

**Biennial Convention 2009**

**Go for Gold**

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Institute of Actuaries of Australia



# **The Funding of Closed Defined Benefit Schemes**

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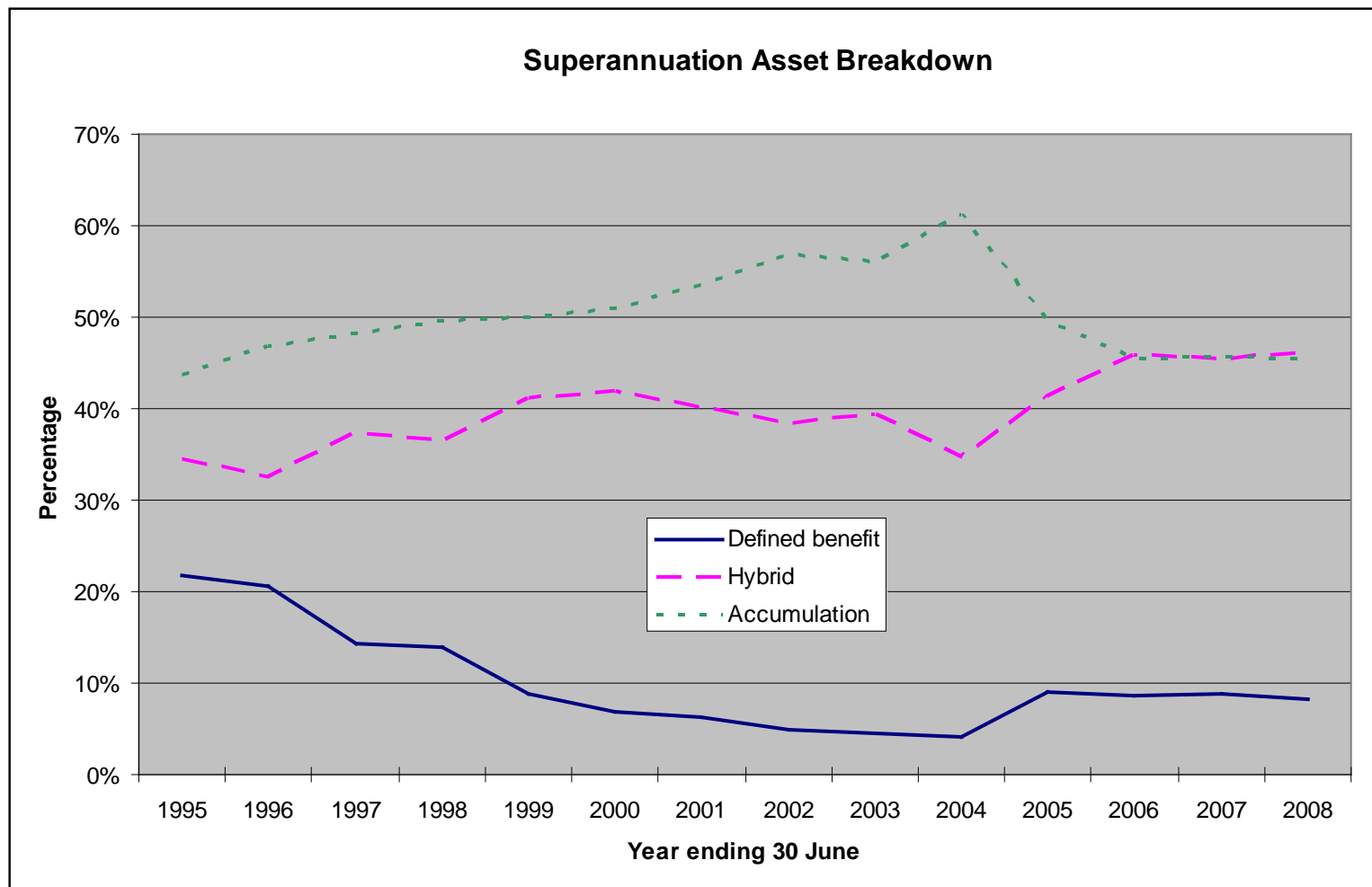


## Overview

- Motivation
- Methodology
- Results
- Conclusions and future research



## Motivation





## How does a closed scheme differ from an open scheme?

- Future liabilities decreasing relative to past liabilities
- Liabilities decreasing in duration
- Benefit outflow greater than contribution inflow



