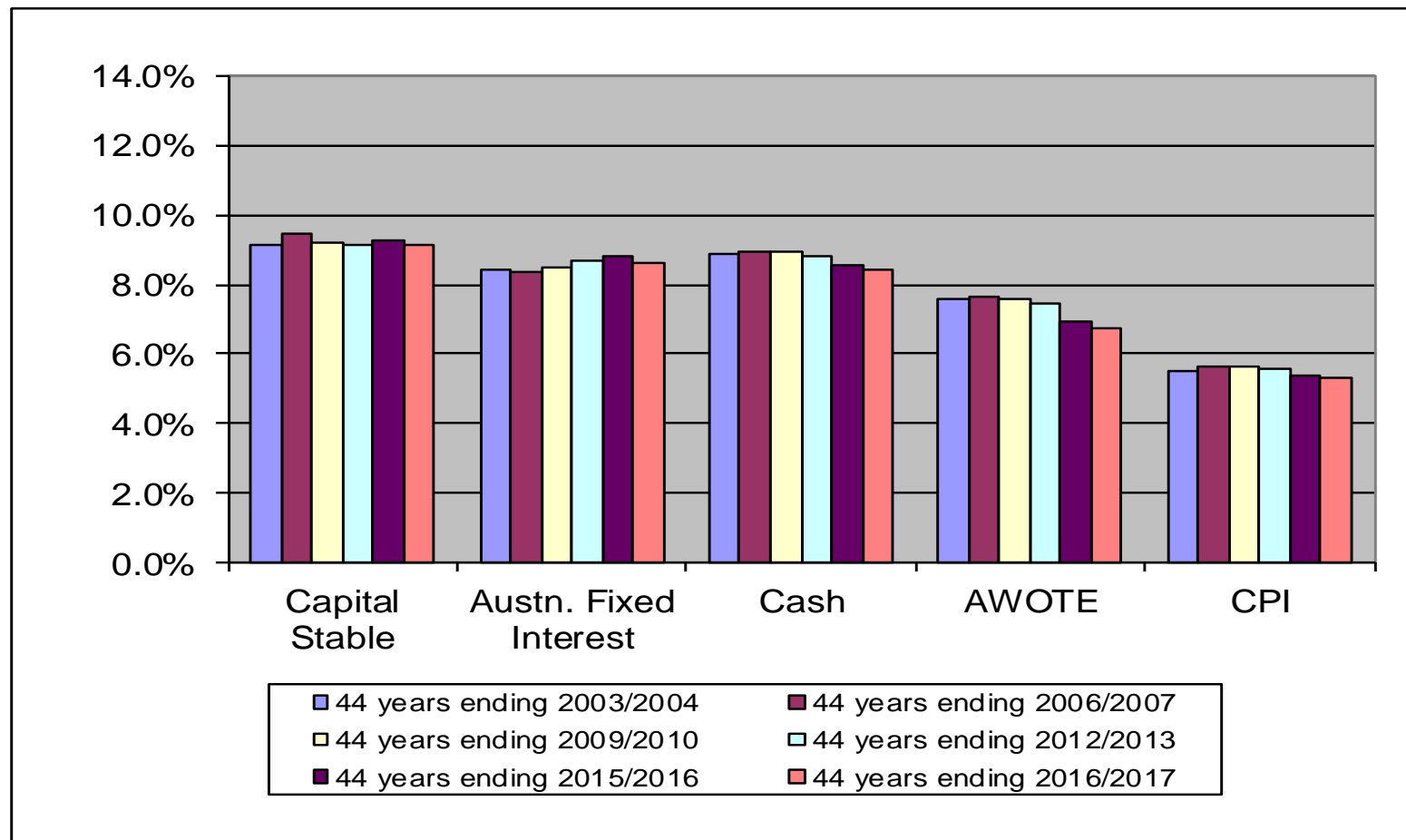
44-year Average (compound) Returns pa



2003/2004 (for example) indicates average of yrs. ending 30/9/03, 31/12/03, 31/3/04 & 30/6/04

Figure 8.1, before tax and fees

44-year Average (compound) Returns pa



2003/2004 (for example) indicates average of yrs. ending 30/9/03, 31/12/03, 31/3/04 & 30/6/04

Figure 8.1, before tax and fees

Impact of GFC on Balanced Portfolio

Figure 9.1

Unit price, before
tax and fees

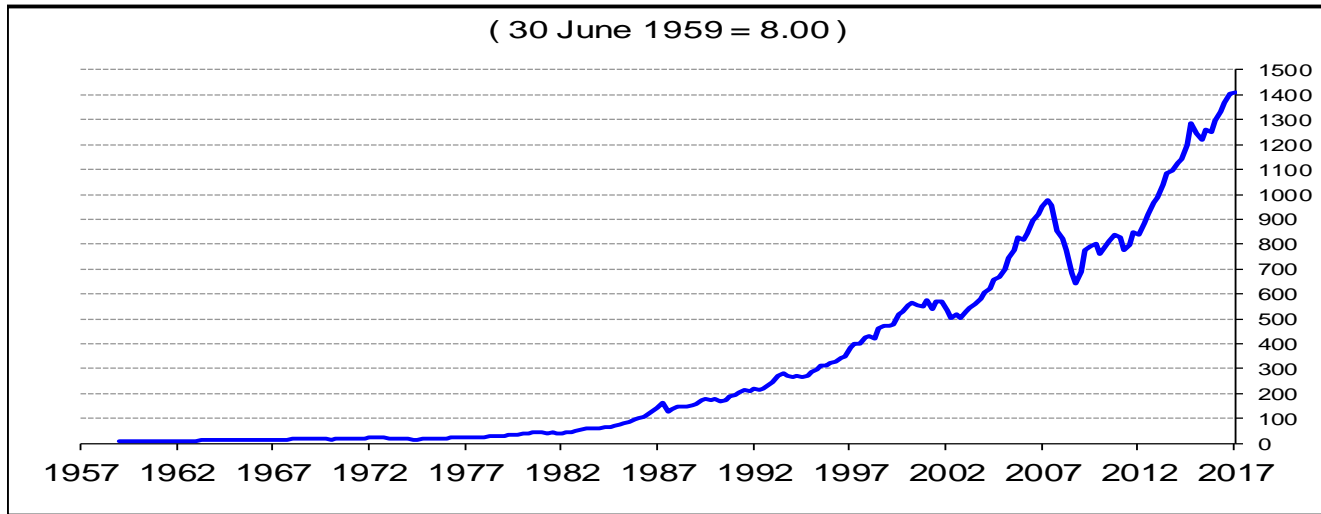
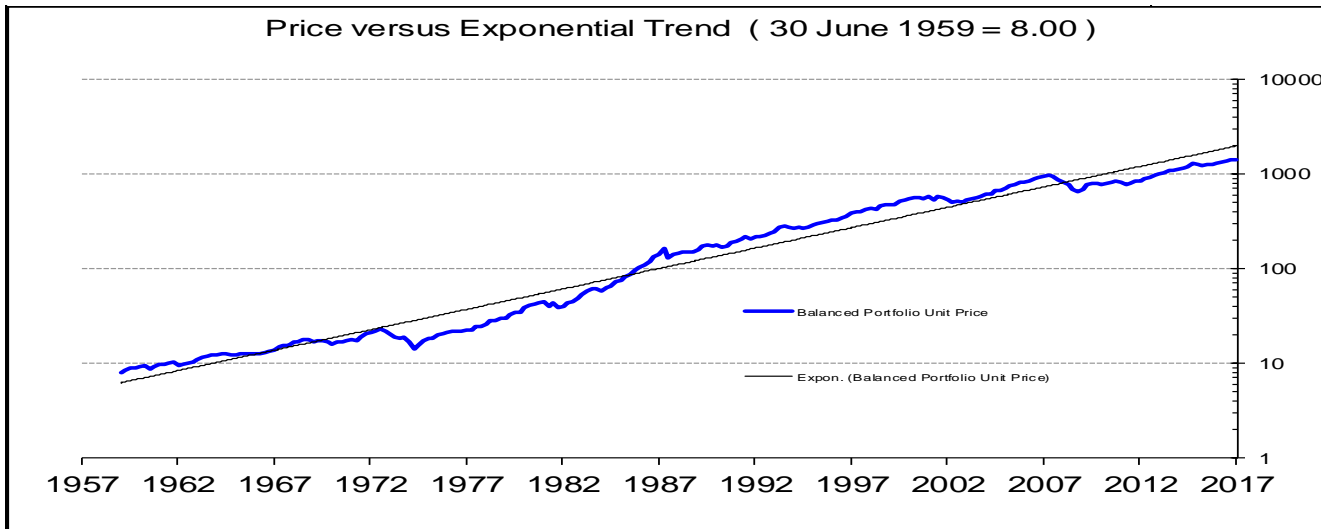


Figure 9.2



Balanced Portfolio “Discounted Price”

