# Beyond Easy Averages: Improved Performance Metrics in Limited Overs Cricket 

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## The Ubiquitous Statistic

Averages are:
o Simple and easy to calculate
o Familiar and (generally) interpretable

But, they rely heavily on:

- Comparability and
o "Equi-relevance" of each component


## In Limited Overs Cricket

Batsmen assessed via:
o Batting average (runs per dismissal)

- Strike rate (runs per delivery)

Bowlers assessed via:

- Bowling average (runs per dismissal)
o Economy rate (runs per over)


## In Limited Overs Cricket

Batsmen assessed via:
o Batting average (runs per dismissal)

- Strike rate (runs per delivery)

Bowlers assessed via:

- Bowling average (runs per dismissal)
- Economy rate (runs per over)

No CONTEXT to components of averages! i.e., not equi-relevant

## "Resource"-based Approach

o "Under what circumstances" as important as "How many"

- Measure output against available resources
- Utilisation = runs scored per resources consumed
o How to measure resources?
- The D/L/S Formula


## ASIDE: The D/L/S Formula

- Duckworth-Lewis-Stern Method

Resources available with $u$ overs remaining and $w$ wickets down:

$$
R(u, w, \lambda)=F_{w} \lambda^{n_{w}-n_{0}} \frac{\left(1-e^{-b u g(u, \lambda) / F_{w} \lambda^{n_{w}}}\right)}{\left(1-e^{-50 b / \lambda^{n_{0}}}\right)}
$$

- $F_{w}$ 's and $n_{w}$ 's estimated (proprietary) parameters
- $\lambda=$ "match factor" $\left[\lambda^{n_{0}}\left(1-e^{-50 b / \lambda^{n_{0}}}\right)=\right.$ first innings total score]
- $g(u, \lambda)$ is DLS "differential straightening" adjustment.


## ASIDE: The D/L/S Formula

The "D/L" methodology models "standard" accelerations
(Dark points represent values based on 20 or more matches)


## ASIDE: The D/L/S Formula

The "/S" component models "straightening" in high scores


## ASIDE: The D/L/S Formula

NOTE: "Straightening" in high scores is "differential"


## Individual Performances

o Assess individual's utilisation rate relative to other players in the match:

- Net Runs Attributable:
- Batsman $i$ :

$$
N R A_{i}=\sum_{k \in K_{i}}\left(\sigma_{k}-U_{i} \rho_{k}\right)
$$

- $K_{i}=$ set of indices of balls faced by batsman $i$
- $\sigma_{k}=$ score (off the bat) on ball $k$
- $\rho_{k}=\mathrm{D} / \mathrm{L} / \mathrm{S}$ resources associated with ball $k$
- $U_{i}=$ utilisation rate of all other batsmen $=\frac{S_{1}+S_{2}-s_{i}}{R_{1}+R_{2}-r_{i}}$


## Individual Performances

o Assess individual's utilisation rate relative to other players in the match:

- Net Runs Attributable:
- Bowler j:

$$
N R A_{j}=\sum_{k \in L_{j}}\left(V_{j} \rho_{k}-\sigma_{k}\right)+X_{j} r_{j}-w_{j}
$$

- $L_{j}=$ set of indices of balls delivered by bowler $j$
- $X_{j}=$ extras rate for all other bowlers $=\frac{W_{1}+W_{2}-w_{j}}{R_{1}+R_{2}-r_{j}}$
- $V_{j}=$ utilisation rate of all other bowlers $=\frac{S_{1}+S_{2}-s_{j}}{R_{1}+R_{2}-r_{j}}$


## Individual Performances

- Individual $N R A^{\prime}$ s now "equi-relevant".

Almost!

## Individual Performances

O aNRA - Adjust for performance levels of opponents faced

- For Batsmen:
$a N R A_{i}=N R A_{i}+\alpha \sum_{j \in J_{i}} \sum_{k \in K_{i} \cap L_{j}} N R A_{j}\left(\rho_{k} / r_{j}\right)$
- $\alpha=$ "tuning" factor (currently set at 0.1 )
- $J_{i}=$ set of indices of bowlers faced by batsman $i$
- Similarly for Bowlers


## Indian Premier League (IPL)

o During 2010 to 2013 seasons:

- 286 Matches scheduled (282 completed)
- 328 Players participated
- 125 Batsmen with at least 10 contributions
- 106 Bowlers with at least 10 contributions
o Player salaries set periodically at auction
- Are 2014 salaries commensurate with past performance? With 2014 performance?