## What are the key decisions for a closed scheme?

- Investment strategy
- Contribution strategy
- Winding up the scheme





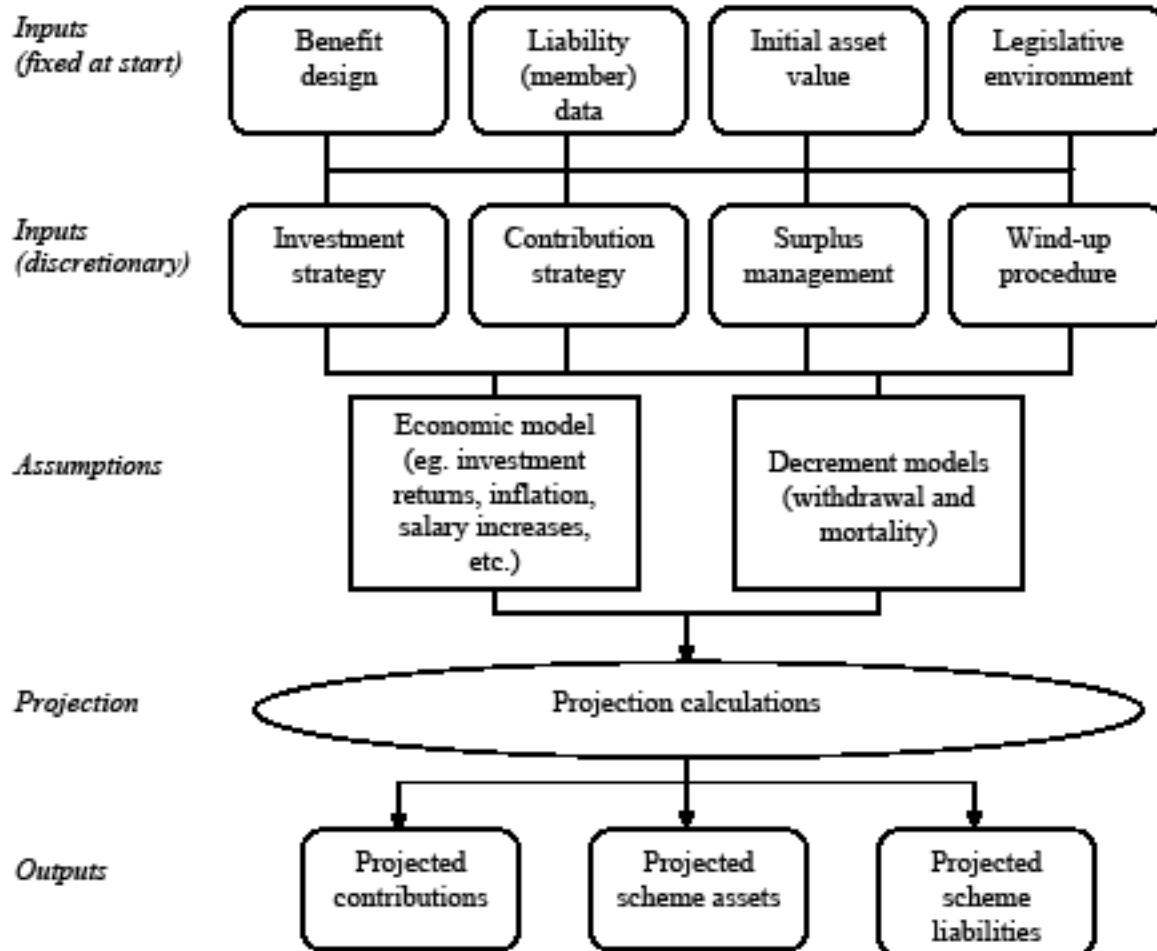
## What am I trying to achieve?

- Investigate the effect of different decisions on the future development of closed scheme contributions and funding levels
- Check if uncontrollable factors such as benefit design have an impact on the results



## Methodology

- Stochastic model and simulations – both financial and demographic factors stochastic
- Model scheme projected forward on an annual basis until wind up
- Annual actuarial valuations with contributions backdated to the valuation date
- Membership projected individually – i.e. Bernoulli process applied to each individual in each year of projection







## The model scheme (base scenario)

- Pays pension benefits to those who have membership greater than 5 years
- 9,000 members – made up of 5,000 active members, 2,080 deferred members and 1,920 pensioner members
- Uses the PUC method to calculate liabilities and contributions – surpluses and deficits spread over 3 years
- Actuarial assumptions equal to the expectations from the stochastic models – discount rate equal to expected return on assets



## The model scheme (base scenario)

- 100% funded at the commencement of projections
- Investment strategy (rebalanced each year):

<b>Asset Class</b>	<b>Percentage</b>
Australian Shares	35%
International Shares	25%
Australian Bonds	20%
International Bonds	15%
Cash	5%



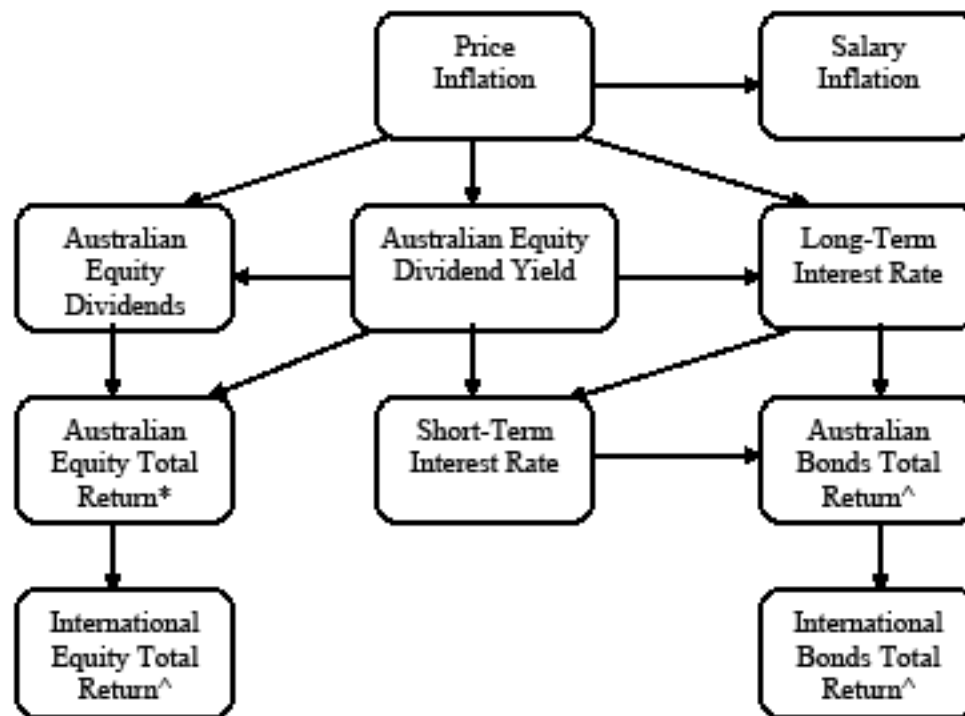
## The model scheme (base scenario)

- Keeps surplus in the scheme at all times until wind up
- Wind up occurs when active membership drops below 50 - liabilities discharged by purchasing annuities valued at a discount rate 0.5% below the long-term interest rate
- Wind up liability increased by 2% to allow for the costs of wind up
- Any deficiency of assets to wind up liability made up by additional employer contributions



## The economic model

- Based on Wilkie (1995) – a “cascade” structure
- Parameterised using annual data from 30 June 1982 – 30 June 2008, period selected due to relatively similar economic conditions at the start and end dates



\* Not calculated directly by the Wilkie model, but can be obtained indirectly via Australian equity dividends and dividend yield.

