

Biennial Convention 2009

Go for Gold

19–22 April 2009 • Sydney



Institute of Actuaries of Australia



UniSuper's Approach to Risk Budgeting

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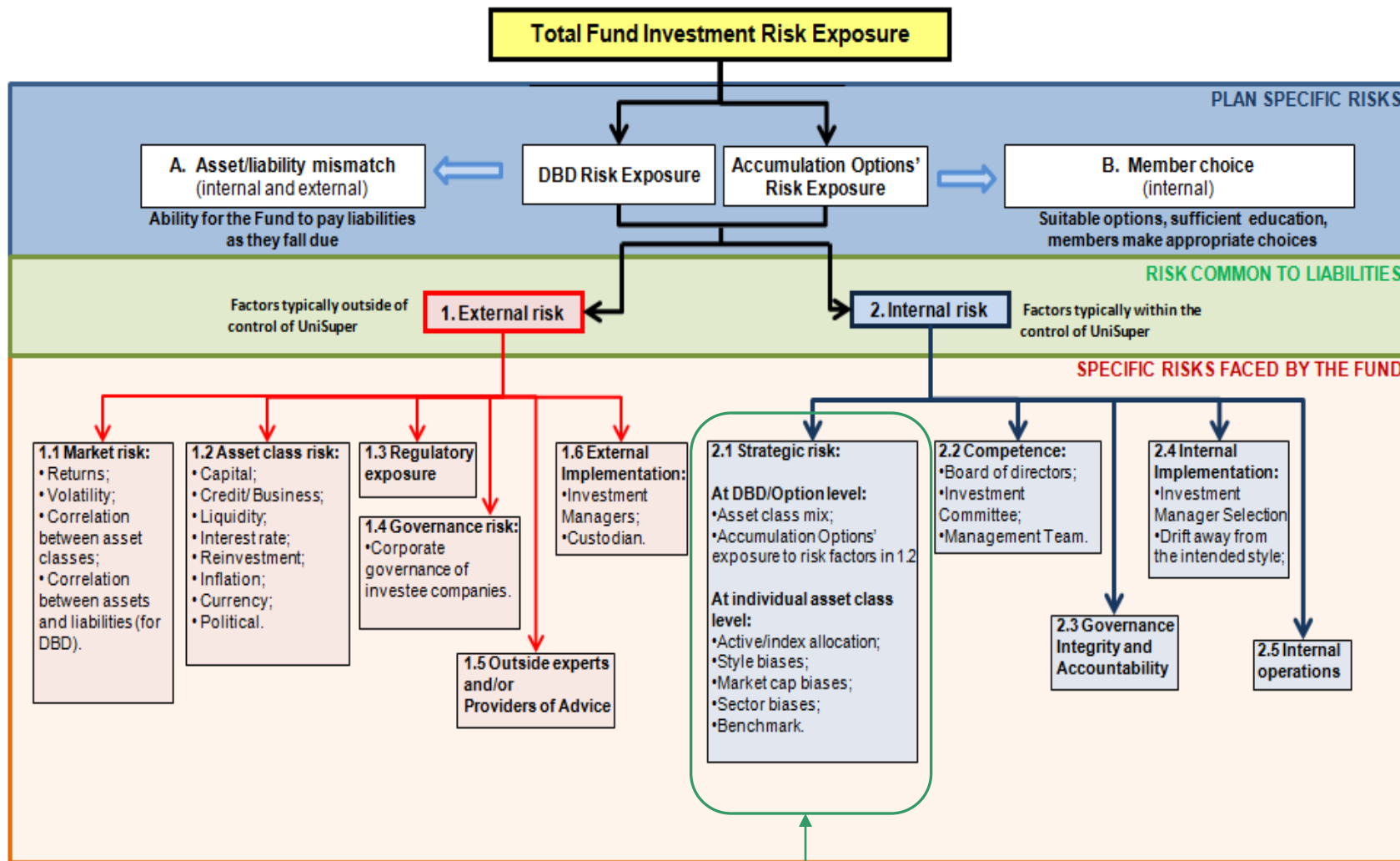
Agenda

- Objective, goals and processes
- Link between SAA and risk budgeting
- Equations
- Framework for discussion
- Questions



Definitions

- Risk budgeting:
 - Set target risk levels by Option
 - Allocating this risk across investments/managers
 - To maximise returns
 - While containing risk within the agreed targets
 - Traditionally via tracking error target
- Ensures that the “risk budget” is efficiently distributed by:
 - Assets
 - Styles
 - Managers



TURBOs



Desired Features

- Key risk: not meeting liabilities as they fall due
- Hence risk budget should be tied to the liabilities
- Must focus on risk allocation not attribution
- Must handle:
 - Alternatives
 - Tilting
 - Operational concerns (rebalancing, tolerance limits etc)
- Must give us insight as to how to change the portfolio