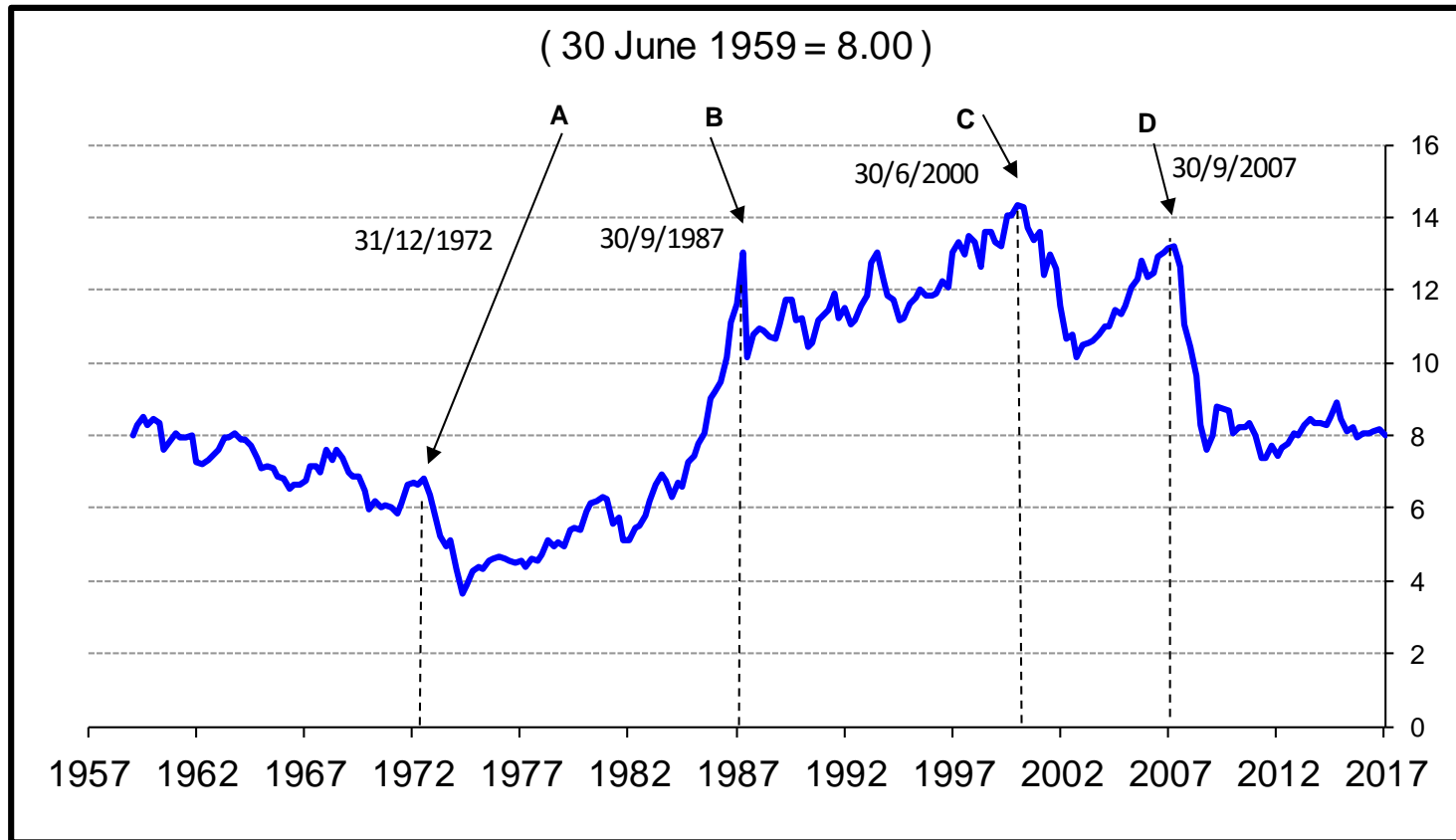


Figure 9.3

A 31 Dec 1972

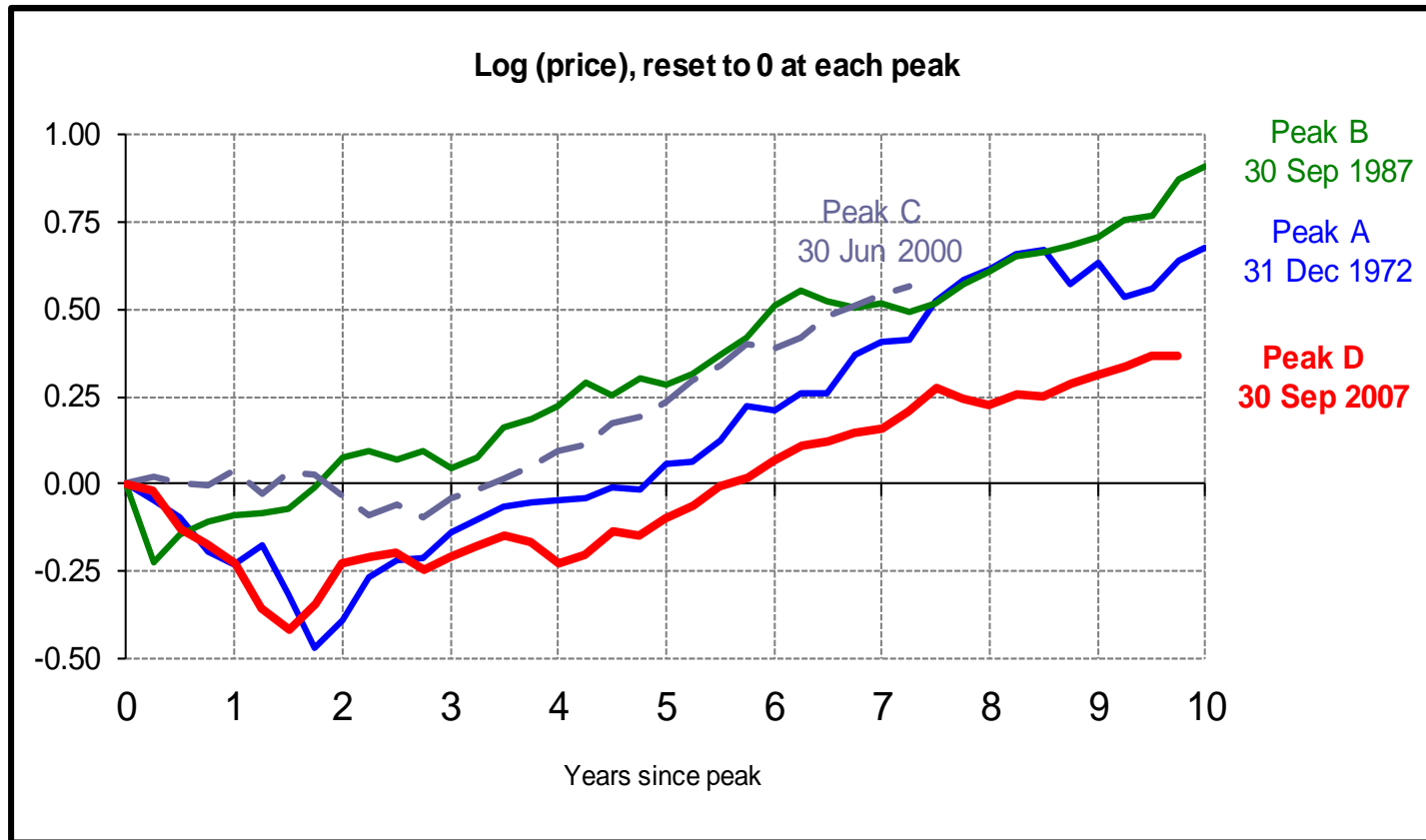
B 30 Sep 1987

C 30 Jun 2000

D 30 Sep 2007

Log Price Reset to 0 at Each Peak

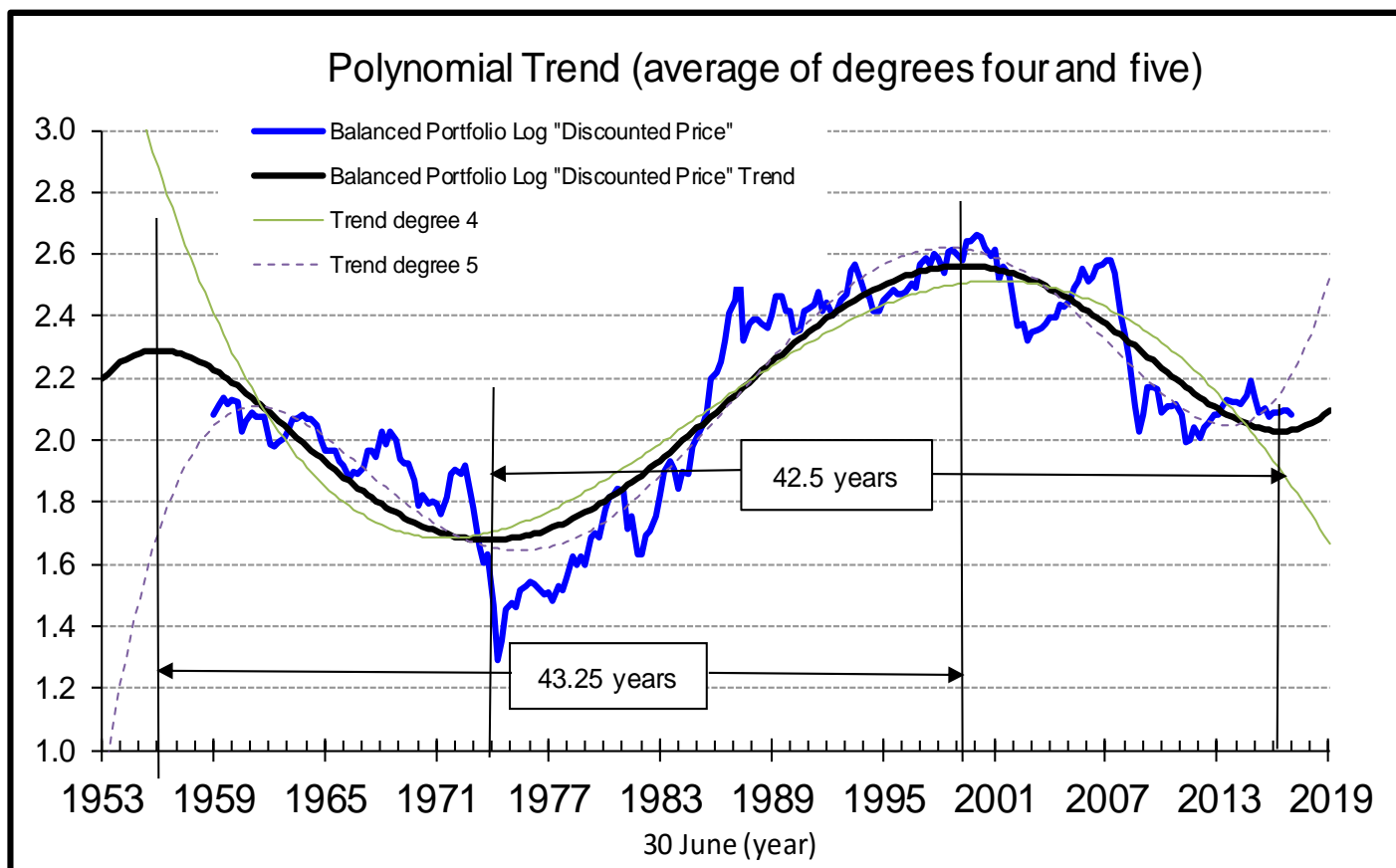
Figure 9.4



**Balanced
Portfolio
with
Price
reset**

Balanced Portfolio Log “Discounted Price” and Trend

Figure 9.5



Bonds

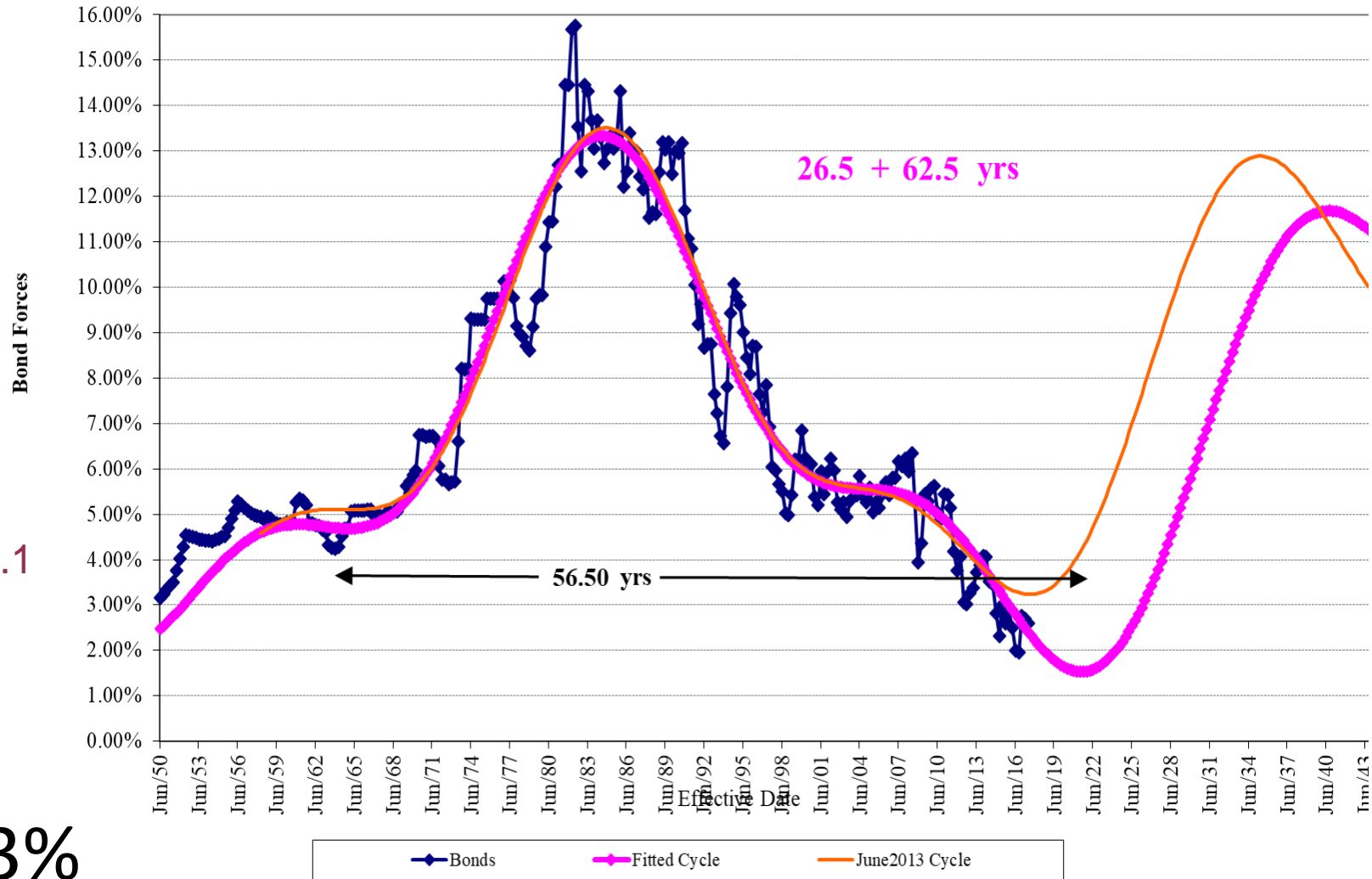