^ Not part of the Wilkie structure but included in addition to the original structure.





## The economic model - summary

Factor	Average Return (p.a.)	Standard Deviation of Return (p.a.)	Annual Autocorrelation
Price inflation	4.7%	2.8%	58%
Salary inflation	5.7%	3.2%	51%
Long-term interest rate	9.0%	2.7%	77%
Australian Equities	13.6%	23.7%	1%
International Equities	11.5%	29.2%	2%
Australian Bonds	8.6%	7.6%	18%
International Bonds	10.0%	6.4%	15%
Cash	8.8%	3.0%	82%
Scheme return <i>(non-pension assets post-tax)</i>	10.9%	13.1%	2%



## The decrement model - withdrawal

- Withdrawal rates currently decrease with age and length of service
- Not currently linked to financial model – ABS job ceasing statistics suggest overall withdrawal relatively steady over economic cycle because of negatively correlated voluntary and involuntary job leaving
- A full analysis of ABS micro-data to be done in future to identify withdrawal rate links to economy, age, service, salary, etc.



## The decrement model - disability

- No separate disability benefit so disability rates not required – members who become disabled are assumed become deferred members



## The decrement model - mortality

- Based on ALT00-02 – lower rates suggested by Knox and Nelson (2007) not used as pension cannot be commuted and disabled members still receive a pension
- Mortality improvement not allowed for computational reasons – uncertain future mortality allowed for through random shocks to ALT00-02 rates and underlying binomial variability



## The decrement model - mortality

- Not linked to economy – literature is inconclusive
- Not currently linked to salary or pension size – literature suggests mortality rate is negatively correlated with income
- Future work to be done to quantify this effect and include in modelling





## Initial Analysis

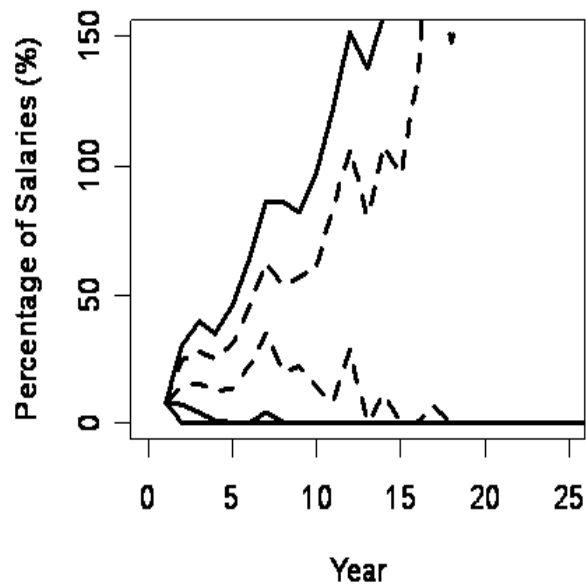
- **Median and 95% Confidence Intervals – contribution rate and funding level**, these are calculated based on the appropriate percentiles of the 1,000 simulations for each projection year
- Contribution rate as a percentage of salaries – additional 90% and 70% percentiles provided
- Funding level is assets divided by liabilities – separate calculations for funding liability and wind-up liability
- **Present value of employer contributions** – frequency plot of results for 1,000 simulations, contributions are discounted at the cash rate appropriate for that simulation



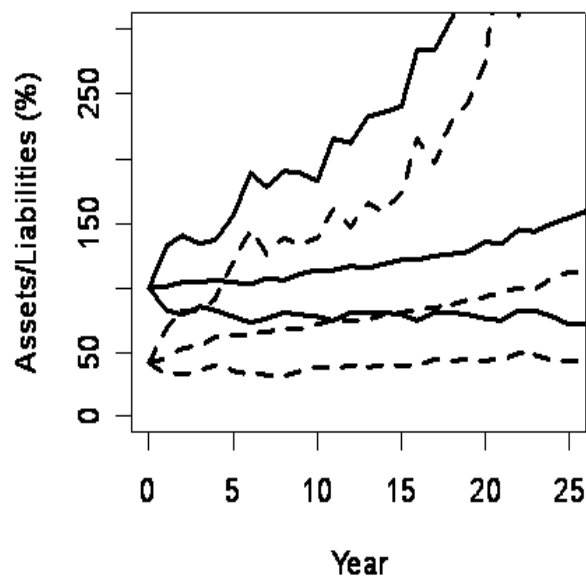
## Results – base scenario

Contributions      — Base      - - Base 90% and 70% lines  
Funding              — Base - Actuarial      - - Base - Wind-up