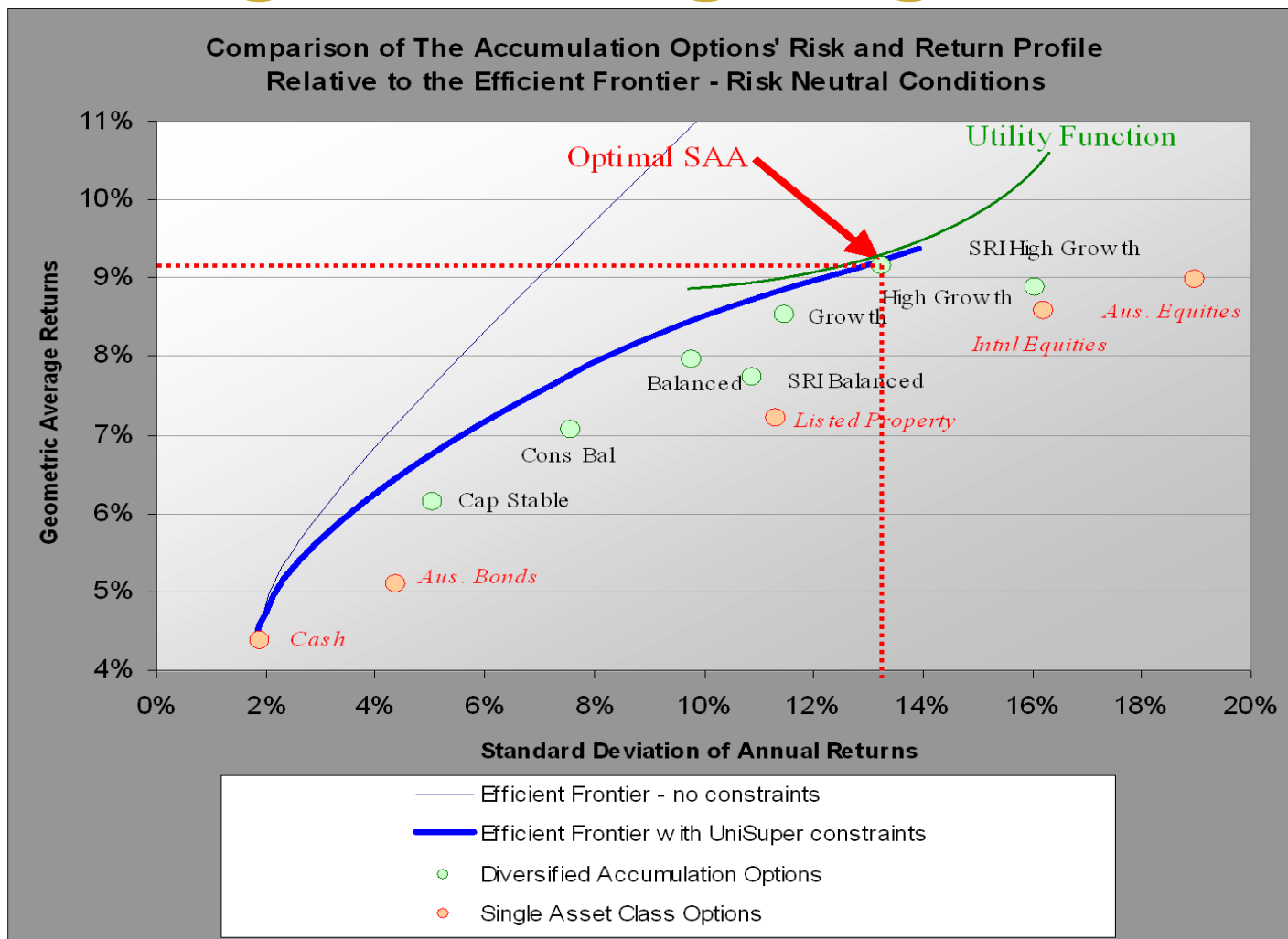


6 Processes Followed by TURBOs

1. Split returns between beta and *ex-post* alpha
2. Compare each Option's beta exposure to the SAA
3. Find historic variance per Option
4. Determine *ex-ante* alpha estimates
5. Set a minimum hurdle for each Option's active risk
6. Find the 'optimal' manager line-up