Figure 5.1

93.3%

CPI

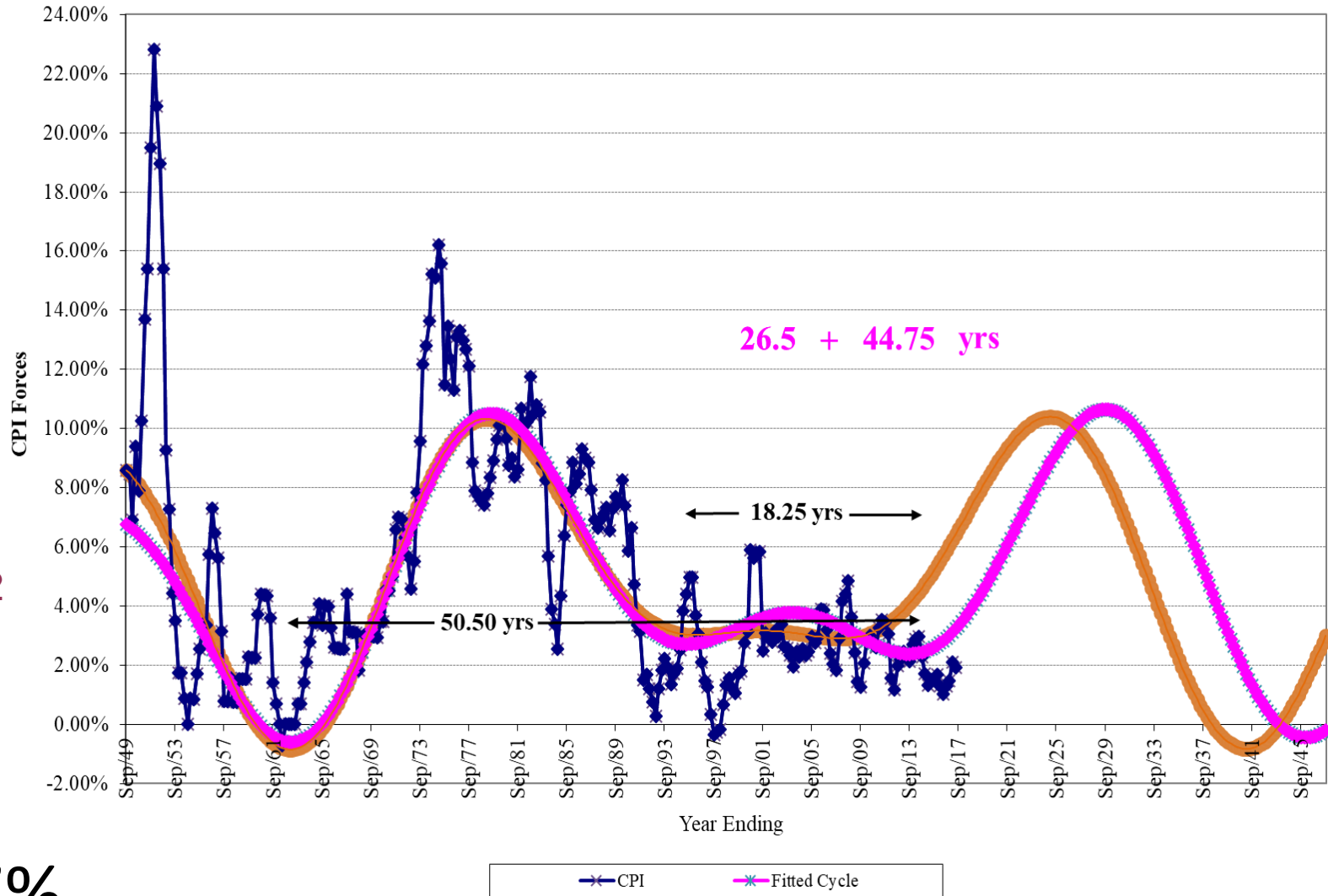


Figure 5.2

56.7%

AWOTE

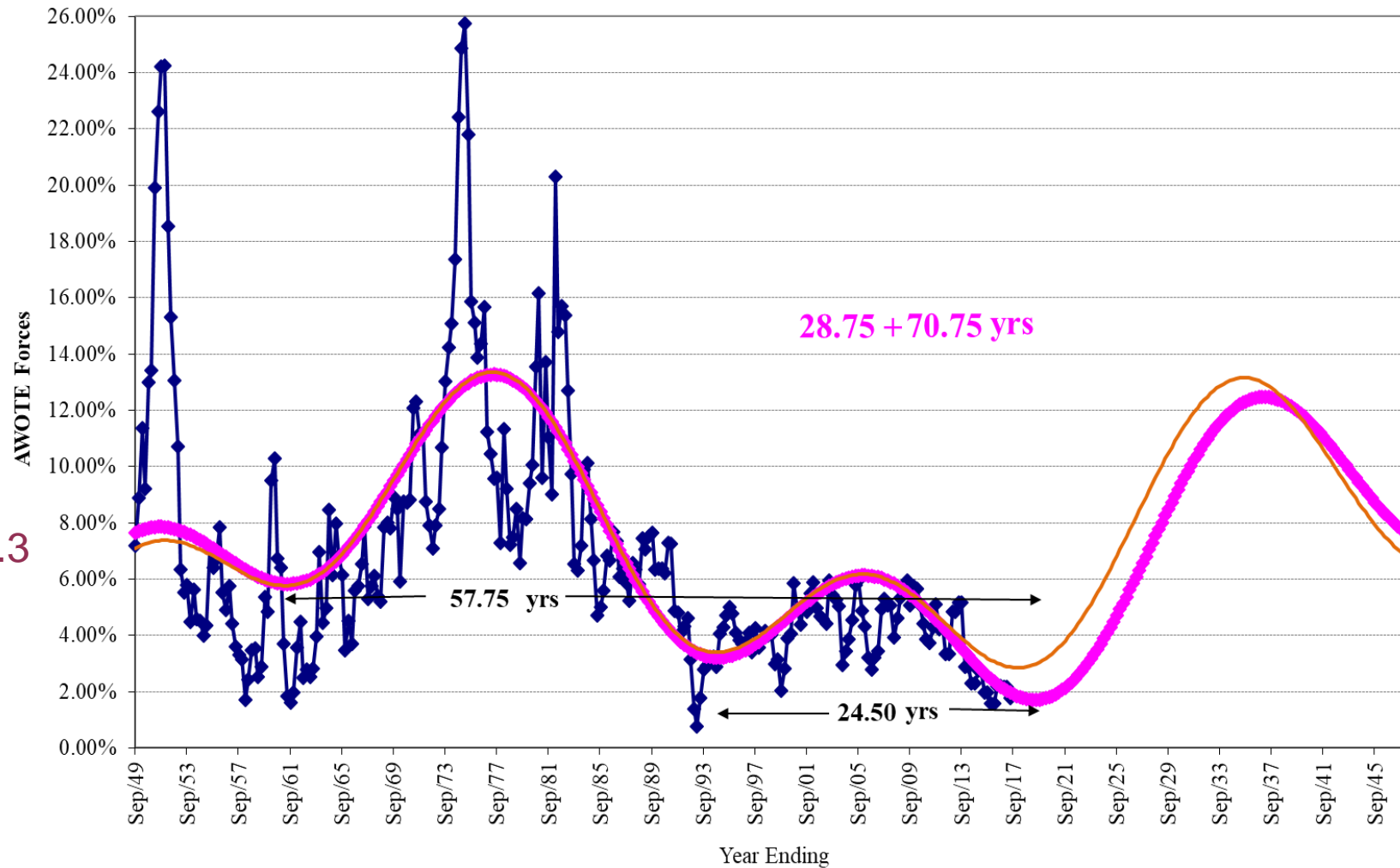
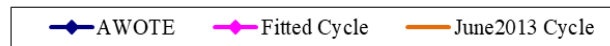


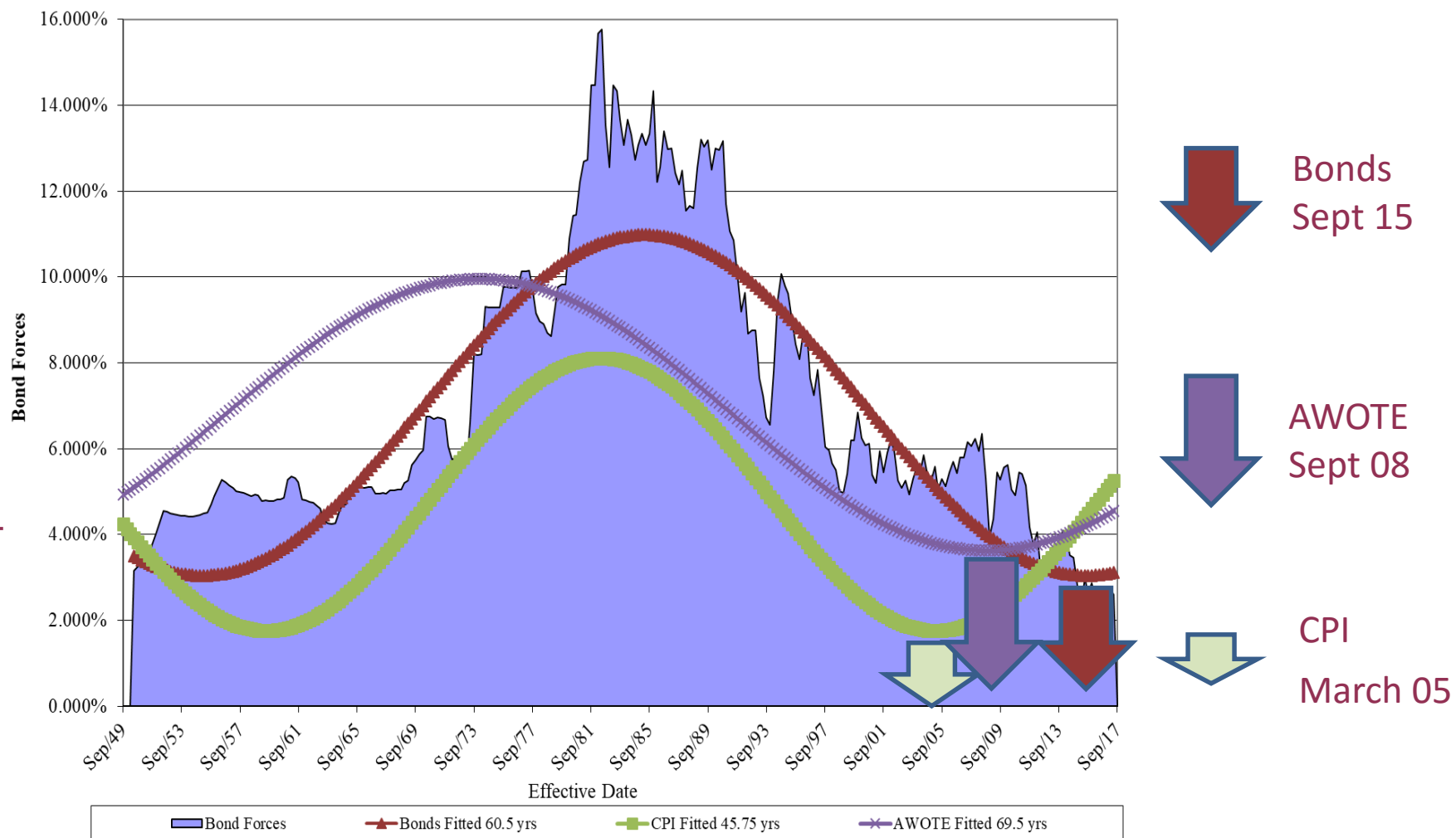
Figure 5.3

56.0%



Bonds, CPI and AWOTE

Figure 5.4



Australian Shares

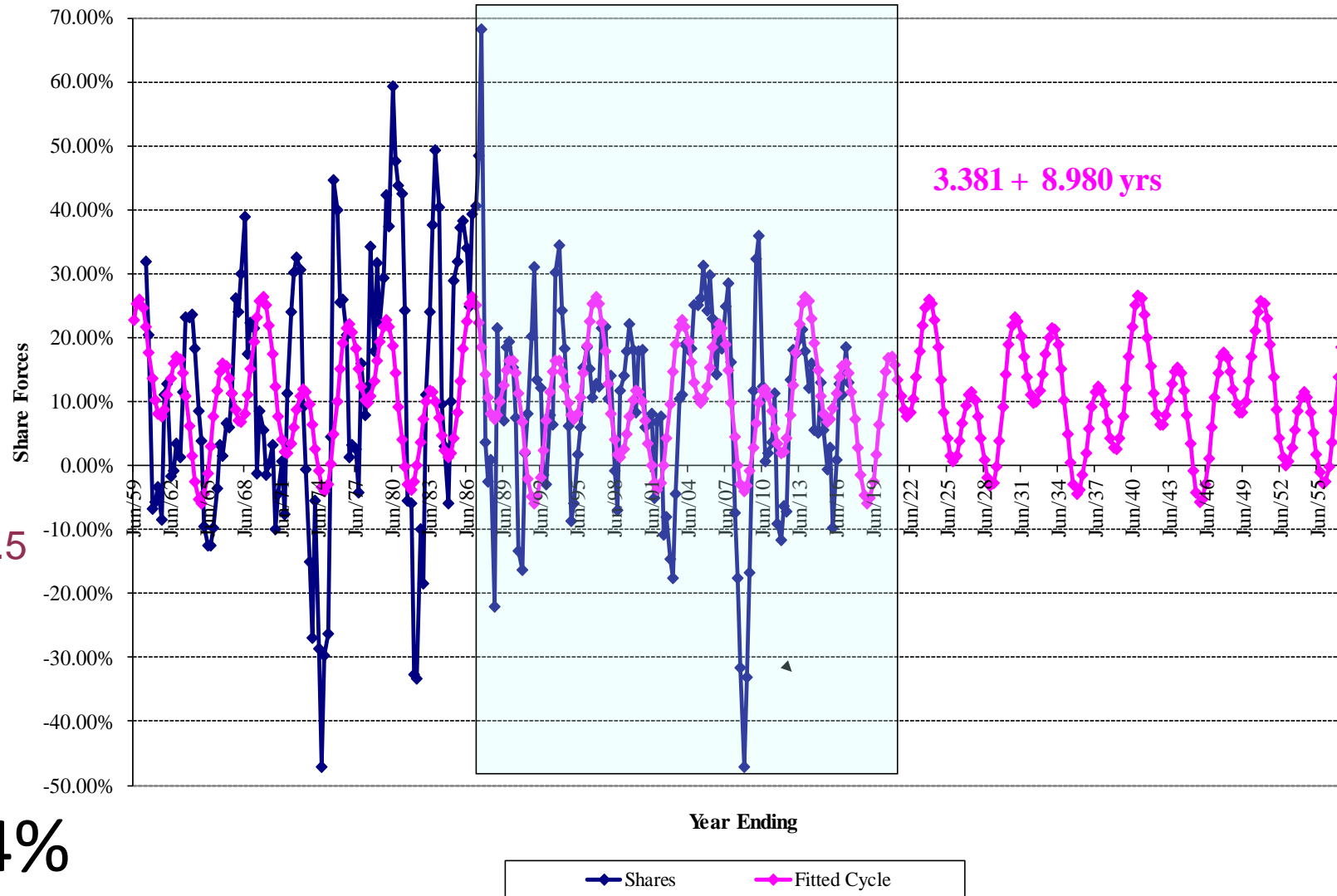
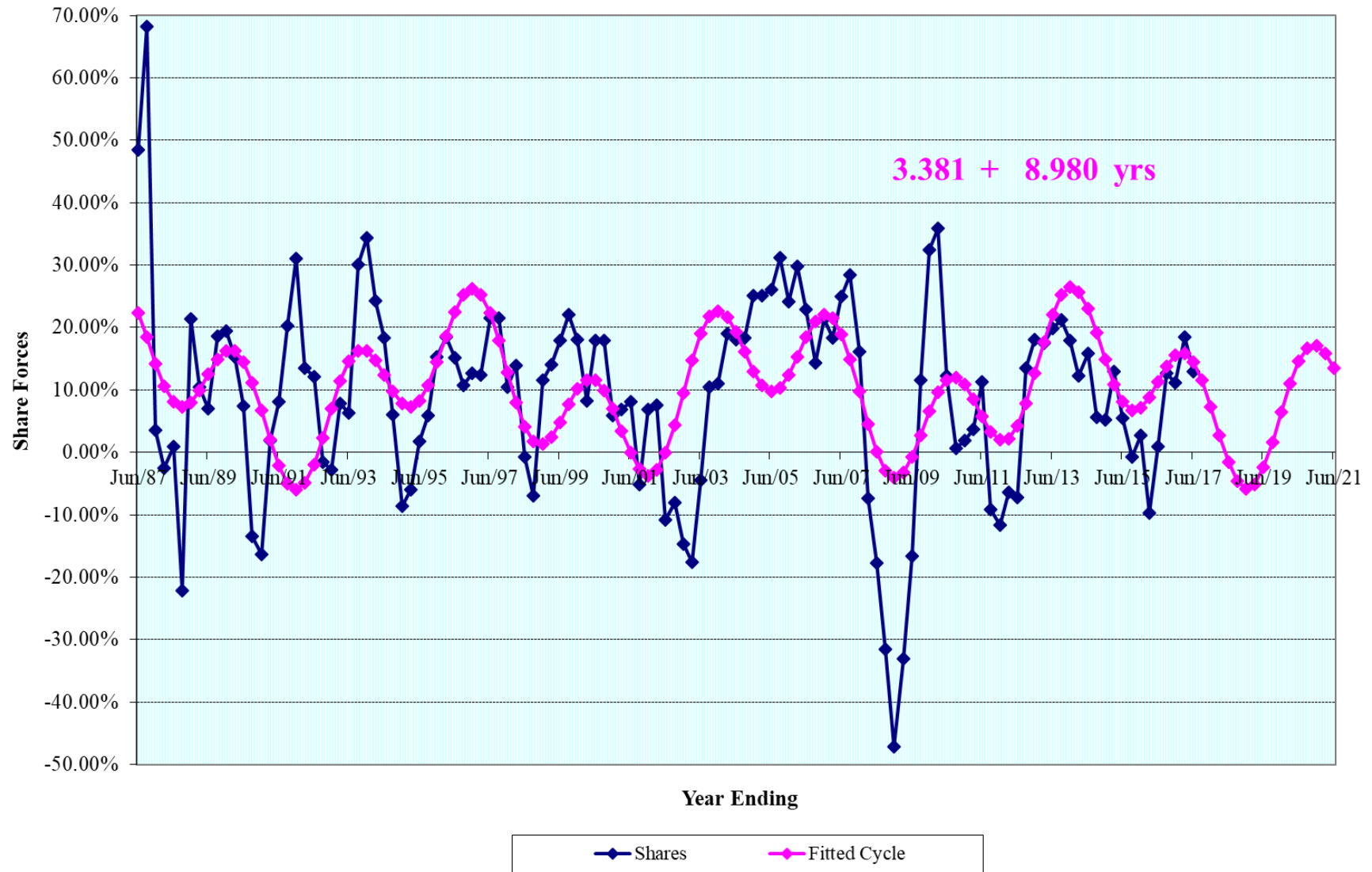