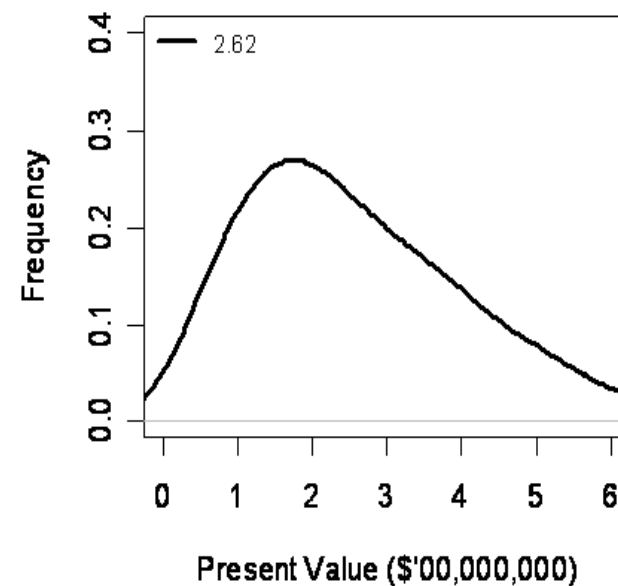
CI - Contribution Rate



CI - Funding Level



Present Value of Conts



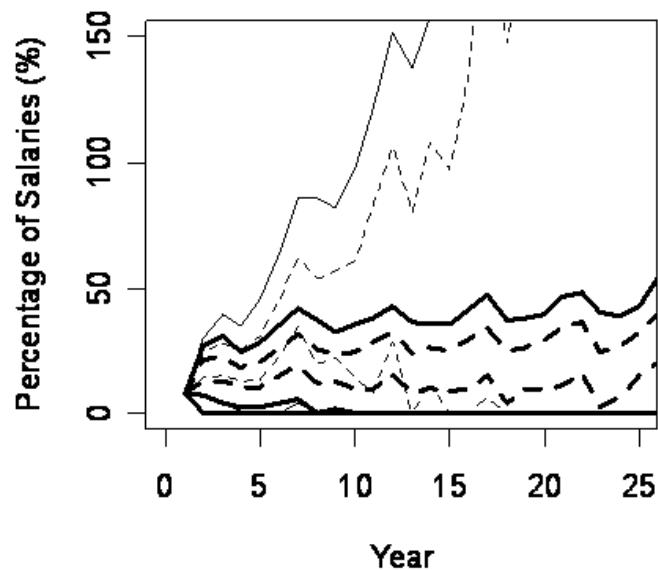
Note – the figure in the plot is the average



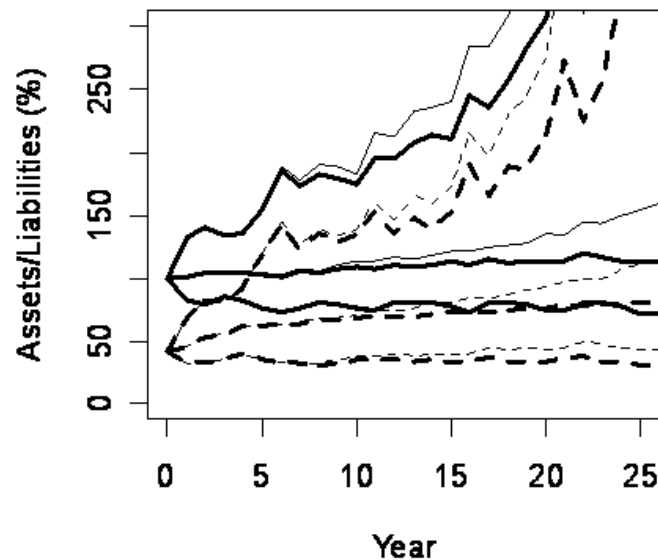
## Results – new entrants allowed (BD2)

- |               |                    |                             |
|---------------|--------------------|-----------------------------|
| Contributions | — BD2              | -- BD2 90% and 70% lines    |
|               | — Base             | ---- Base 90% and 70% lines |
| Funding       | — BD2 - Actuarial  | -- BD2 - Wind-up            |
|               | — Base - Actuarial | ---- Base - Wind-up         |

CI - Contribution Rate



CI - Funding Level





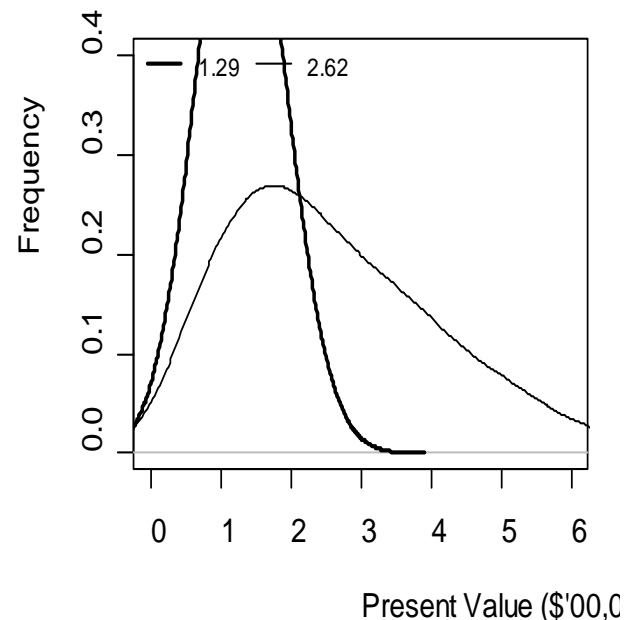
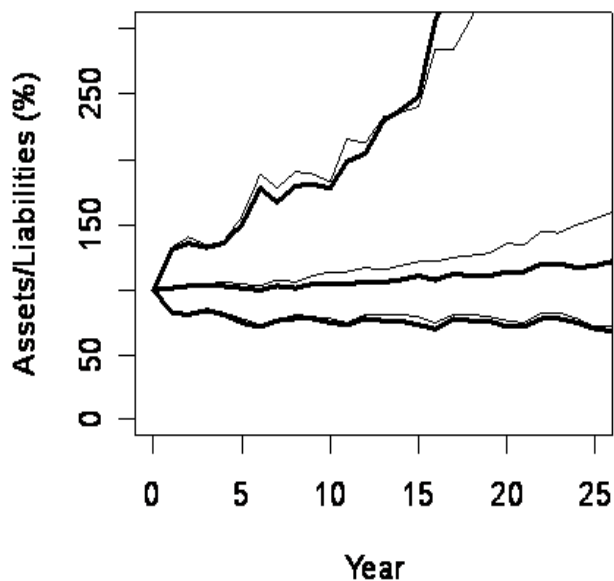
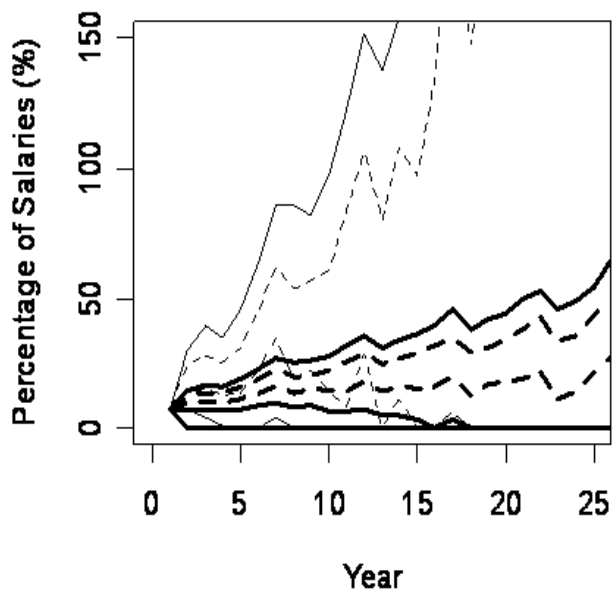
## Results – lump sum only (BD3)