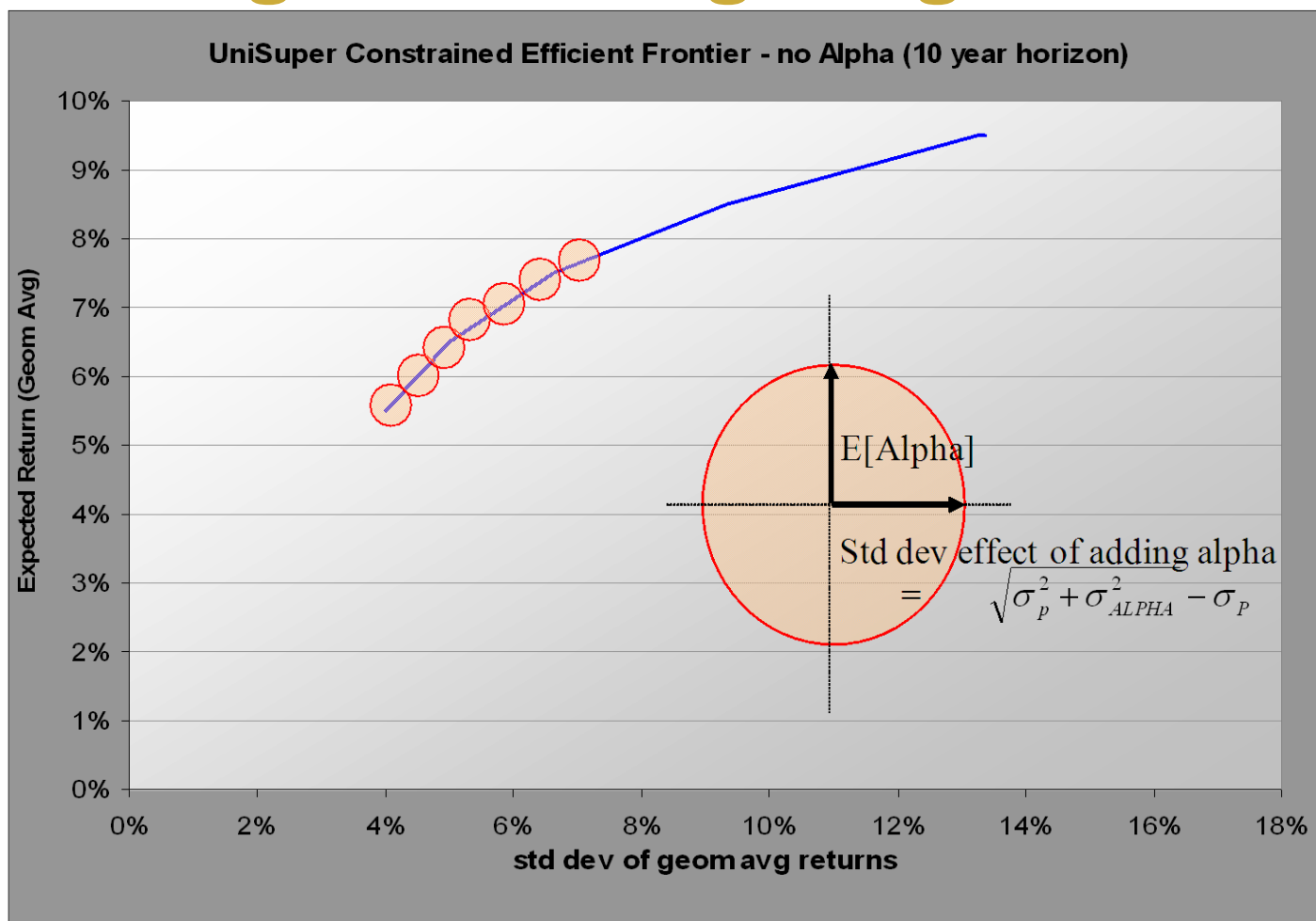


Linking Risk Budgeting to SAA



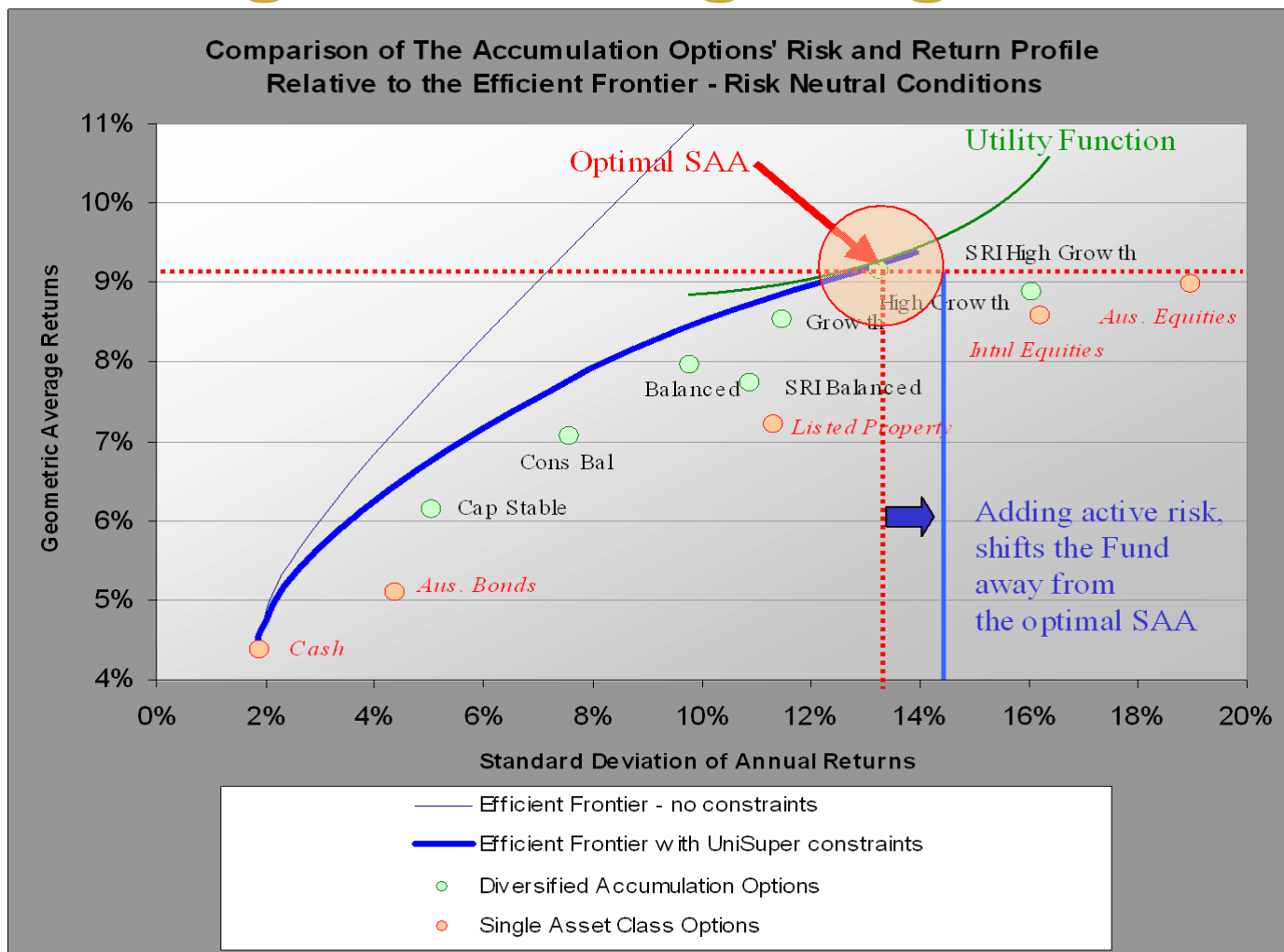


Linking Risk Budgeting to SAA



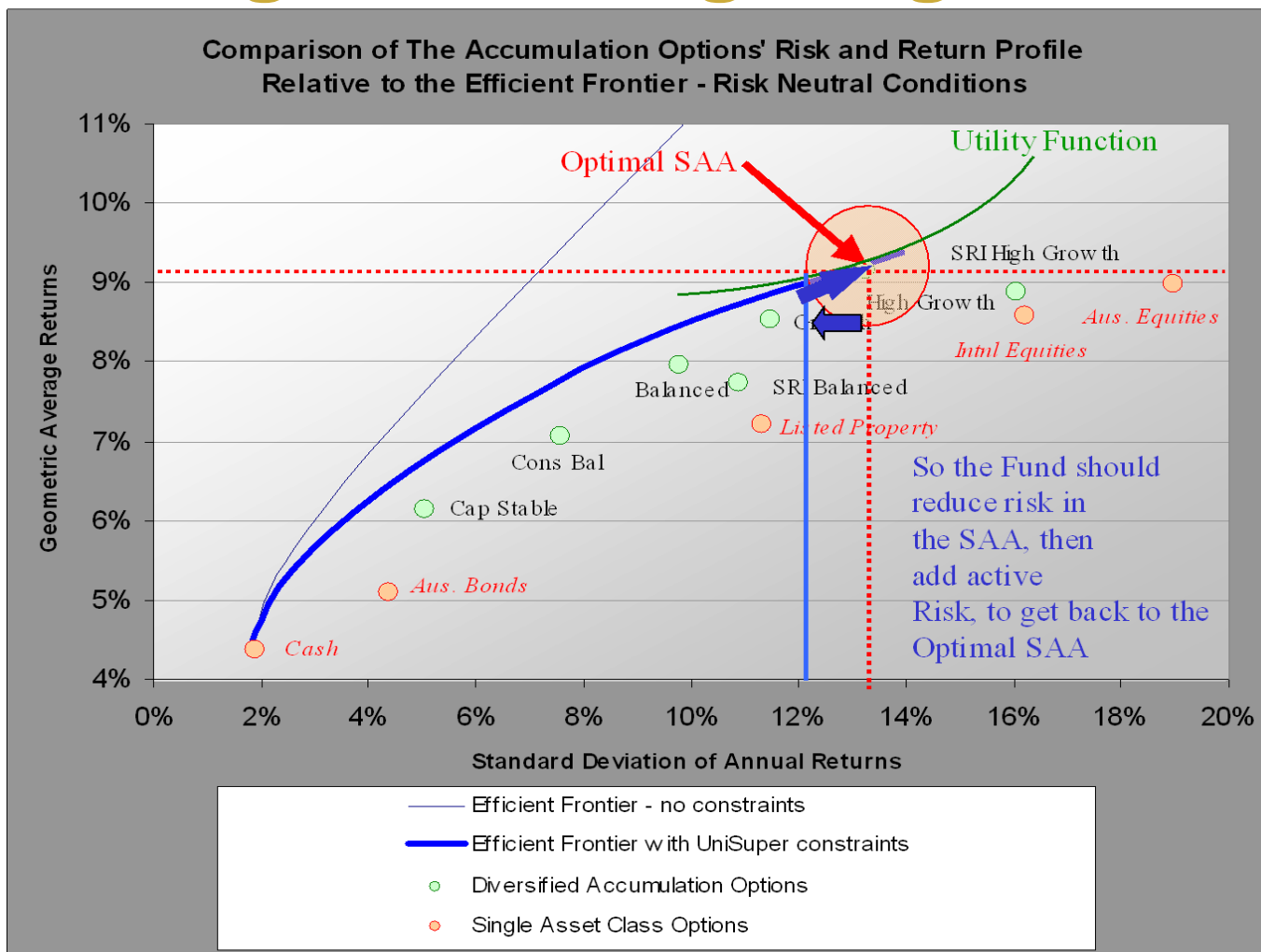


Linking Risk Budgeting to SAA