Figure 5.5

20.4%

Shares (close-up)



QUESTIONS ?

- Demand and supply
- Database
- 15 sectors
- Backdating
- 44-year returns
- GFC
- Cycles
- Sine curves

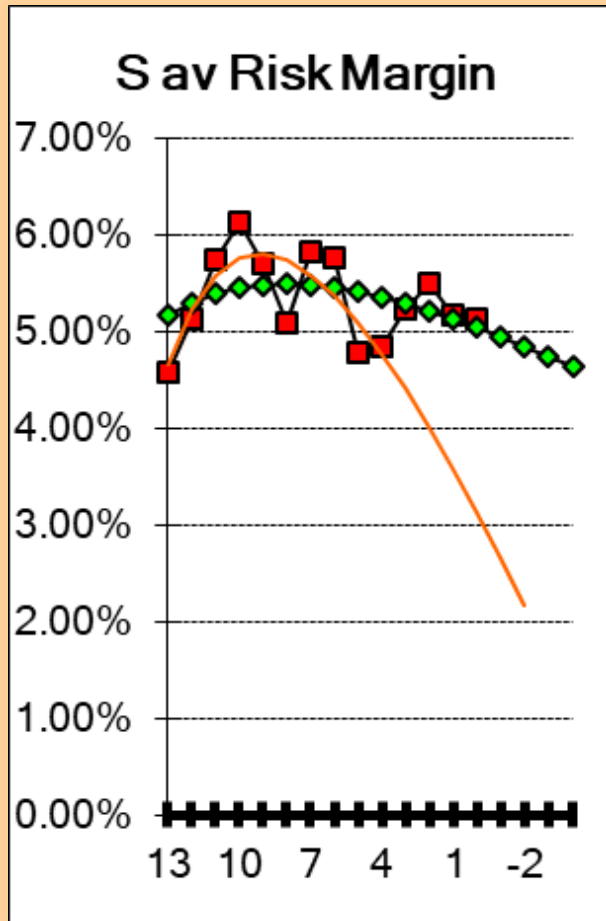
How?

Assumptions - Methodology

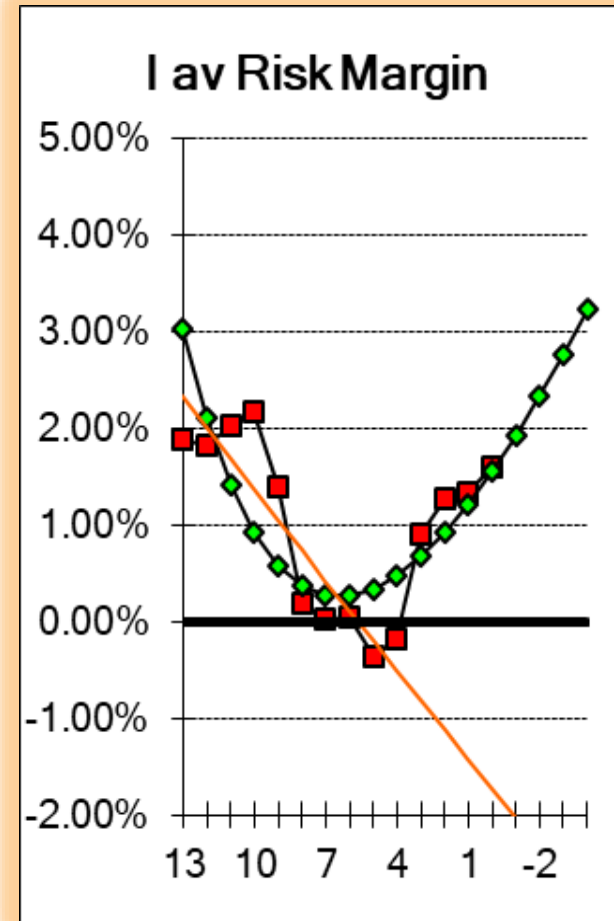
- Step 1** Sep, Dec, March, June data
- Step 2** determine calculation periods
(see previous slides, 44 and 40 years)
- Step 3** annual statistics for the step 2 periods
- Step 4** 14 “running” averages of 4 quarter-end results
- Step 5** weighted quadratic trend and 6 year projection
- Step 6** year - 2 (and judgment)

see Section 2

Results: Risk Margins over 44 years



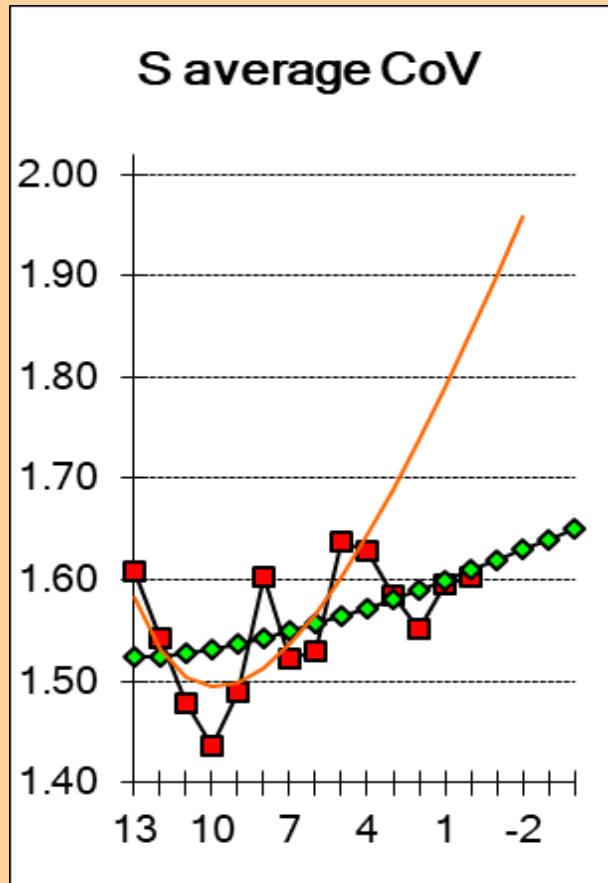
[4.4%]



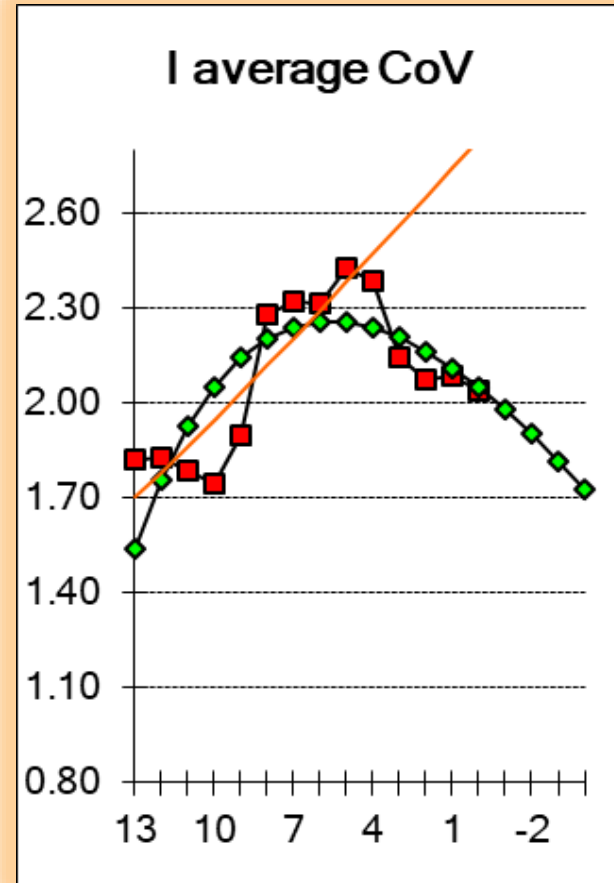
[3.0%]

Figure 6.1

Results: CoV's over 44 years

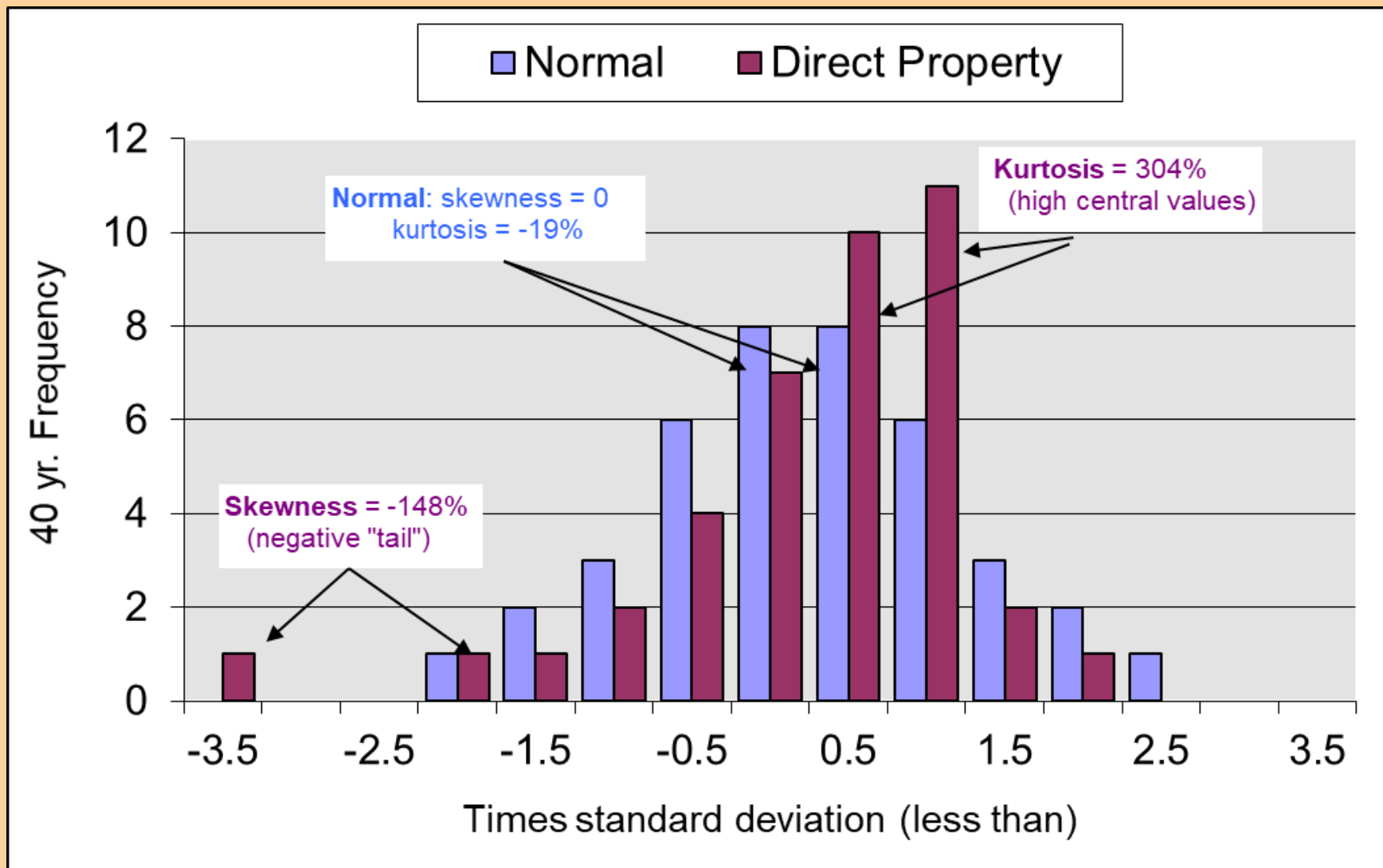


[1.616]