- |               |                    |                              |
|---------------|--------------------|------------------------------|
| Contributions | — BD3              | - - - BD3 90% and 70% lines  |
|               | — Base             | - - - Base 90% and 70% lines |
| Funding       | — BD3 - Actuarial  |                              |
|               | — Base - Actuarial |                              |

CI - Contribution Rate

CI - Funding Level

Present Value of



Note – the figure in the plot is the average



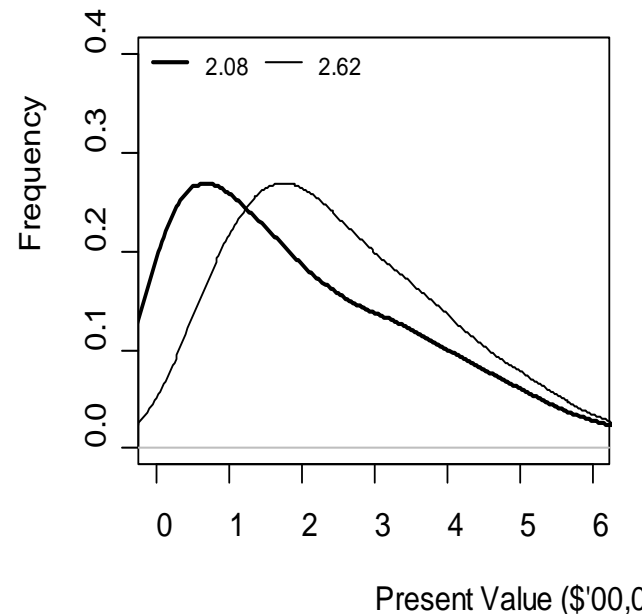
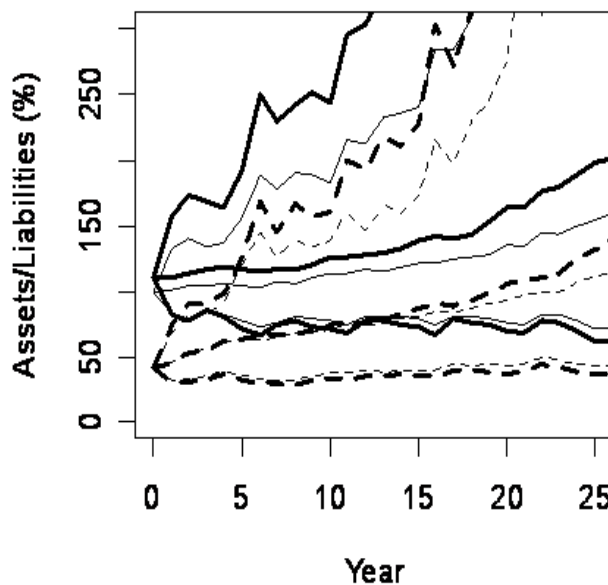
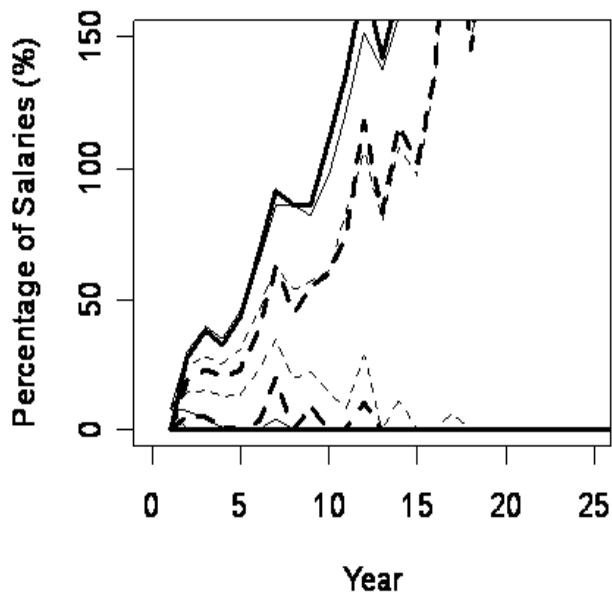
## Results – more aggressive investment (IS1)

- |               |                    |                              |
|---------------|--------------------|------------------------------|
| Contributions | — IS               | - - IS 90% and 70% lines     |
|               | — Base             | - - - Base 90% and 70% lines |
| Funding       | — IS - Actuarial   | - - IS - Wind-up             |
|               | — Base - Actuarial | - - - Base - Wind-up         |

CI - Contribution Rate (IS1)