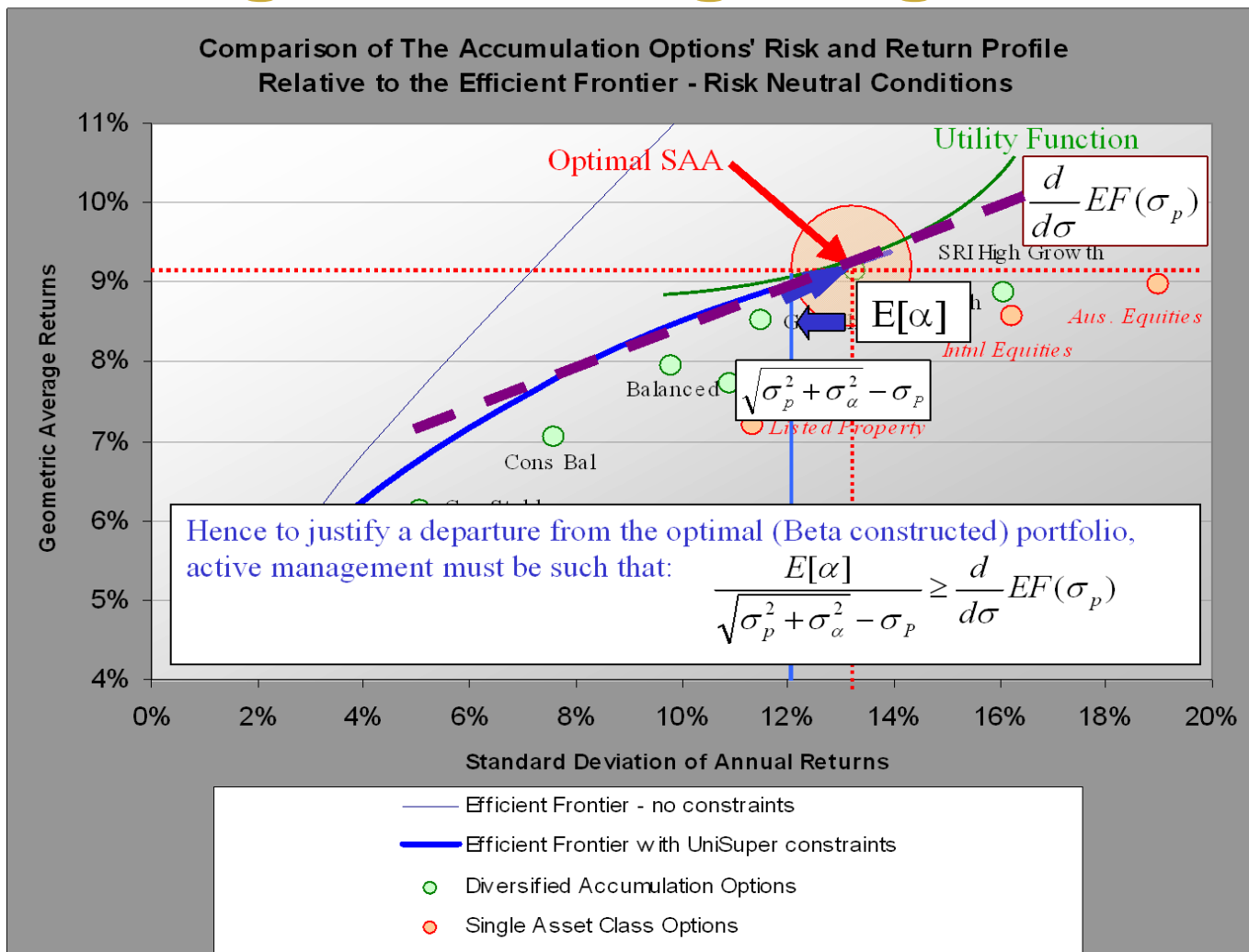


Linking Risk Budgeting to SAA



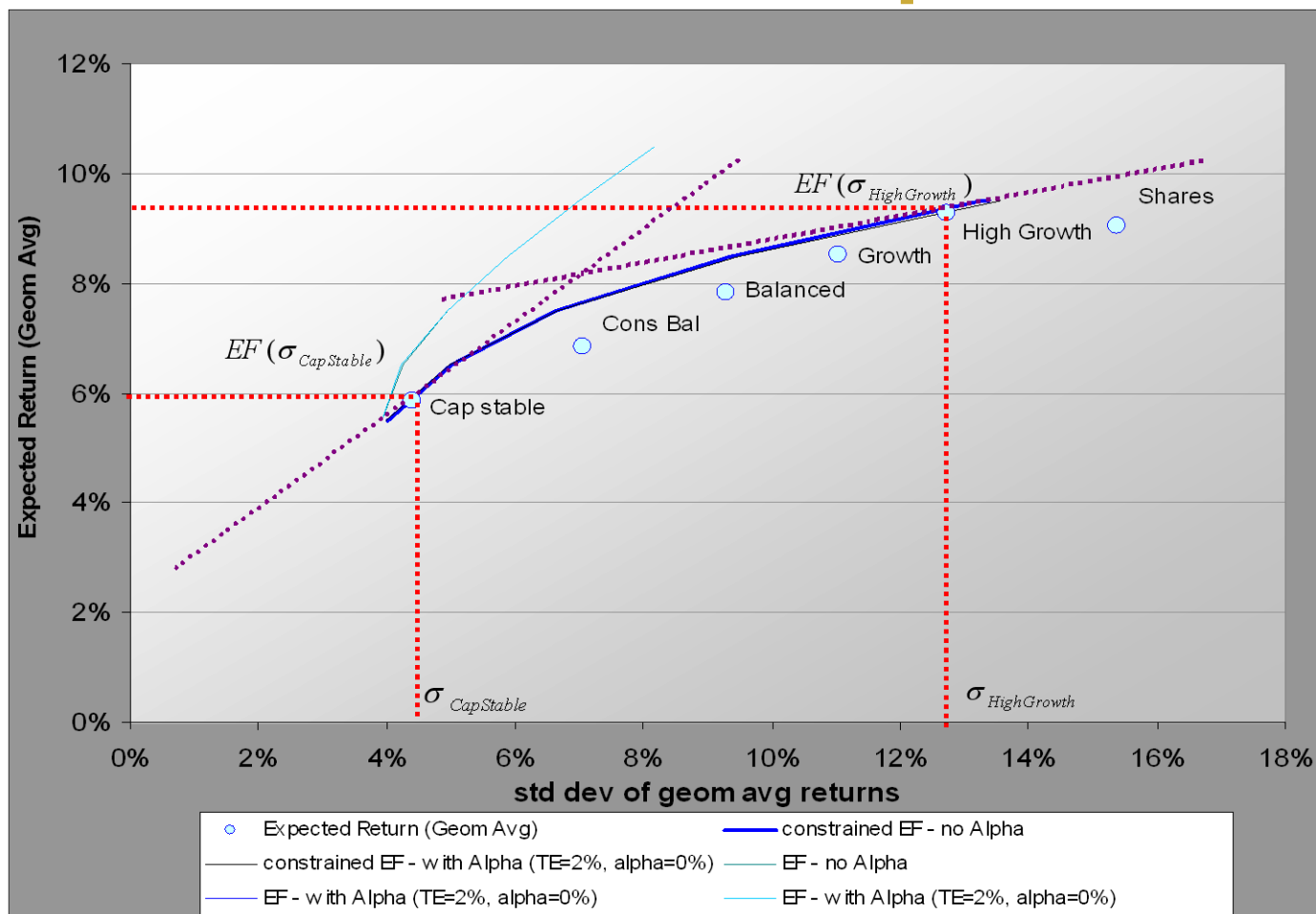


Linking Risk Budgeting to SAA



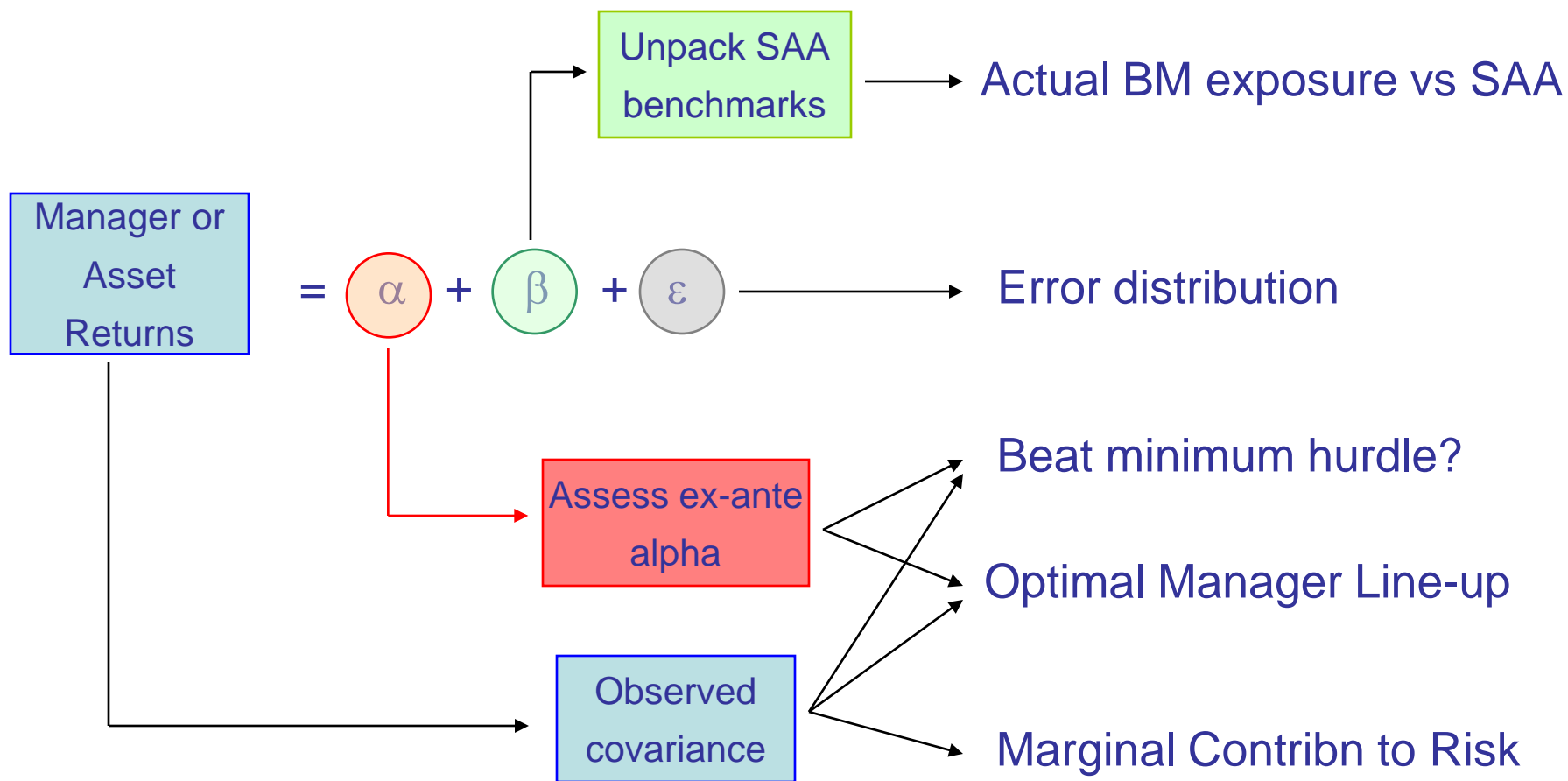


Practical Example