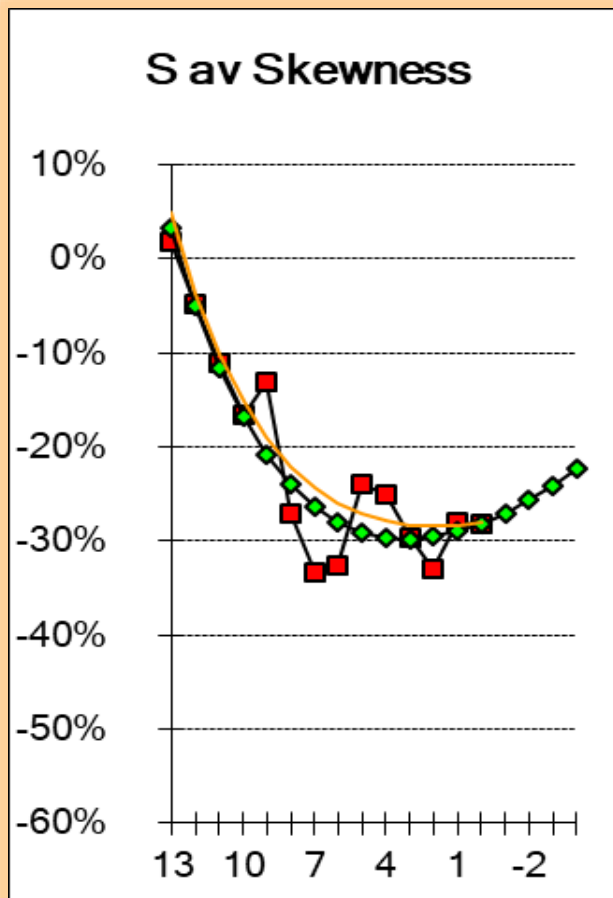


[1.623]

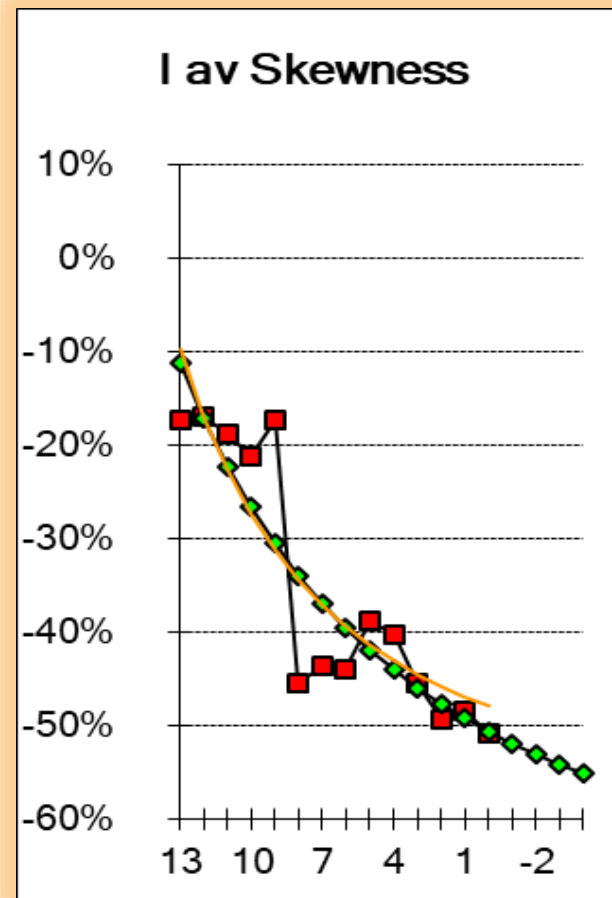
Skewness and Kurtosis



Results: Skewness over 44 years

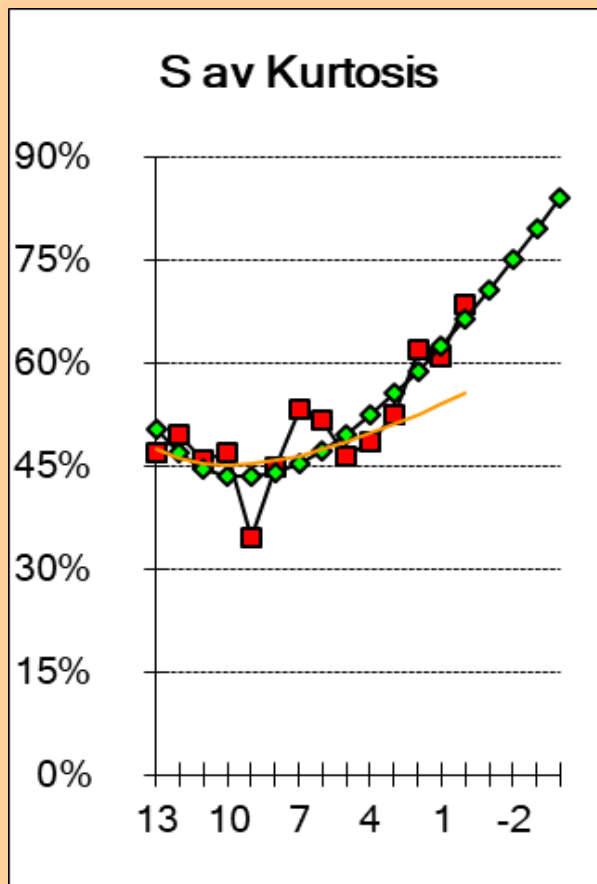


[-26%]

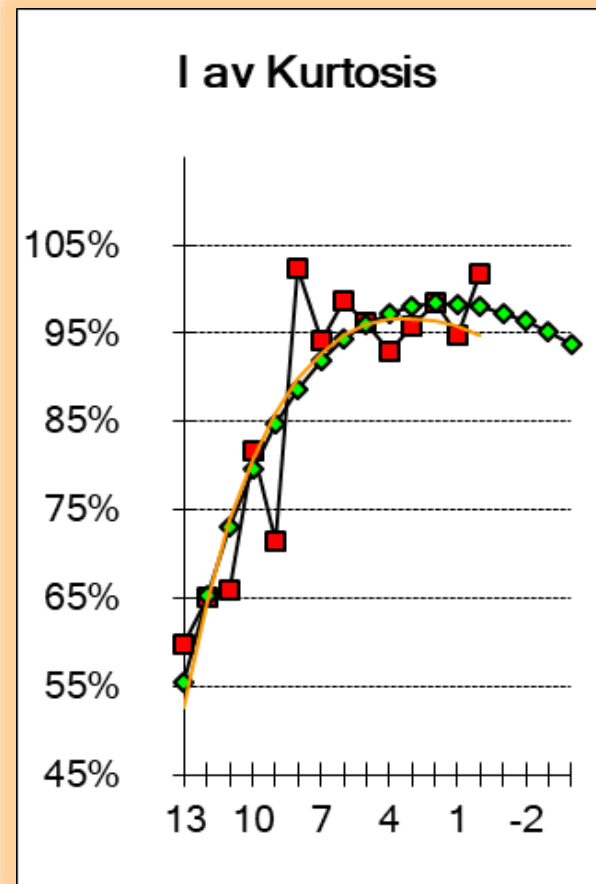


[-53%]

Results: Kurtosis over 44 years



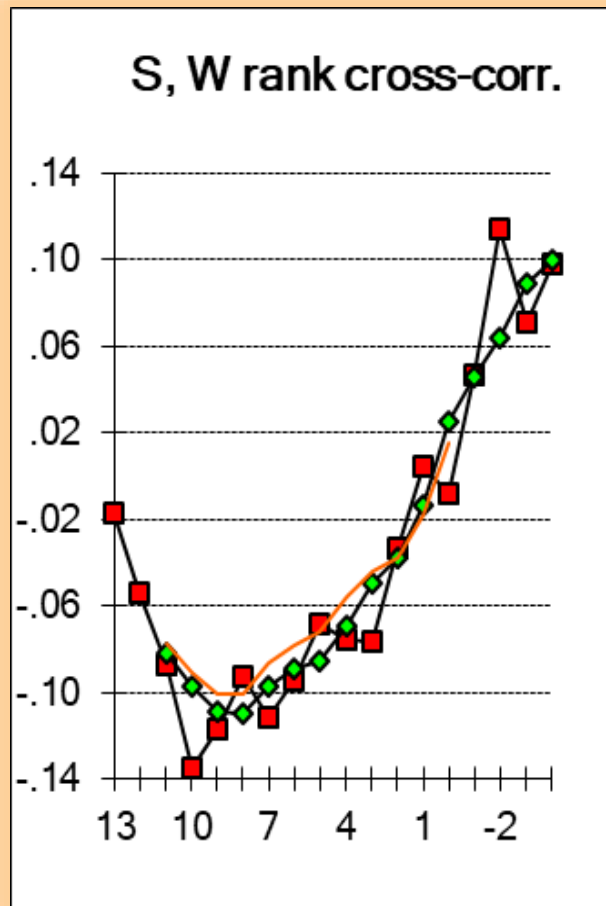
[75%]



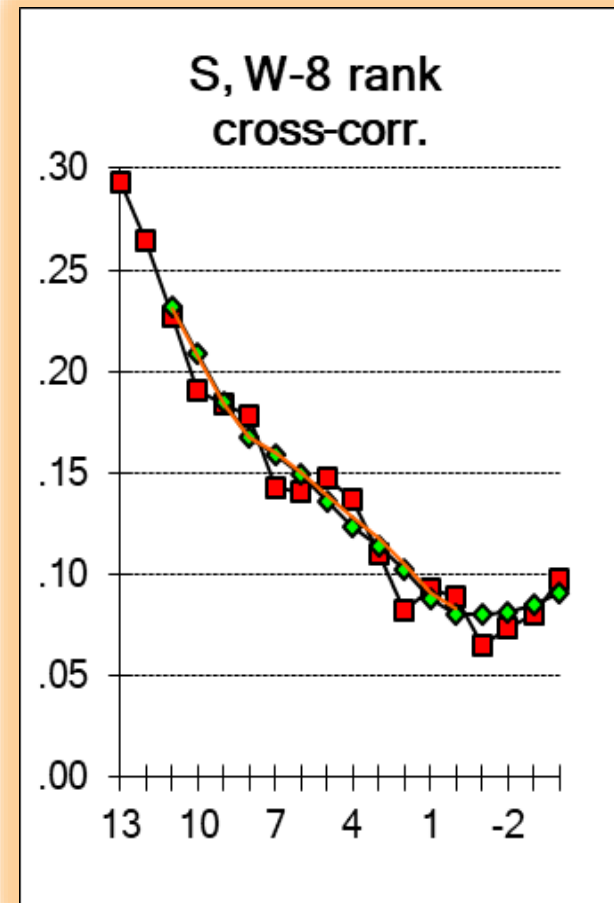
[96%]

Figure 12.1

Results: Rank Cross-correlations over 44 years



[6%]