CI - Funding Level (IS1)

Present Value of



Note – the figure in the plot is the average





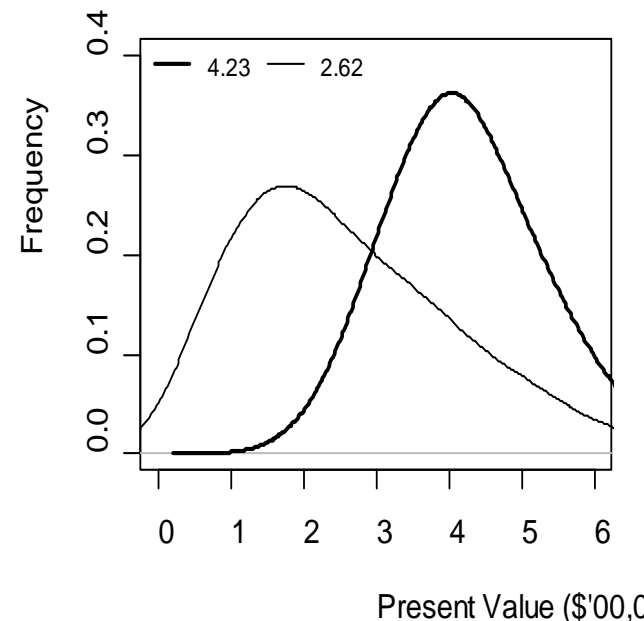
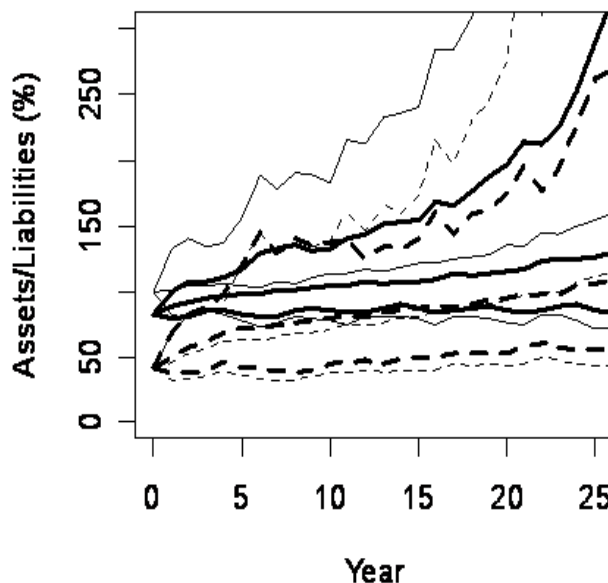
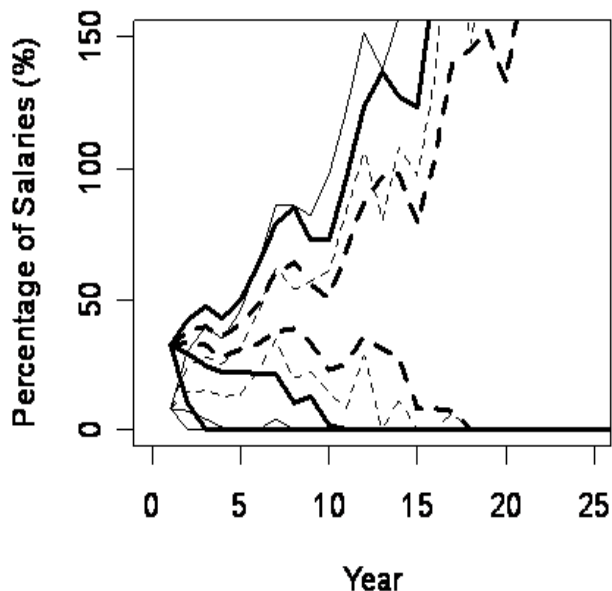
## Results – more defensive investment (IS2)

- |               |                    |                             |
|---------------|--------------------|-----------------------------|
| Contributions | — IS               | --- IS 90% and 70% lines    |
|               | — Base             | ---- Base 90% and 70% lines |
| Funding       | — IS - Actuarial   | --- IS - Wind-up            |
|               | — Base - Actuarial | ---- Base - Wind-up         |

CI - Contribution Rate (IS2)

CI - Funding Level (IS2)