## Rating Batsmen: IPL 2010-3

Figure 1: Average aNRA vs Batting Average


## Rating Batsmen: IPL 2010-3

Figure 2: Average aNRA vs Batting Average + Strike Rate


## Rating Bowlers: IPL 2010-3

Figure 3: Average aNRA vs Bowling Average


## Rating Bowlers: IPL 2010-3

Figure 4: Average aNRA vs Economy Rate


## "Expert" Evaluation

o Overall value in single match for individual player:

$$
c N R A=a N R A(\text { batting })+a N R A \text { (bowling) }
$$

o Breakdown of 282 Man of the Match Awards:

- 147 (52\%) MotM's = highest $c N R A$
- 160 (57\%) MotM's = highest $c$ NRA on winning side
- 227 (80\%) MotM's = cNRA among top 3 in match


## "Expert" Evaluation

Case Study \#1

## Kolkata Knight Riders: 4/180 (20) Sunrisers Hyderabad: 7/132 (20)



## "Expert" Evaluation

## Case Study \#1

| Kolkata Knight Riders: $4 / 180(20)$ | Sunrisers Hyderabad: 7/132 (20) |  |  |  |  |  |
| :--- | :---: | :---: | :--- | :--- | :--- | :--- |
| MS Bisla | $28(24)[116.7]$ | 0.207 | PA Patel | $27(31)[87.1]$ | -9.868 |  |
| G Gambhir | $53(45)[117.8]$ | 1.315 | CL White | $34(31)[109.7]$ | -2.139 |  |
| EJG Morgan | $47(21)[223.8]$ | 21.469 | KC Sangakkara | $2(3)[66.7]$ | -3.531 |  |
| JH Kallis | $41(27)[151.9]$ | 7.130 | DB Ravi Teja | $10(13)[76.9]$ | -6.049 |  |
| YK Pathan | $3^{*}(3)[100.0]$ | -1.262 | A Ashish Reddy | $4(5)[80.0]$ | -2.824 |  |
|  |  |  | NLTC Perera | $36(25)[144.0]$ | 6.531 |  |
| Bowling |  |  | GH Vihari | $1(2)[50.0]$ | -1.747 |  |
| KV Sharma | $1 / 13(2)[6.50]$ | 3.514 | KV Sharma | $5^{*}(9)[55.6]$ | -7.276 |  |
| DW Steyn | $0 / 29(4)[7.25]$ | 0.256 | A Mishra | $1^{*}(1)[100.0]$ | -0.407 |  |
| A Ashish Reddy | $1 / 15(2)[7.50]$ | 1.075 |  |  |  |  |
| ISharma | $0 / 33(4)[8.25]$ | -2.683 | Bowling |  |  |  |
| A Mishra | $0 / 28(3)[9.33]$ | -6.472 | JH Kallis | $3 / 13(4)[3.25]$ | 22.664 |  |
| NLTC Perera | $0 / 44(4)[11.0]$ | -15.382 | SMSM Senanayake | $1 / 18(4)[4.50]$ | 11.205 |  |
| GH Vihari | $0 / 14(1)[14.0]$ | -7.772 | L Balaji | $0 / 30(4)[7.50]$ | -3.107 |  |
|  |  |  | SP Narine | $1 / 31(4)[7.75]$ | -1.038 |  |
|  |  |  | R Bhatia | $2 / 33(4)[8.25]$ | -1.458 |  |

## "Expert" Evaluation

Case Study \#2

## Mumbai Indians: 2/182 (20)

Kochi Tuskers Kerala: 2/184 (19)

| DJ Jacobs | $12(21)[57.1]$ |  | DPMD Jayawardene | $56(36)[155.6]$ |  |
| :--- | :---: | :---: | :--- | :---: | :---: |
| AT Rayudu | $53(33)[160.6]$ |  | BB McCullum | $81(60)[135.0]$ |  |
| SR Tendulkar | $100^{*}(66)[151.5]$ |  | RA Jadeja | $25^{*}(11)[227.3]$ |  |
|  |  | BJ Hodge | $11^{*}(7)[157.1]$ |  |  |
| Bowling |  |  |  |  |  |
| RP Singh | $0 / 15(4)[3.75]$ |  | Bowling |  |  |
| RA Jadeja | $0 / 29(4)[7.25]$ |  | MM Patel | $0 / 15(3)[5.00]$ |  |
| NLTC Perera | $0 / 38(4)[9.50]$ |  | Harbhajan Singh | $0 / 33(4)[8.25]$ |  |
| RV Gomez | $1 / 29(3)[9.66]$ |  | AG Murtaza | $0 / 37(4)[9.25]$ |  |
| R Vinay Kumar | $0 / 48(4)[12.0]$ |  | SL Malinga | $2 / 42(4)[10.5]$ |  |
| RR Powar | $0 / 12(1)[12.0]$ |  | R Sathish | $0 / 11(1)[11.0]$ |  |
|  |  | KA Pollard | $0 / 43(3)[14.3]$ |  |  |