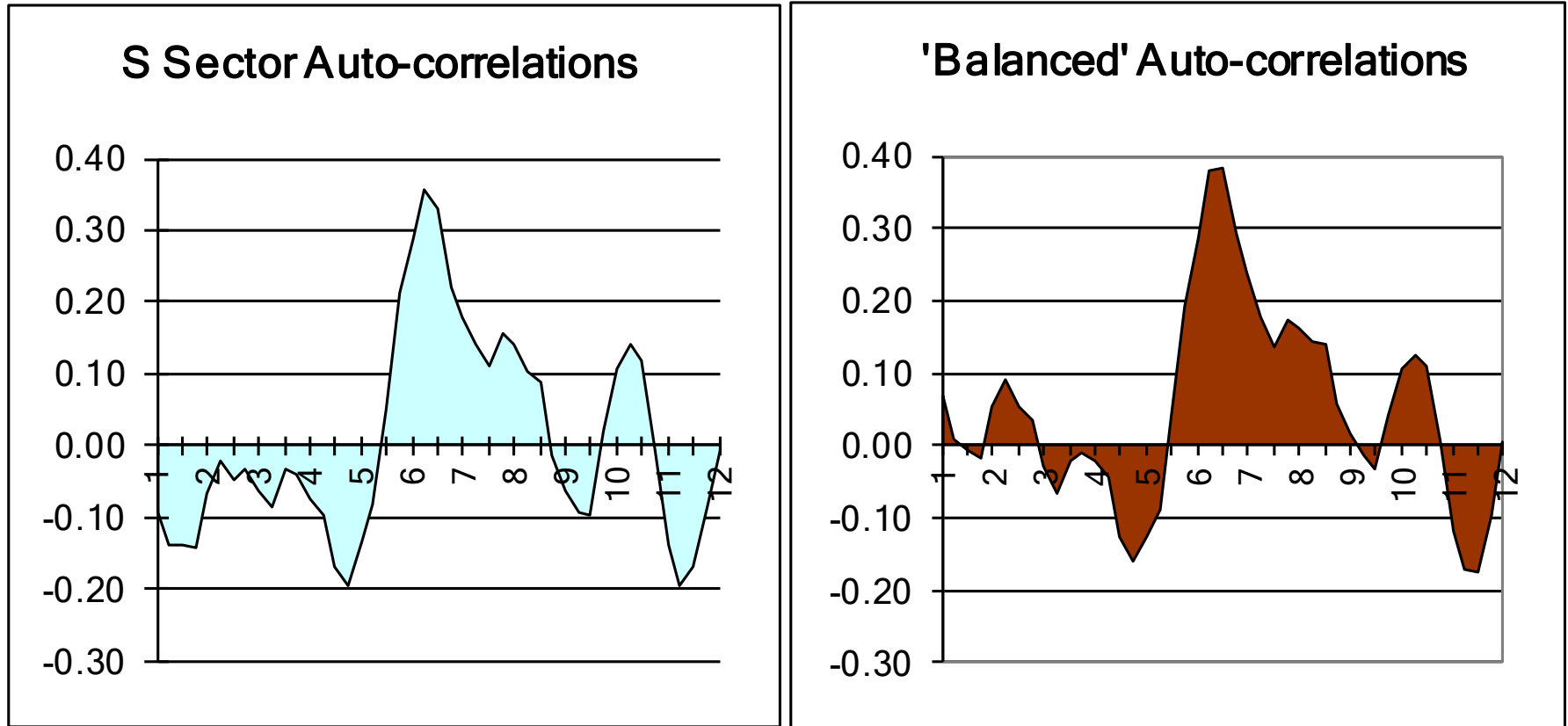
[+8%]

Cross-correlation Assumptions (abridged)

	CROSS-CORRELATIONS @ 2 YRS (5-point average, rounded)						
SECTOR	Austrn. Shares	Listed Property	Fixed Interest	Cash	Direct Property	CPI	AWOTE
Austrn. Shares	1	.49	-.06	.21	.13	.08	.06
Listed Property	.49	1	.25	.13	.18	-.04	.04
Fixed Interest	-.06	.25	1	.41	-.03	.11	.17
Cash	.21	.13	.41	1	.41	.71	.69
Direct Property	.13	.18	-.03	.41	1	.55	.44
CPI	.08	-.04	.11	.71	.55	1	.80
AWOTE	.06	.04	.17	.69	.44	.80	1

Section 13 and Table 16.3

Auto-correlations over 40 years



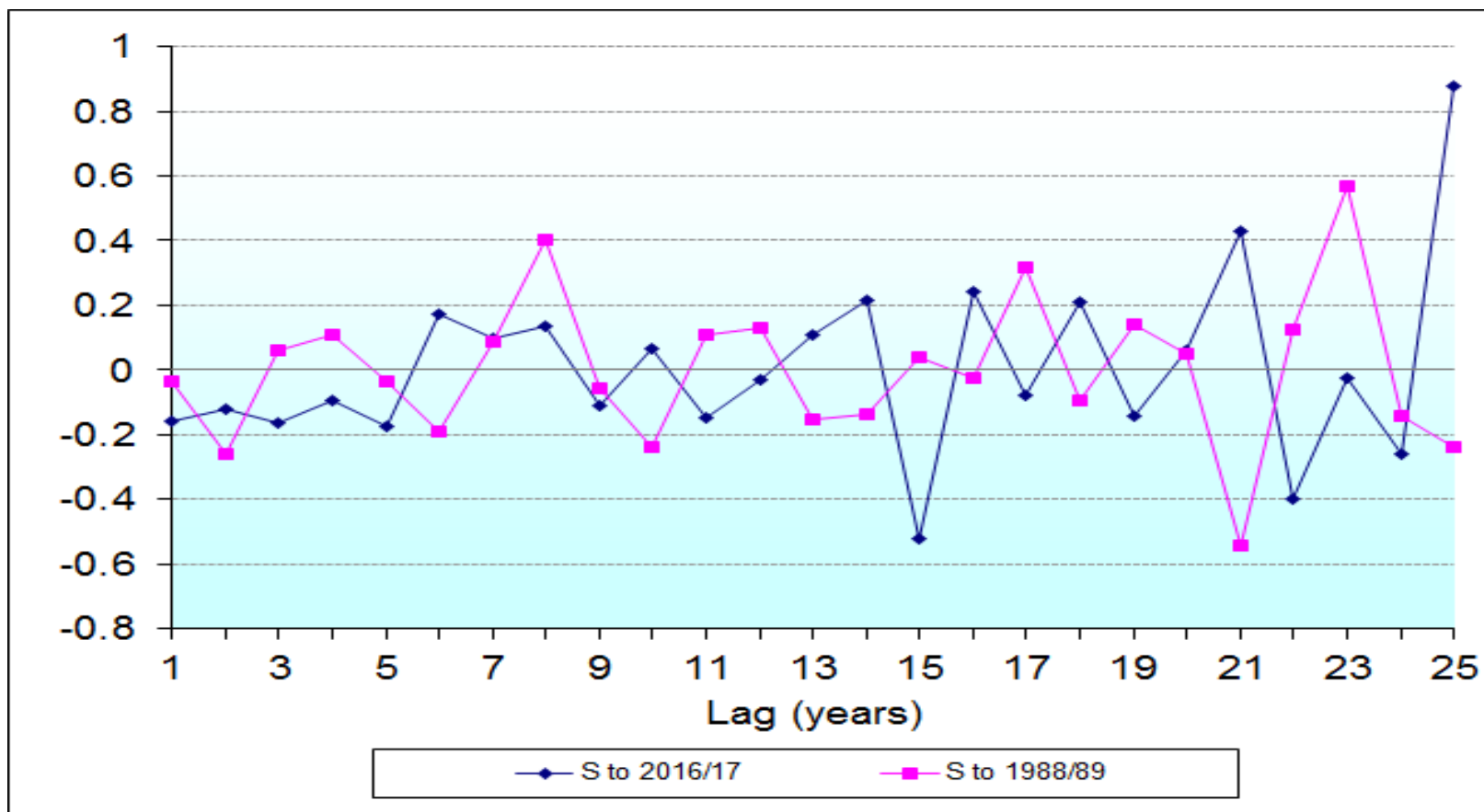
Lags 1 to 12 years

Figure 15.1

Auto-correlations over 28 years

Australian Shares

Figure 15.3



Auto-correlations over 33 years

10-year Bonds

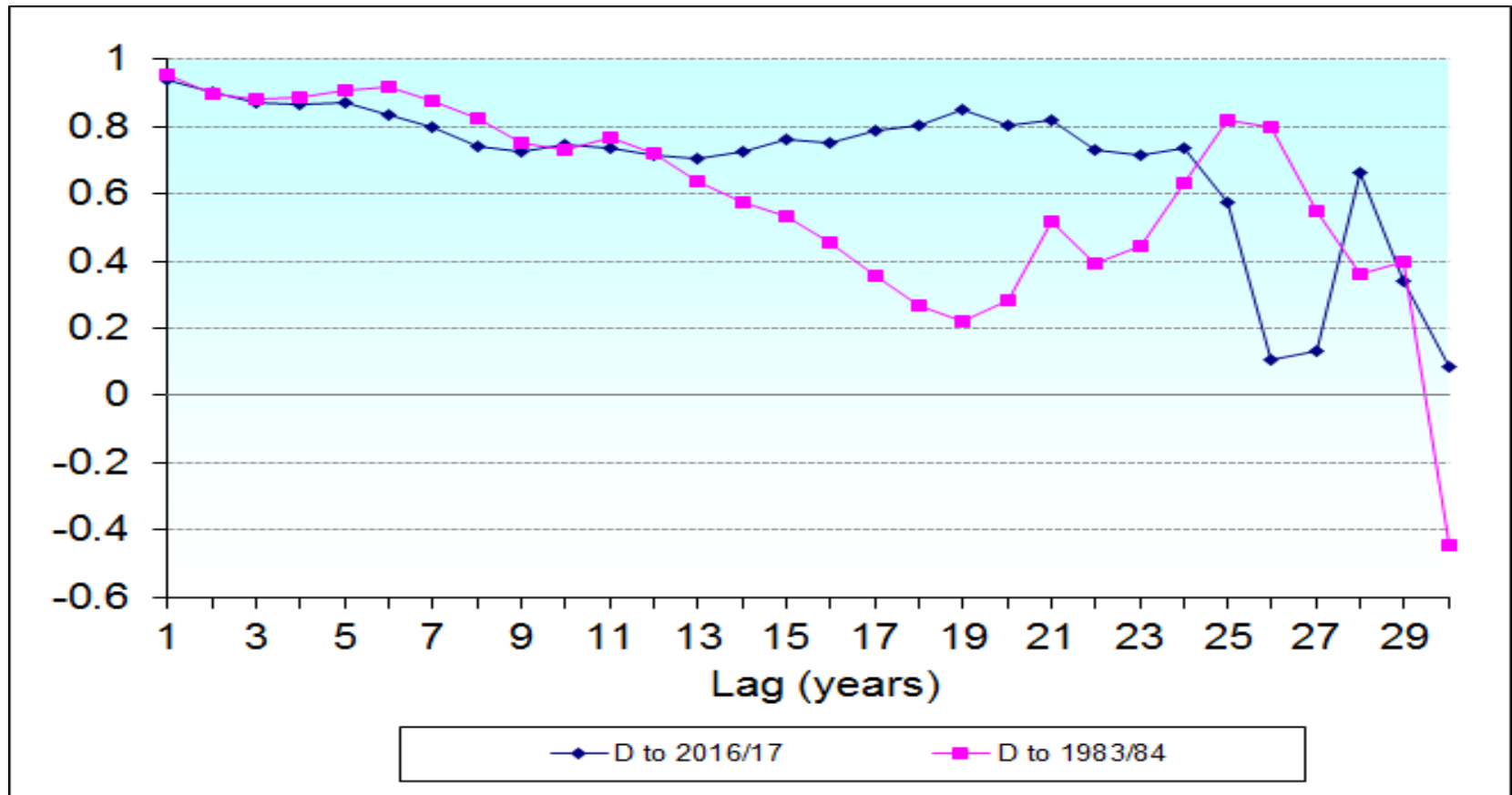
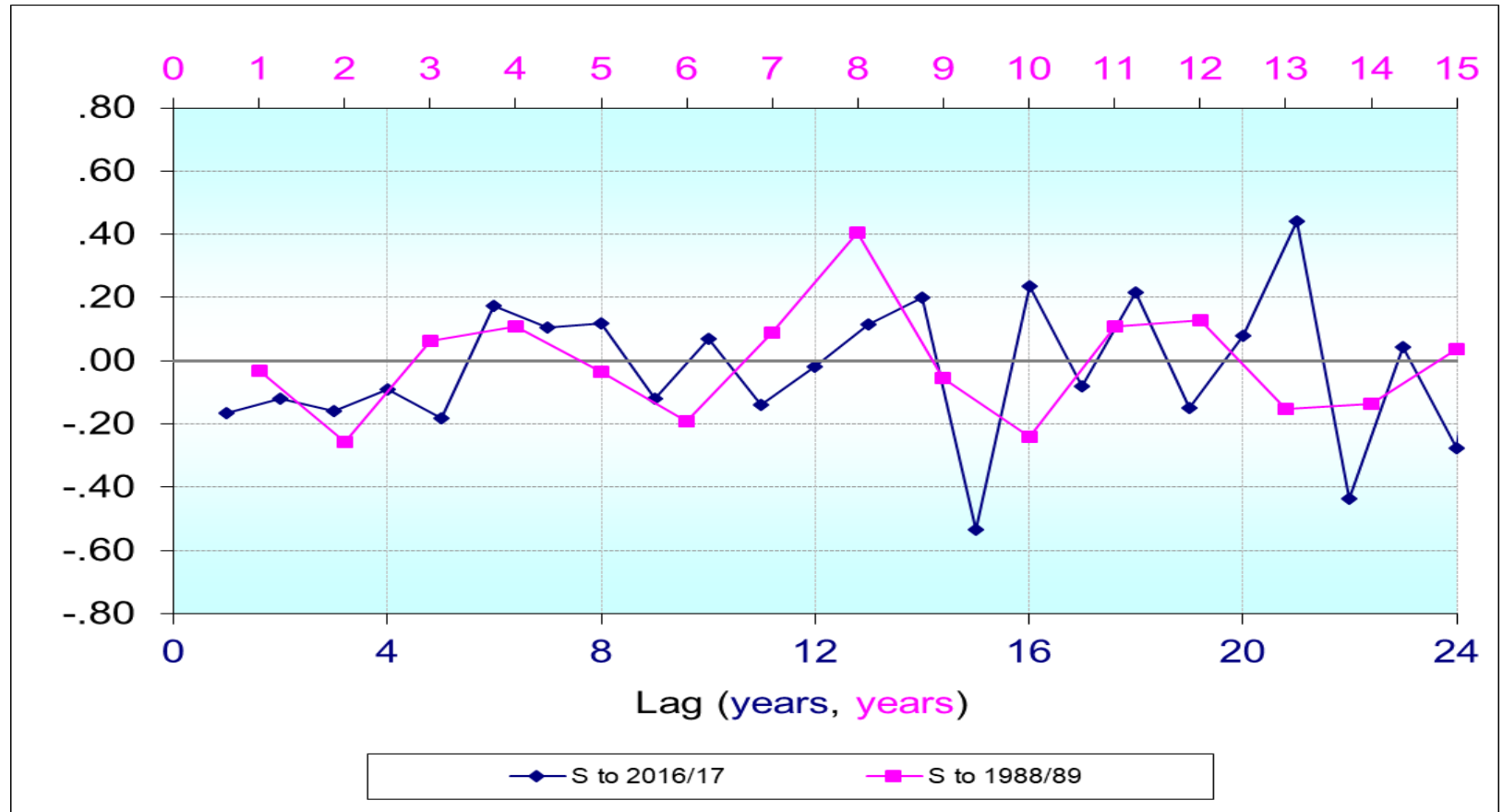