Present Value of



Note – the figure in the plot is the average



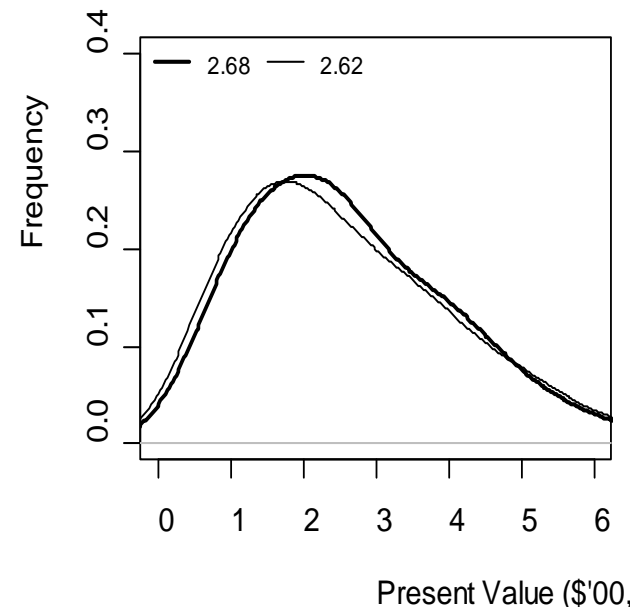
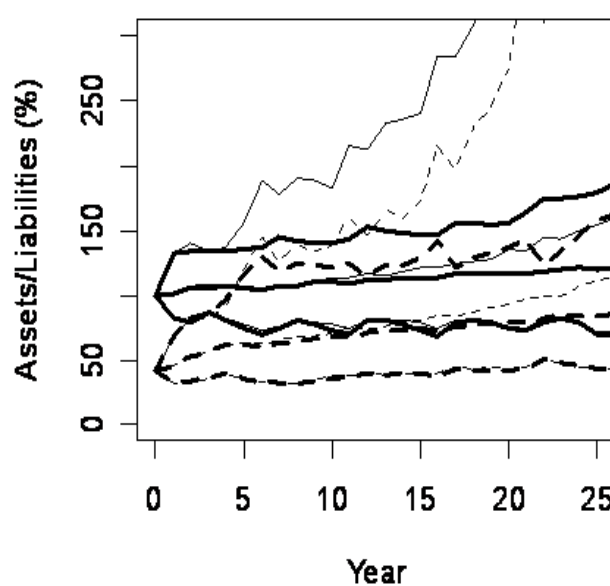
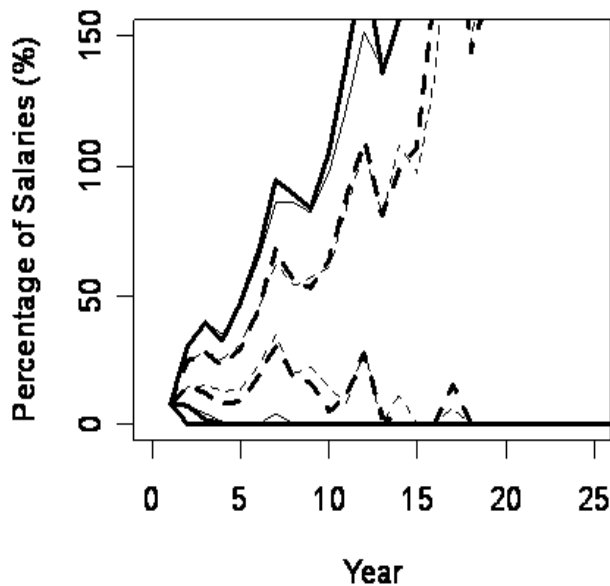
## Results – reduce investment risk as surplus increases (IS3)

- |               |                    |                              |
|---------------|--------------------|------------------------------|
| Contributions | — IS               | - - IS 90% and 70% lines     |
|               | — Base             | - - - Base 90% and 70% lines |
| Funding       | — IS - Actuarial   | - - IS - Wind-up             |
|               | — Base - Actuarial | - - - Base - Wind-up         |

CI - Contribution Rate (IS3)

CI - Funding Level (IS3)

Present Value c



Note – the figure in the plot is the average



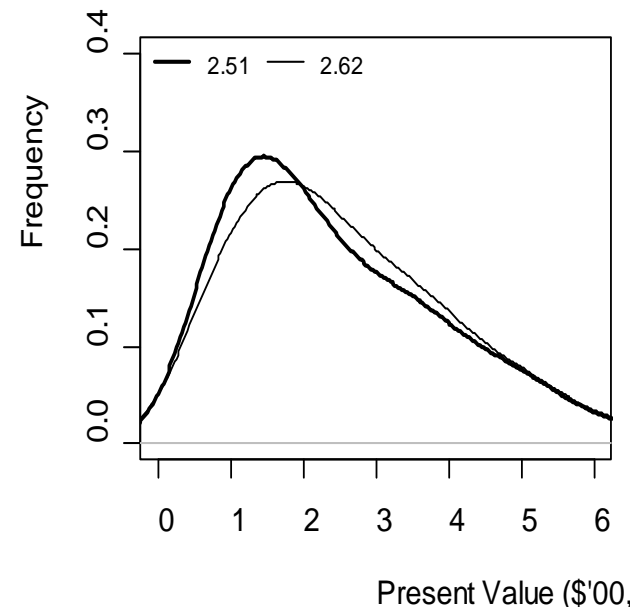
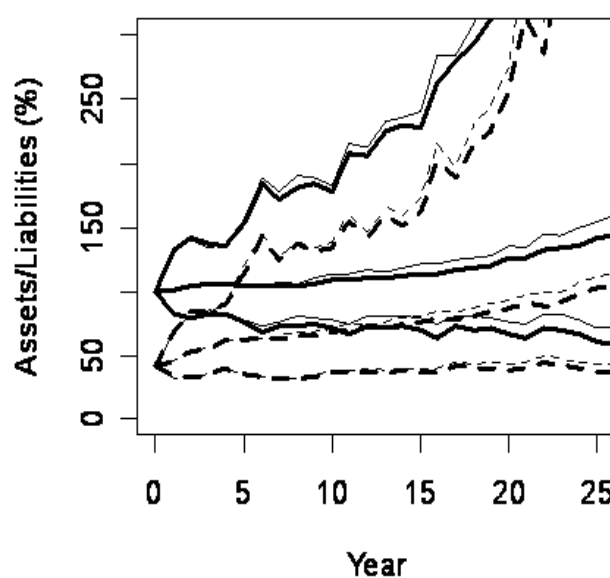
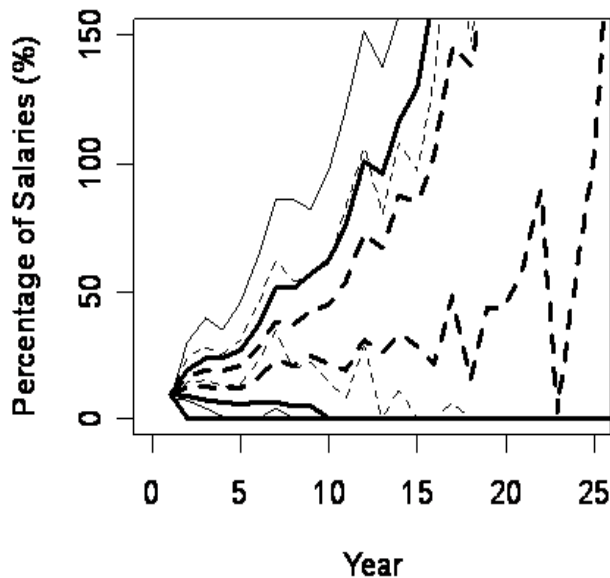
## Results – aggregate funding (CS3)