## "Expert" Evaluation

Case Study \#2

| Mumbai Indians: 2/182 (20) |  |  | Kochi Tuskers Kerala: 2/184 (19) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| DJ Jacobs | 12(21) [57.1] | -18.675 | DPMD Jayawardene | 56(36) [155.6] | 5.272 |
| AT Rayudu | 53(33) [160.6] | 3.622 | BB McCullum | 81(60) [135.0] | -2.568 |
| SR Tendulkar | 100*(66) [151.5] | 6.756 | RA Jadeja | 25*(11) [227.3] | 7.620 |
|  |  |  | BJ Hodge | 11*(7) [157.1] | -0.635 |
| Bowling |  |  |  |  |  |
| RP Singh | 0/15(4) [3.75] | 20.536 | Bowling |  |  |
| RA Jadeja | 0/29(4) [7.25] | 9.152 | MM Patel | 0/15(3) [5.00] | 11.234 |
| NLTC Perera | 0/38(4) [9.50] | -1.511 | Harbhajan Singh | 0/33(4) [8.25] | 3.864 |
| RV Gomez | 1/29(3) [9.66] | -1.101 | AG Murtaza | 0/37(4) [9.25] | -0.531 |
| R Vinay Kumar | 0/48(4) [12.0] | -13.062 | SL Malinga | 2/42(4) [10.5] | -6.661 |
| RR Powar | 0/12(1) [12.0] | -2.392 | R Sathish | 0/11(1) [11.0] | -1.945 |
|  |  |  | KA Pollard | 0/43(3) [14.3] | -17.204 |

- McCullum's score high, but (relatively speaking) slow (Tendulkar's century better except in losing effort)
- Singh's economy lowest by some way (and his team won narrowly), just took no wickets!


## "Expert" Evaluation

Case Study \#3

| Chennai Super Kings: 8/173 (20) |  | Mumbai Indians: 8/174 (20) |  |
| :---: | :---: | :---: | :---: |
| F du Plessis | 9(11) [81.8] | JEC Franklin | 1(9) [11.1] |
| M Vijay | 41(29) [141.4] | SR Tendulkar | 74(44) [168.2] |
| SK Raina | 36(21) [171.4] | KD Karthik | 11 (5) [220.0] |
| DJ Bravo | 40(33) [121.2] | AT Rayudu | 0(2) [0.0] |
| MS Dhoni | 25(15) [166.7] | RG Sharma | 60(46) [130.4] |
| JA Morkel | 3(3) [100.0] | RJ Peterson | 0(2) [0.0] |
| RA Jadeja | $9(6)$ [150.0] | Harbhajan Singh | 0(1) [0.0] |
| R Ashwin | O(1) [0.0] | SL Malinga | 0(1) [0.0] |
| S Badrinath | $1^{*}(1)$ [100.0] | DR Smith | 24*(16) [266.7] |
| Bowling |  | RP Singh | 1*(1) [100.0] |
| Harbhajan Singh | 0/14(3) [4.67] | Bowling |  |
| SL Malinga | 3/25(4) [6.25] | RA Jadeja | 2/12(2) [6.00] |
| RP Singh | 3/28(4) [7.00] | R Ashwin | 1/28(4) [7.00] |
| JEC Franklin | 1/8(1) [8.00] | BW Hilfenhaus | 2/34(4) [8.50] |
| RJ Peterson | 0/22(2) [11.0] | SB Jakati | 0/27(3) [9.00] |
| MM Patel | 0/46(4) [11.5] | DJ Bravo | 2/39(4) [9.75] |
| DR Smith | 0/26(2) [13.0] | JA Morkel | 0/34(3) [11.3] |