Figure 15.3

Auto-correlations over 28 years S to 2016/17 versus S to 1988/89

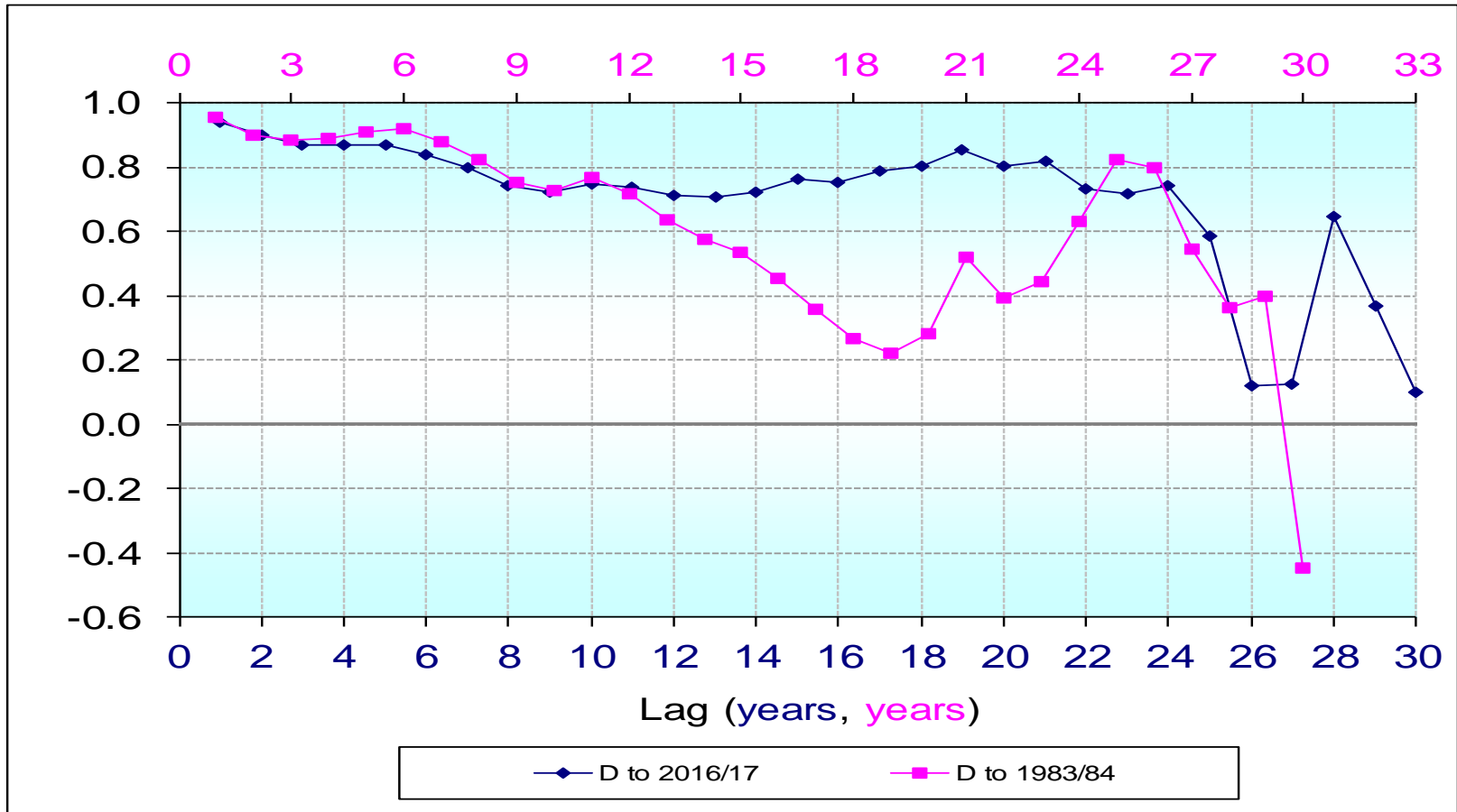
Figure 15.4



Auto-correlation features for last 28 yrs occurred more slowly

Auto-correlations over 33 years

D to 2016/17 versus D to 1983/84



Auto-correlation features for last 33 yrs occurred more quickly

Auto-correlations over 40 years

Australian Shares

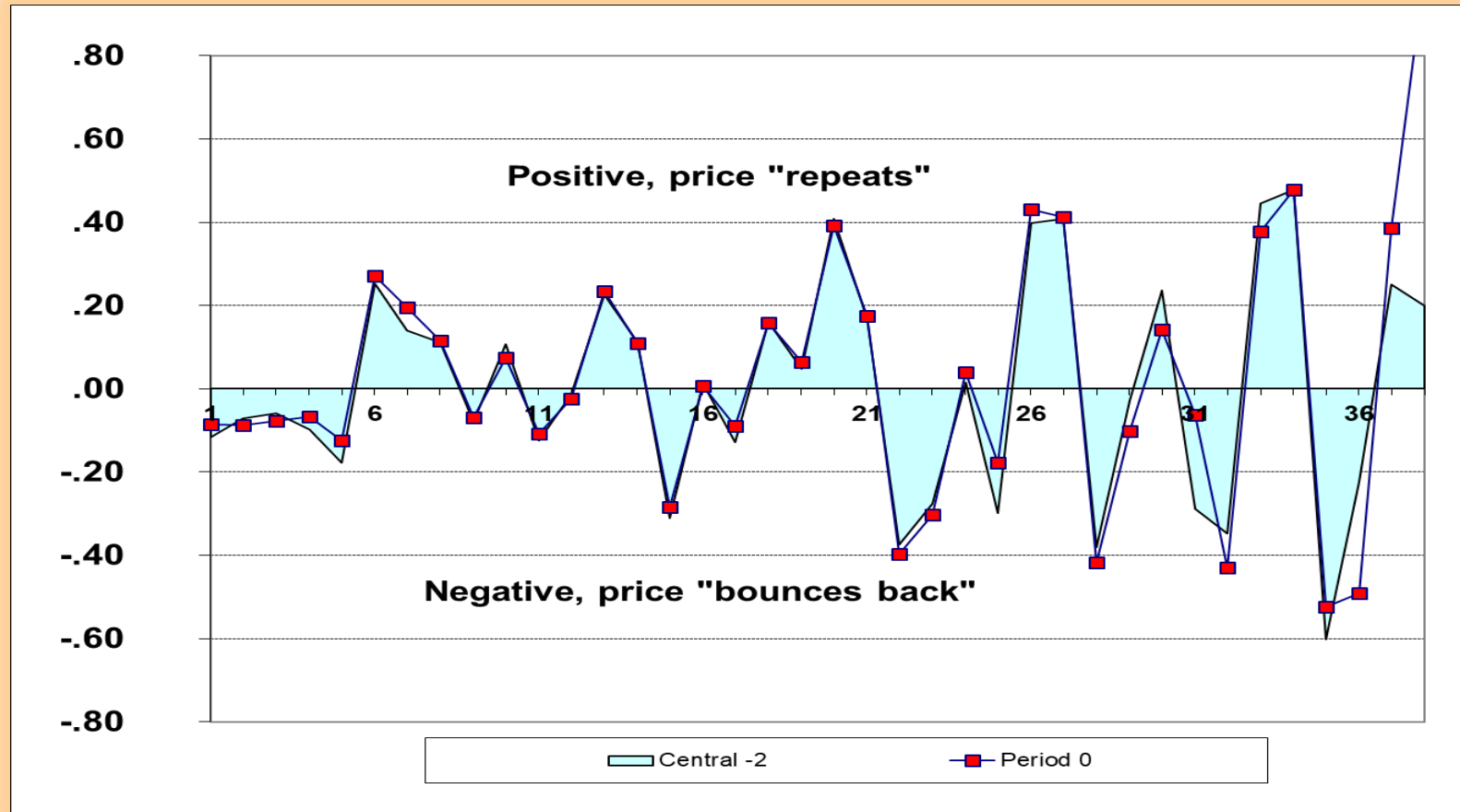
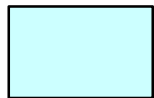


Figure 15.5

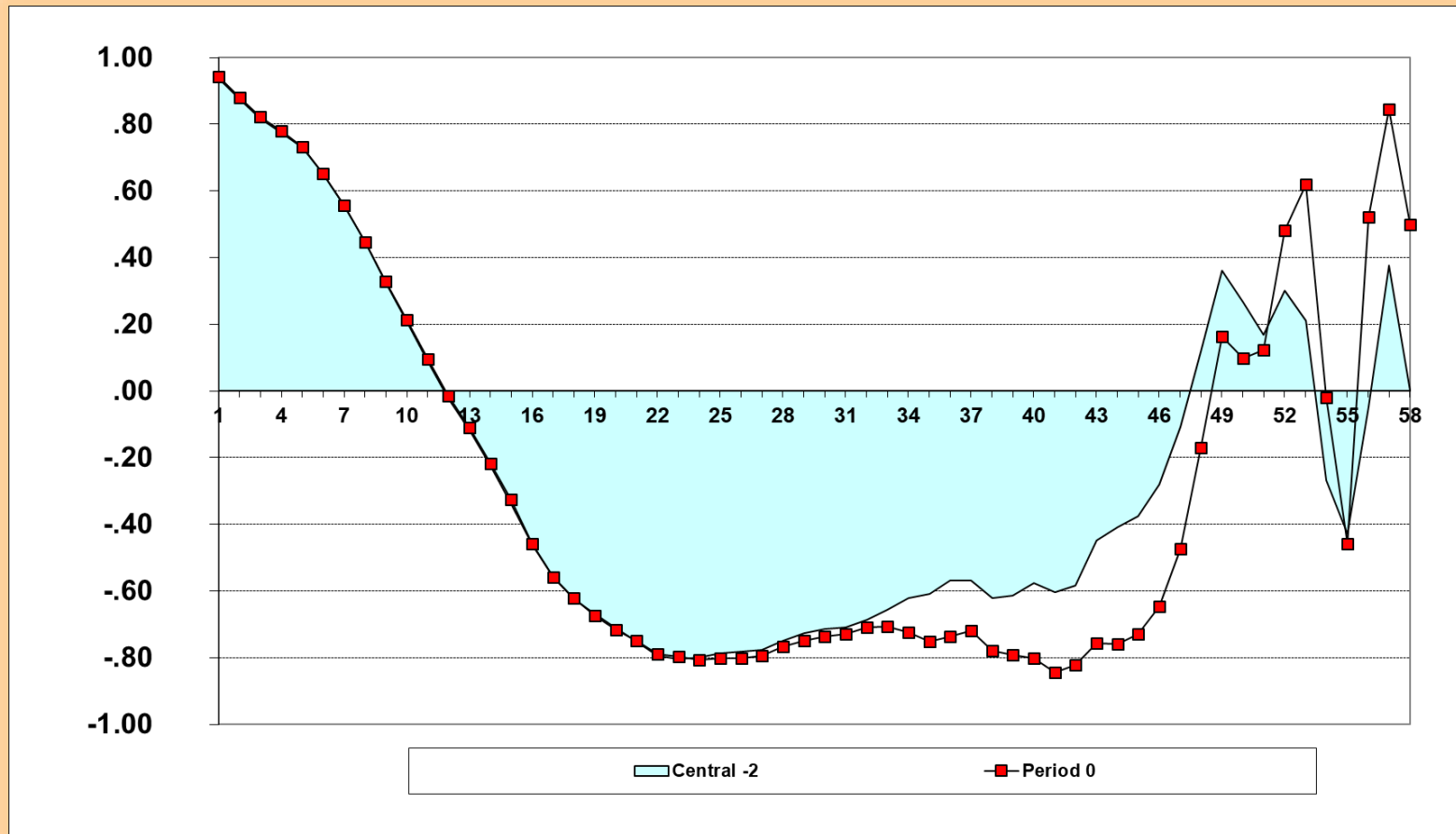
Auto-correlations over 60 years

10-year Bonds



Moves
to the
left

Figure 15.6



Assumptions – Changes in Means

Section 6.12

Sector		NEW	OLD	Change
S	Shares	9.9%	10.0%	-0.1%
I	Int'l Shrs	8.5%	8.6%	-0.1%
Q	Prop Trust	8.5%	8.6%	-0.1%
P	Direct Prop	7.3%	7.5%	-0.2%
H	Hedged IS	8.6%	8.7%	-0.1%
L	Loans/credit	7.1%	7.2%	-0.1%
F	Fixed Int	6.2%	6.4%	-0.2%
G	Semi-govt	6.2%	6.4%	-0.2%
J	Int'l Fxd Int	6.0%	6.2%	-0.2%
C	Cash	5.3%	5.8%	-0.5%
N	Infln Linked	7.0%	7.0%	0.0%
Balncd	Balanced	7.89%	8.03%	-0.14%
CapStb	Cap Stable	6.57%	6.81%	-0.23%
B	Bills	5.30%	5.80%	-0.50%
D	Bonds	5.50%	6.00%	-0.50%
W	AWOTE	3.70%	4.20%	-0.50%
X	CPI	2.50%	2.70%	-0.20%