- |               |                    |                              |
|---------------|--------------------|------------------------------|
| Contributions | — CS               | - - CS 90% and 70% lines     |
|               | — Base             | - - - Base 90% and 70% lines |
| Funding       | — CS - Actuarial   | - - CS - Wind-up             |
|               | — Base - Actuarial | - - - Base - Wind-up         |

CI - Contribution Rate (CS3)

CI - Funding Level (CS3)

Present Value c



Note – the figure in the plot is the average



## Funding Level regressions

$$FLR = \beta_0 + \beta_1 i_{diff} + \beta_2 w_{diff} + \beta_3 q_{diff} + \beta_4 m_{diff} + \beta_5 r_{diff} \\ + \beta_6 i_{chnng} + \beta_7 FL_{diff} + \beta_8 I \times FL_{diff}^2 + \varepsilon$$

- $FLR$  - % change in funding level over the year
- $i_{diff}$  – actual investment return less discount rate
- $w_{diff}$  – actual less expected salary increases
- $q_{diff}$  – actual less expected pension increases
- $m_{diff}$  – actual less expected mortality rate
- $r_{diff}$  – actual less expected withdrawal rate (lump sums)
- $i_{chnng}$  – % change in liability discount rate
- $FL_{diff}$  – funding level last year less 1
- $I$  – equal to one if  $FL_{diff} > 0$  or zero otherwise
- $FL_{diff}^2$  – (funding level last year less 1)<sup>2</sup>





## Regression Results – base scenario

- Done in year 2 and year 21 to test differences

	Actuarial						Wind-up					
	t = 2			t = 21			t = 2			t = 21		
	Coef	S.E.	SS	Coef	S.E.	SS	Coef	S.E.	SS	Coef	S.E.	SS
$B_0$	0.007	0.000	NA	0.038	0.001	NA	-0.108	0.009	NA	<i>0.002</i>	0.002	NA
$i_{diff}$	0.914	0.002	0.922	0.970	0.007	0.926	1.036	0.011	0.357	0.930	0.015	0.428
$w_{diff}$	-0.305	0.016	0.002	<i>0.009</i>	0.042	0.000	<i>-0.136</i>	0.079	0.000	<i>0.068</i>	0.095	0.000
$q_{diff}$	-0.671	0.016	0.028	-0.870	0.045	0.034	-0.224	0.088	0.001	<i>-0.135</i>	0.113	0.000
$m_{diff}$	1.009	0.263	0.000	<i>0.635</i>	0.329	0.000	<i>1.694</i>	1.323	0.000	<i>0.478</i>	0.728	0.000
$r_{diff}$	<i>0.115</i>	0.147	0.000	NA	NA	NA	<i>0.419</i>	0.743	0.000	NA	NA	NA
$i_{chg}$	NA	NA	NA	NA	NA	NA	1.030	0.010	0.602	0.603	0.009	0.478
$FL_{diff}$	-0.375	0.004	0.031	<i>0.003</i>	0.002	0.000	-0.127	0.018	0.004	0.035	0.004	0.007
$FL^2_{diff}$	0.927	0.016	0.014	0.002	0.001	0.004	NA	NA	NA	-0.004	0.002	0.000
	Total 0.996			Total 0.964			Total 0.964			Total 0.914		

Coefficients in bold italics are insignificant at the 5% level.





## Regression Results – lump sum only

- Wind-up liability not relevant for lump sums so not included

	Lump Sum - BD3						Base					
	t = 2			t = 21			t = 2			t = 21		
	Coef	S.E.	SS	Coef	S.E.	SS	Coef	S.E.	SS	Coef	S.E.	SS
$B_0$	0.004	0.000	NA	0.020	0.004	NA	0.007	0.000	NA	0.038	0.001	NA
$i_{diff}$	0.940	0.001	0.898	1.030	0.012	0.838	0.914	0.002	0.922	0.970	0.007	0.926
$w_{diff}$	-0.993	0.008	0.046	-1.012	0.072	0.031	-0.305	0.016	0.002	<b>0.009</b>	0.042	0.000
$q_{diff}$	<b>0.015</b>	0.009	0.000	0.176	0.077	0.000	-0.671	0.016	0.028	-0.870	0.045	0.034
$m_{diff}$	-1.278	0.220	0.000	-0.235	0.319	0.000	1.009	0.263	0.000	<b>0.635</b>	0.329	0.000
$r_{diff}$	<b>0.015</b>	0.028	0.000	0.274	0.064	0.001	<b>0.115</b>	0.147	0.000	NA	NA	NA
$i_{chng}$	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA	NA
$FL_{diff}$	-0.418	0.002	0.047	0.047	0.002	0.042	-0.375	0.004	0.031	<b>0.003</b>	0.002	0.000
$FL^2_{diff}$	0.711	0.009	0.008	-0.003	0.000	0.008	0.927	0.016	0.014	0.002	0.001	0.004
	Total		0.999	Total		0.921	Total		0.996	Total		0.964



## Conclusions

- Surplus a significant problem for closed schemes – more of a problem for pensions
- Reducing investment risk reduces surplus but increases future contributions
- Reducing the speed at which deficits are removed may lead to a slight overall reduction in contributions
- Investment returns by far the most important factor in predicting funding level changes



## Future research

- Effect of alternative investment models
- Cash flow matching
- Changes to timing of wind-up
- Use of scheme surplus
- Effect of government insurance