## "Expert" Evaluation

Case Study \#3

| Chennai Super Kings: 8/173 (20) | Mumbai Indians: 8/174(20) |  |  |  |  |
| :--- | :---: | :---: | :--- | :---: | :---: |
| F du Plessis | $9(11)[81.8]$ | -6.173 | JEC Franklin | $1(9)[11.1]$ | -14.861 |
| M Vijay | $41(29)[141.4]$ | 1.099 | SR Tendulkar | $74(44)[168.2]$ | 19.942 |
| SK Raina | $36(21)[171.4]$ | 8.273 | KD Karthik | $11(5)[220.0]$ | 3.041 |
| DJ Bravo | $40(33)[121.2]$ | -4.777 | AT Rayudu | $0(2)[0.0]$ | -3.454 |
| MS Dhoni | $25(15)[166.7]$ | 2.965 | RG Sharma | $60(46)[130.4]$ | -1.350 |
| JA Morkel | $3(3)[100.0]$ | -1.873 | RJ Peterson | $0(2)[0.0]$ | -3.260 |
| RA Jadeja | $9(6)[150.0]$ | -0.596 | Harbhajan Singh | $0(1)[0.0]$ | -1.823 |
| R Ashwin | $0(1)[0.0]$ | -1.697 | SL Malinga | $0(1)[0.0]$ | -1.816 |
| S Badrinath | $1^{*}(1)[100.0]$ | -0.646 | DR Smith | $24^{*}(16)[266.7]$ | 10.420 |
| Bowling |  |  | RP Singh | $1^{*}(1)[100.0]$ | -0.453 |
| Harbhajan Singh | $0 / 14(3)[4.67]$ | 9.569 | Bowling |  | $2 / 12(2)[6.00]$ |
| SL Malinga | $3 / 25(4)[6.25]$ | 10.719 | RA Jadeja | 7.497 |  |
| RP Singh | $3 / 28(4)[7.00]$ | 8.667 | R Ashwin | $1 / 28(4)[7.00]$ | 5.905 |
| JEC Franklin | $1 / 8(1)[8.00]$ | 1.860 | BW Hilfenhaus | $2 / 34(4)[8.50]$ | 1.860 |
| RJ Peterson | $0 / 22(2)[11.0]$ | -6.473 | SB Jakati | $0 / 27(3)[9.00]$ | -1.102 |
| MM Patel | $0 / 46(4)[11.5]$ | -14.759 | DJ Bravo | $2 / 39(4)[9.75]$ | -4.663 |
| DR Smith | $0 / 26(2)[13.0]$ | -10.223 | JA Morkel | $0 / 34(3)[11.3]$ | -12.440 |

- Smith scored 6, 4, 4 from last 3 balls to grab victory!


## "Expert" Evaluation

Case Study \#4

| Mumbai Indians: 5/139 (20) |  |  | Chennai Super Kings: 10/79 (15.2) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| SR Tendulkar | 15(18) [83.3] |  | M Vijay | 2(4) [50.0] |  |
| DR Smith | 22(24) [91.7] |  | SK Raina | O(1) [0.0] |  |
| KA Pollard | 1(3) [33.3] |  | S Badrinath | 0(3) [0.0] |  |
| KD Karthik | 23(23) [100.0] |  | DJ Bravo | 9(7) [128.6] |  |
| AT Rayudu | 10(11) [90.9] |  | R Ashwin | 2(8) [25.0] |  |
| RG Sharma | 39*(30) [130.0] |  | MEK Hussey | 22(26) [84.6] |  |
| Harbhajan Singh | 25*(11) [227.3] |  | MS Dhoni | 10(12) [83.3] |  |
|  |  |  | CH Morris | 1(4) [25.0] |  |
| Bowling |  |  | MM Sharma | 0(3) [0.0] |  |
| CH Morris | 0/14(3) [4.67] |  | RA Jadeja | 20(16) [125.0] |  |
| MM Sharma | 0/20(4) [5.00] |  | B Laughlin | 4(8) [50.0] |  |
| R Ashwin | 1/11(2) [5.50] |  | Bowling |  |  |
| DJ Bravo | 1/19(3) [6.33] |  | SL Malinga | 2/6(3) [2.00] |  |
| RA Jadeja | 3/29(4) [7.25] |  | Harbhajan Singh | 1/13(4) [3.25] |  |
| B Laughlin | 0/46(4) [11.5] |  | PP Ojha | 3/11(2.2) [4.71] |  |
|  |  |  | P Suyal | 1/21 (3) [7.00] |  |
|  |  |  | MG Johnson | 3/27(3) [9.00] |  |