Arithmetic, before tax, fees and imputation credits

Investment Assumptions

Table 16.1

Sector		Risk margin (arithmetic average)	Mean rate (arithmetic average)	Compound average	Coefficient of variation	Standard deviation of rates	Skewness Kurtosis	
							'Moderate'	
							High'	
							'Extreme'	
S	Shares	4.4%	9.9%	8.7%	1.616	16.0%	-26%	75%
I	Int'l Shrs	3.0%	8.5%	7.6%	1.623	13.8%	-53%	96%
Q	Prop Trust	3.0%	8.5%	7.3%	1.624	13.8%	-247%	1000%
P	Direct Prop	1.8%	7.3%	7.1%	0.877	6.4%	-148%	304%
H	Hedged IS	3.1%	8.6%	7.7%	1.558	13.4%	-84%	146%
L	Loans/credit	1.6%	7.1%	7.0%	0.493	3.5%	66%	-12%
F	Fixed Int	0.7%	6.2%	6.1%	0.758	4.7%	-91%	388%
G	Semi-govt	0.7%	6.2%	6.1%	0.613	3.8%	39%	-50%
J	Int'l Fxd Int	0.5%	6.0%	5.9%	0.633	3.8%	-93%	367%
C	Cash	-0.2%	5.3%	5.3%	0.566	3.0%	52%	-77%
N	Infln Linked	1.5%	7.0%	6.9%	0.714	5.0%	-43%	52%
Balncd CapStb	Balanced	2.39%	7.89%	7.53%	1.124	8.87%	-82%	132%
	Cap Stable	1.07%	6.57%	6.48%	0.671	4.41%	-61%	205%
B	Bills	-0.20%	5.30%	5.26%	0.585	3.10%	66%	-44%
D	Bonds		5.50%	5.47%	0.472	2.60%	19%	-103%
W	AWOTE	-1.80%	3.70%	3.66%	0.758	2.80%	200%	447%
X	CPI	-3.00%	2.50%	2.48%	0.800	2.00%	86%	-24%

Before tax, fees and imputation credits

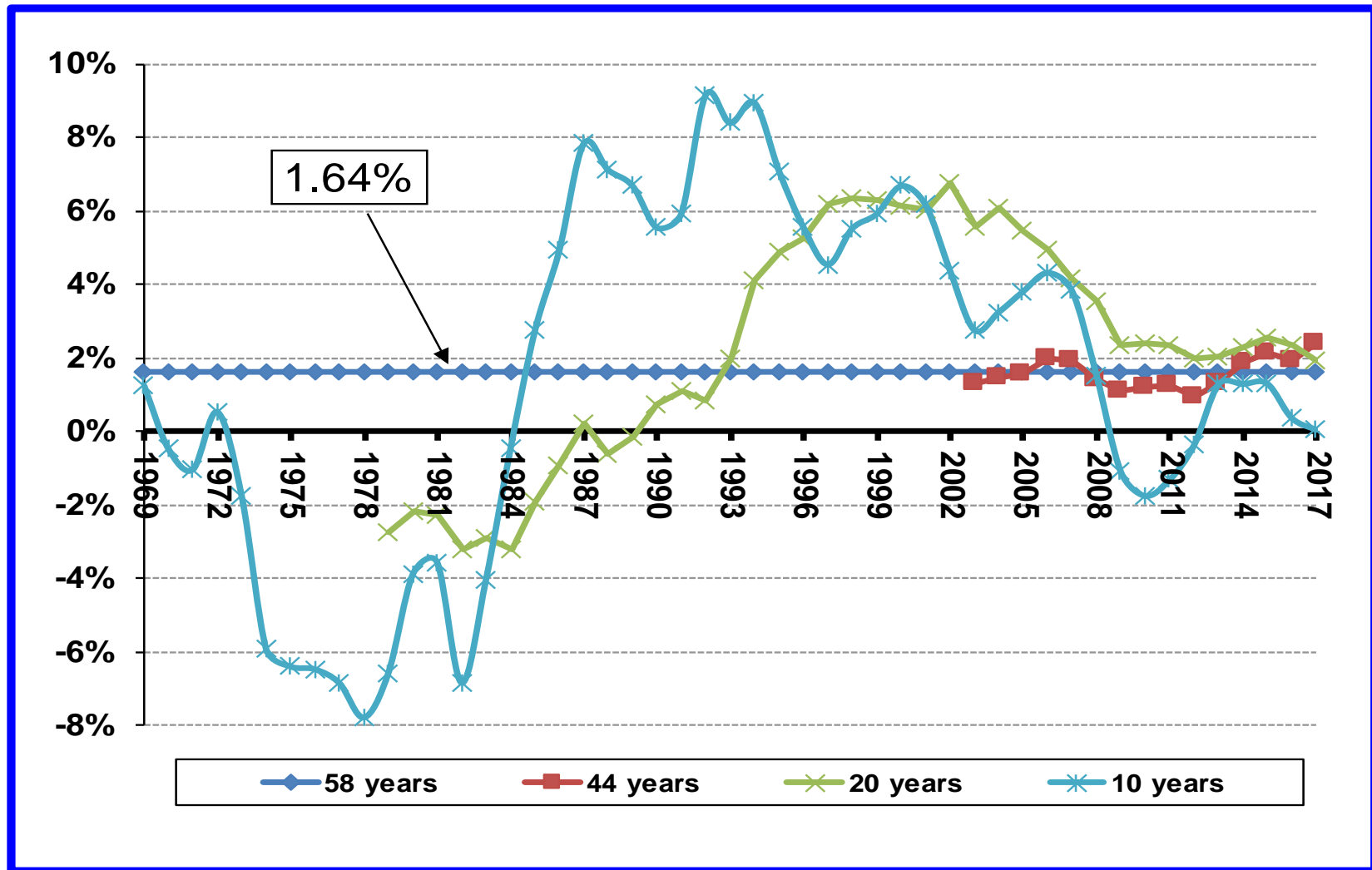
Assumptions gross/net tax/fees

Table 18.1

Sector		Mean rate (arithmetic average)			Accumulation	Pension
		Before tax Before fees	Before tax After fees	After tax & IC's After fees	Compound average rates after tax & IC's after fees	
S	Shares	9.90%	9.64%	9.45%	8.51%	9.62%
I	Int'l Shrs	8.50%	8.21%	7.55%	6.83%	7.67%
Q	Prop Trust	8.50%	8.21%	7.35%	6.38%	7.34%
P	Direct Prop	7.30%	6.60%	5.63%	5.47%	6.39%
H	Hedged IS	8.60%	8.31%	7.64%	6.93%	7.78%
L	Loans	7.10%	6.81%	5.79%	5.75%	6.75%
F	Fixed Int	6.20%	6.02%	5.12%	5.03%	5.91%
G	Semi-govt	6.20%	6.02%	5.12%	5.07%	5.95%
J	Int'l Fxd Int	6.00%	5.82%	4.95%	4.89%	5.75%
C	Cash	5.30%	5.15%	4.38%	4.35%	5.11%
N	Infln Linked	7.00%	6.81%	5.85%	5.76%	6.69%
Balncd	Balanced	7.89%	7.64%	7.12%	6.83%	7.79%
CapStb	Cap Stable	6.57%	6.36%	5.67%	5.60%	6.48%
B	Bills	5.30%	5.30%	4.51%	4.47%	5.26%
D	Bonds	5.50%	5.50%	4.68%	4.65%	5.47%

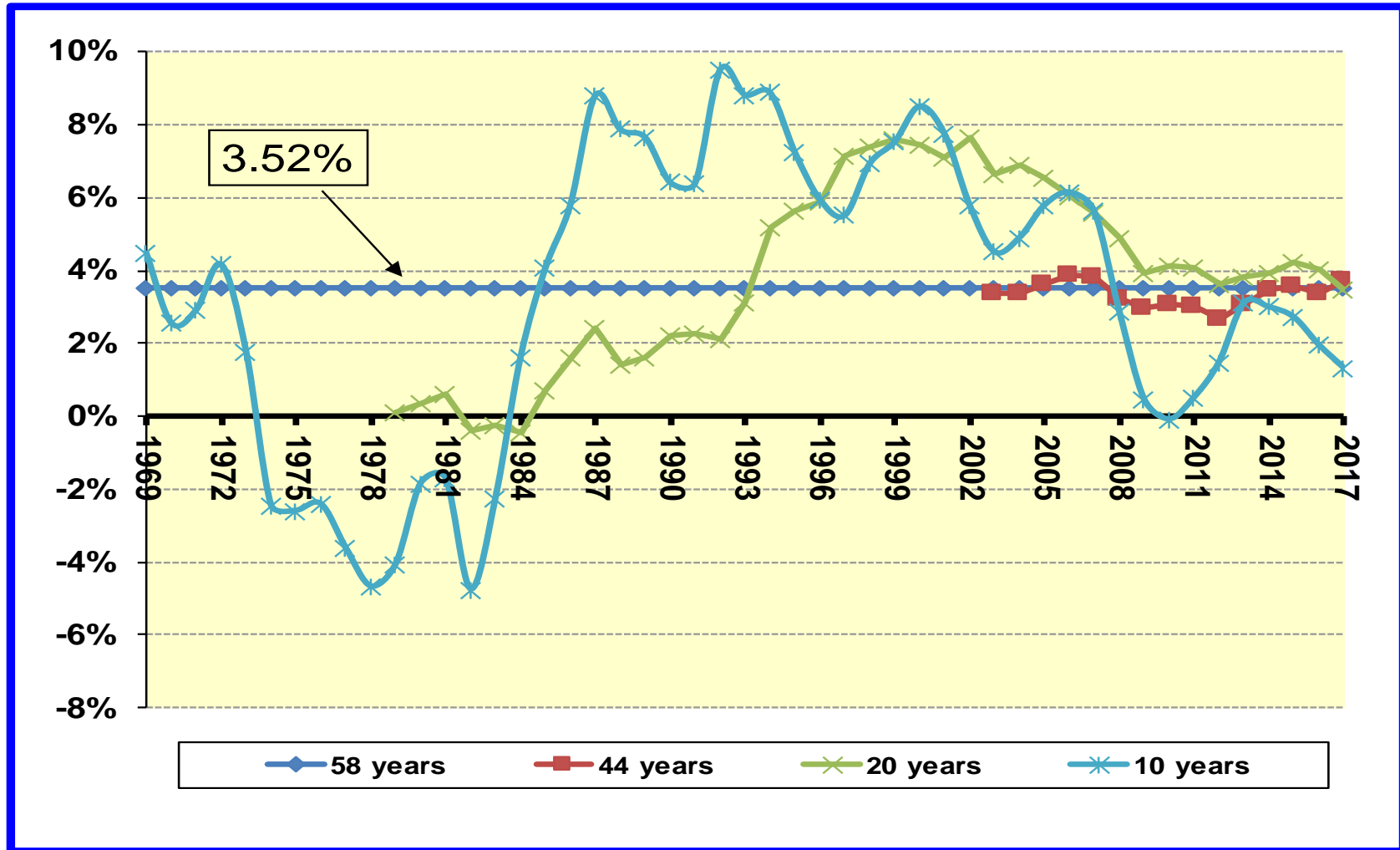
Rolling Average Real 'Balanced' Returns over AWOTE

Figure 19.1



Rolling Average Real 'Balanced' Returns over CPI

Figure 19.1



Appendices

A Modelling Skewness and Kurtosis

Normal power approximation, and
a gamma exponential variable

B Modelling Auto-correlations

Shares (S sector) – one extreme
Bonds (D sector) – other extreme

C *Austmod* Investment Simulation Model

The 26 inputs are described
“Historical random start” modelling defined
Summary of algorithms and output

Concluding Remarks Section 20

- It is desirable for the setting of long-term assumptions to analyse results over at least one full economic cycle
- **The 'sum of two sine curves' technique is a powerful tool for analysing economic cycles but a single sine curve is sometimes preferable**
- Care is needed when using running averages because their trends are impacted by the old data dropping off
- **The impact of the GFC was not an isolated event**
- Skewness and kurtosis assumptions for many sectors indicate that their return distributions are not normal or lognormal
- **There is a slight negative bias in Balanced portfolio (and share) auto-correlations up to a lag of about 5.5 years**
- Average 28-year S and 33-year D auto-correlations indicate some stability after rescaling the x-axis

Acknowledgments

- Alan Brown
- Cary Helenius and Clive Amery
- Janice Jones
- Ray Stevens, Darren Grenfell and Hazel Lamden
- Ord Minnett
- Designers of National Mutual EFG investment system
- Ken Tan
- *“Black Swans, Fat Tails and Spherical Cows”*
by Jeremy Waite

NEXT ?

2017	Quarterly Data Updates
2018	Over 60 years
2021	Paper (s)

QUESTIONS ?

- Methodology
- Assumptions
- Rank correlations
- Auto correlations
- Skewness & kurtosis
- Real returns
- Next ?

Thank you very much for your attention!

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