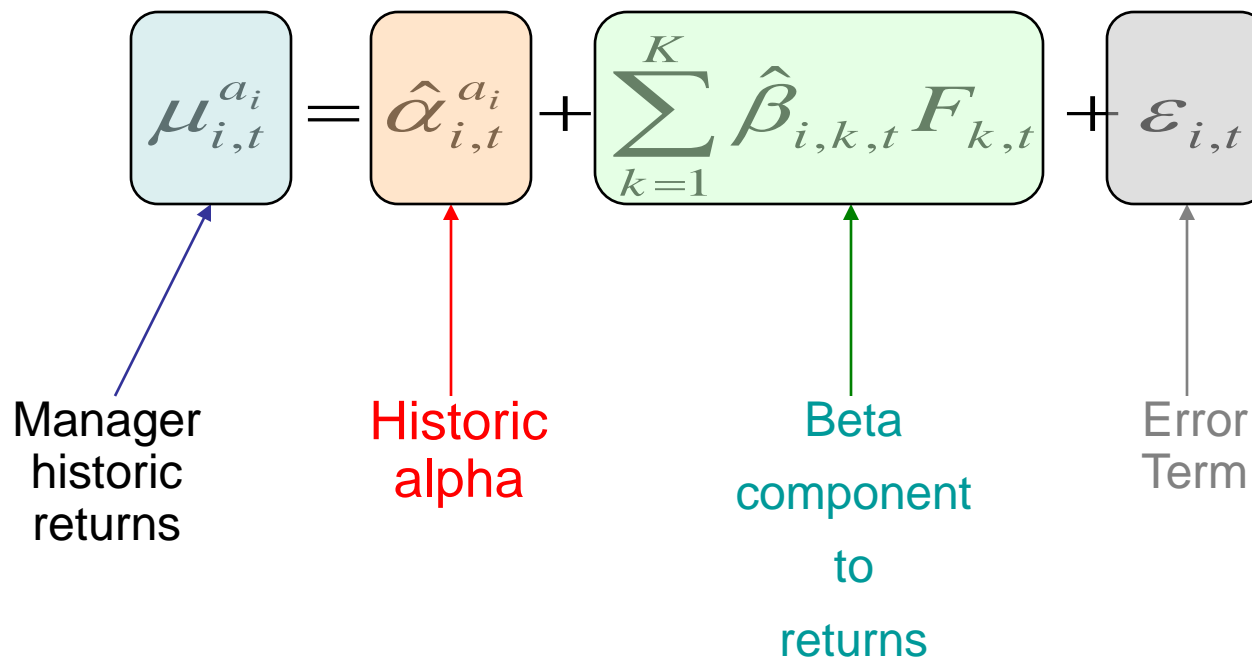


Graphical Representation





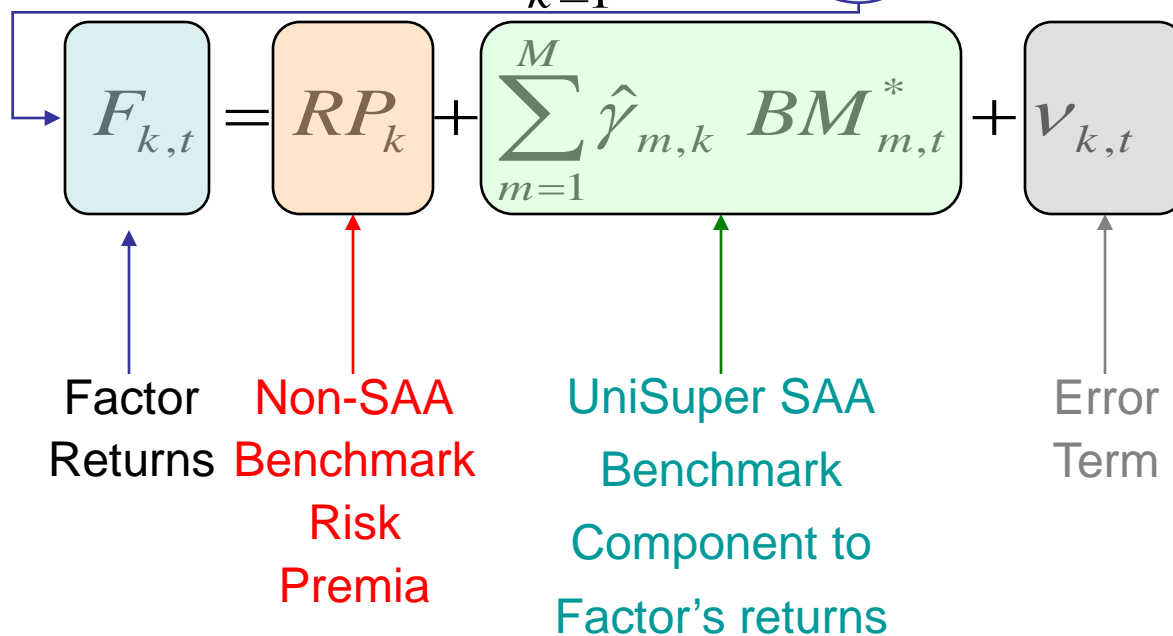
Mathematical Equations Factor Analysis





Mathematical Equations Return Attribution

$$\mu_{i,t}^{a_i} = \hat{\alpha}_{i,t}^{a_i} + \sum_{k=1}^K \hat{\beta}_{i,k,t} F_{k,t} + \varepsilon_{i,t}$$





Mathematical Equations Return Attribution (2)

$$R_t^o = \left\{ \sum_{i=1}^N w_{i,t}^{o,a_i} \hat{\alpha}_{i,t}^{a_i} \right\} + \left\{ \left[\sum_{i=1}^N \sum_{k=1}^K \sum_{m=1}^M w_{i,t}^{o,a_i} \hat{\gamma}_{m,k} \hat{\beta}_{i,k,t} BM_{m,t}^* \right] \right\} + \left\{ \left[\sum_{i=1}^N \sum_{k=1}^K w_{i,t}^{o,a_i} \hat{\beta}_{i,k,t} RP_k \right] \right\} + \varepsilon$$

Option's
historic
returns

Average
ex-post
Alpha

UniSuper SAA
Benchmark
Component

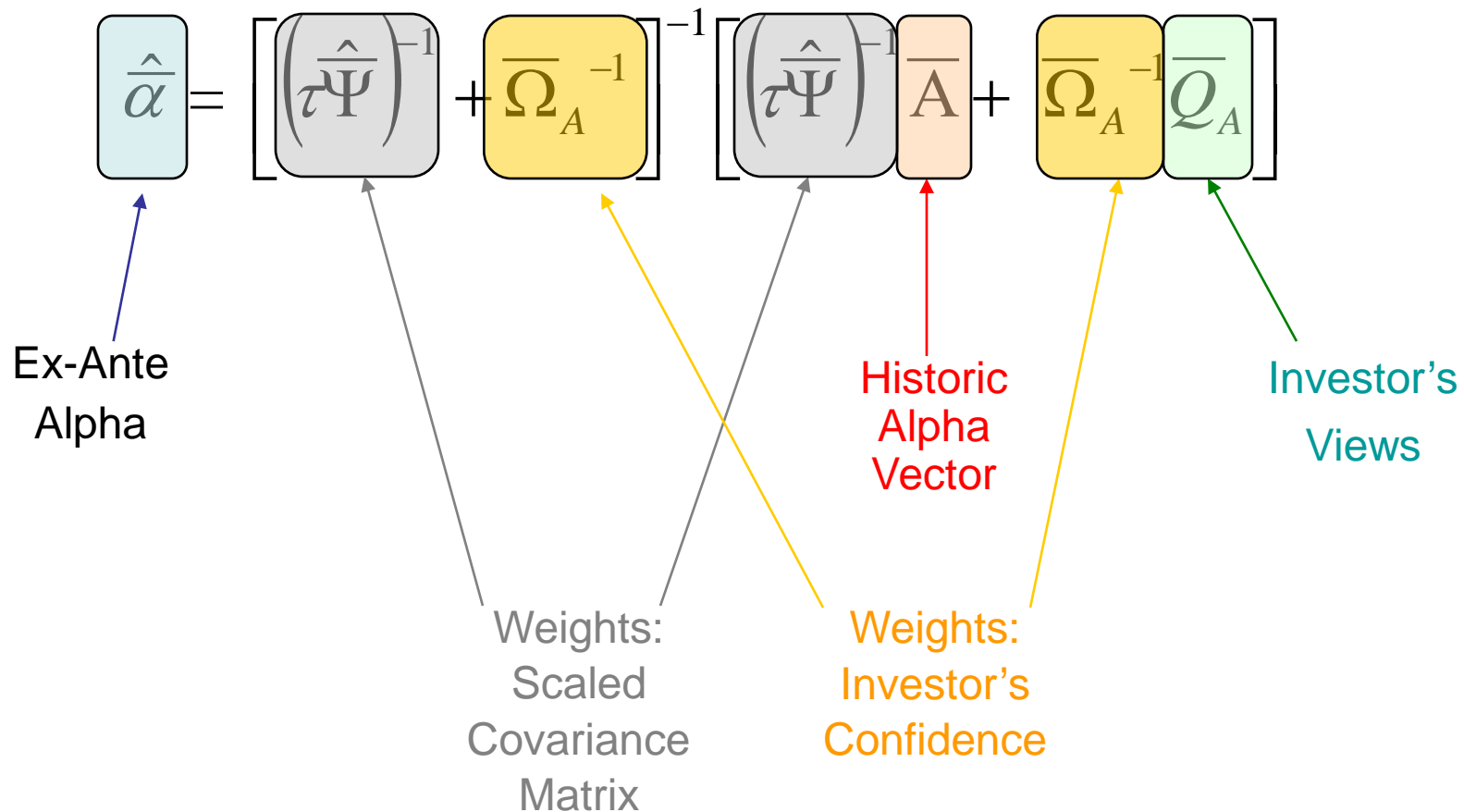
Extraneous
Beta

Error
Term

$$\varepsilon = \left\{ \sum_{i=1}^N \sum_{k=1}^K w_{i,t}^{o,a_i} \hat{\beta}_{i,k,t} v_{k,t} + \sum_{i=1}^N w_{i,t}^{o,a_i} \varepsilon_{i,t} \right\}$$



Mathematical Equations Ex-Ante Alpha Estimation





Mathematical Equations

Reverse Optimisation

$$\bar{w}^* = \frac{2\sigma_o \frac{\delta EF(\sigma_o)}{\delta \sigma} \hat{\Psi}^{-1} \hat{\alpha}}{\left(\frac{\delta EF(\sigma_o)}{\delta \sigma} \right)^2 \hat{\alpha}' \hat{\Psi}^{-1} \hat{\alpha}}$$

The equation is annotated with several labels and arrows:

- A blue arrow points from the text "Vector of Optimal Manager Weights" to the \bar{w}^* term on the left.
- A grey arrow points from the text "Constant" to the top-right term $\hat{\Psi}^{-1} \hat{\alpha}$.
- A red arrow points from the text "Information Ratio / σ_A " to the top-right term $\hat{\Psi}^{-1} \hat{\alpha}$.
- A grey arrow points from the text "Another Constant" to the bottom-left term $\left(\frac{\delta EF(\sigma_o)}{\delta \sigma} \right)^2$.
- A green arrow points from the text "Information Ratio ²" to the bottom-right term $\hat{\alpha}' \hat{\Psi}^{-1} \hat{\alpha}$.

Hence w^* is a function of:

- Actual information ratio
- Minimum required information ratio



Framework for Discussion

1. *What was the observed Option volatility, and how did each manager contribute to that volatility?*
2. *Is there a danger that a specific manager is holding a negative or short position in a given sector and that this could adversely affect the Fund's SAA?*
3. *Are there any managers who have too little tracking error and are effectively invested passively?*
4. *What levels of alpha do we expect from each manager?*
5. *Are we allocating funds to those managers in which we have the greatest confidence?*
6. *Do we expect to earn sufficient alpha from each manager, to justify active management at the Option level?*
7. *Is there an alternative manager line-up that is expected to produce better risk-adjusted returns for each Option?*



Summary – 7 Step Process

1. Determine the factor exposures by manager/asset
2. Contrast factors to the SAA factor exposures
3. Derive the ex-ante alpha per manager/asset
4. Determine marginal contribution to risk
5. Deduce an alternative “optimal” managers/assets line-up
6. Check
 1. Active program appropriate?
 2. Are we getting the factor exposures aimed for by the SAA?
 3. The error term composition
7. Interpret

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Questions?

The UniSuper Risk Budgeting and Optimisation System (TURBOs) ver 1.0 Build 1.0.0

File Menu Help

Welcome

Connect

Version Details

Please specify the path of the database file: "TURBOS.dat"

I:\RESEARCH\Programs\TURBOS\TURBOS.dat

Connect to the workspace

Welcome to TURBOs ver 1.0 - you have successfully connected to the database
Number of times the database has been used: 978

User Name:

Password:

Login Change Password

Database

Workings

Calculators

Utilities

The UniSuper Risk Budgeting and Optimisation System (TURBOs) ver 1.0 Build 1.0.0

File Menu Help

Manager Regression Calculation Page

Welcome

Database

Workings

Mngr Regression

Factor Regression

Compute Results

Manager Code: AEQ_AMP

Manager Name: AMP Capital Investors

Asset Sub-Class: AEQ_Growth

5% Significance level

End: Apr 2008 Durn (Months): 120

Compute Regression Results

Backward Elimination Regression

Waiting for user...

Log transform data

Weighted Least Squares

Model Results Residuals Backward Elimination Results Save Output

Date	er Returns (%)	ASX300A (%)	ASX VMG (%)	ASX
	2.3899	2.1974	0.6043	
	-1.5919	-2.0629	-1.3105	
	-0.1194	-0.1134	-1.1012	
	1.8721	2.6085	-0.3542	
	2.4836	2.9548	0.5142	
	3.2300	3.2490	-2.2059	
	2.2922	0.9485	-1.2530	
	1.8858	2.5279	0.2257	
	3.2377	3.6049	0.9645	
	1.3939	2.0800	0.4193	
	4.6002	4.8688	-2.0847	
	0.0017	1.3030	1.6002	
	2.3733	3.2879	1.9584	
	-2.4521	-1.6954	2.1445	
	2.4124	2.0199	0.0977	
	-4.7650	-5.8269	-0.6237	
	3.0361	3.5444	-1.3901	
	5.6907	4.6605	-4.3543	
	0.8590	0.5786	2.7535	
	3.7620	3.4951	-2.3685	
	3.1079	3.0559	-1.7756	
	5.2068	4.3424	-1.3290	
	-4.6319	-3.9190	3.2240	
	5.5394	4.9669	-1.4758	
	2.3538	2.2314	0.2164	

Calculators

Utilities

Moments of the residuals

Residual Statistic	Value
Average Residual	0.00049
Standard Deviation	0.00467
Skewness	0.09216
Kurtosis less 3	-0.55265
Durbin Watson Stat	1.74291
Auto Regression Factor	0.09806

Residual Histogram

Normal Probability Plot

Histogram of residuals relative to a Normal distribution