## "Expert" Evaluation

Case Study \#4

| Mumbai Indians: 5/139 (20) |  |  | Chennai Super Kings: 10/79 (15.2) |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| SR Tendulkar | 15(18) [83.3] | 0.721 | M Vijay | 2(4) [50.0] | -4.291 |
| DR Smith | 22(24) [91.7] | 3.622 | SK Raina | $0(1)$ [0.0] | -5.236 |
| KA Pollard | 1(3) [33.3] | -3.919 | S Badrinath | 0(3) [0.0] | -7.457 |
| KD Karthik | 23(23) [100.0] | 4.912 | DJ Bravo | 9(7) [128.6] | -0.949 |
| AT Rayudu | 10(11) [90.9] | 0.375 | R Ashwin | 2(8) [25.0] | -8.661 |
| RG Sharma | $39^{*}(30)$ [130.0] | 14.396 | MEK Hussey | 22(26) [84.6] | 2.602 |
| Harbhajan Singh | 25*(11) [227.3] | 15.434 | MS Dhoni | 10(12) [83.3] | -2.098 |
|  |  |  | CH Morris | 1(4) [25.0] | -10.215 |
| Bowling |  |  | MM Sharma | 0(3) [0.0] | -11.556 |
| CH Morris | 0/14(3) [4.67] | -1.085 | RA Jadeja | 20(16) [125.0] | 10.252 |
| MM Sharma | 0/20(4) [5.00] | -2.203 | B Laughlin | 4(8) [50.0] | 3.942 |
| R Ashwin | 1/11(2) [5.50] | 0.395 | Bowling |  |  |
| DJ Bravo | 1/19(3) [6.33] | 0.265 | SL Malinga | 2/6(3) [2.00] | 21.061 |
| RA Jadeja | 3/29(4) [7.25] | -4.424 | Harbhajan Singh | 1/13(4) [3.25] | 4.765 |
| B Laughlin | 0/46(4) [11.5] | -26.528 | PP Ojha | 3/11(2.2) [4.71] | 19.104 |
|  |  |  | P Suyal | 1/21(3) [7.00] | -4.656 |
|  |  |  | MG Johnson | 3/27(3) [9.00] | -5.805 |

- Johnson's 3rd cost 20 (game essentially over) and 3 catches dropped!


## The "Market"

Figure 5: Average cNRA (2010-2013) vs 2014 Salary


## The "Market"

Figure 6: Average cNRA (2014) vs 2014 Salary


## Career Arcs

Figure 7: V Sehwag (2008-2014)


## Career Arcs

Figure 8: CH Gayle (2009-2014)


## Career Arcs

Figure 10: DA Warner (2009-2014)


## Career Arcs

Figure 11: Steve Smith (2012-2014)


## Career Arcs

Figure 12: AB de Villiers (2008-2014)


## Career Arcs

Figure 13: Glen Maxwell (2012-2014)


## Career Arcs

Figure 14: Murali (2008-2014)


## Career Arcs

Figure 15: Brett Lee (2008-2013)


## Career Arcs

Figure 16: Jacques Kallis (2008-2014)


## Career Arcs

Figure 17: Dale Steyn (2009-2014)


## Career Arcs

Figure 18: Kevin Pietersen (2009-2014)


## Conclusions:

○ aNRA avoids inflated averages of runs scored in "low pressure" situations (and also the issue of multiple "not out" innings)

- aNRA gives reasonable trade-off between quantity and "quality" of runs (i.e., runs at good utilisation rate)
○ aNRA misses "symbiotic" relationships (e.g., "sheet anchor" role and the importance of partnerships) and fielding


## Conclusions:

o aNRA may be useful in assessing player "value", but other factors are also relevant
o aNRA may be useful in tracking "career arcs" to project future performance

## Extensions:

o BBL Ratings

- Average vs Aggregate?
- CHOICE: Aggregate but with downweighting
- All-rounder Ratings, total vs "balance"
- CHOICE: Balance - Use harmonic mean of batting and bowling aggregates


## Extensions:

o BBL Ratings

- End of 2014/2015 Season:

| Batsmen |  |  | Bowlers |  |  |  | All-Rounders |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rank | Player | Rating | Rank | Player | Rating | Rank | Player | Rating |  |
| $\mathbf{1}$ | Nic Maddinson | 52.71 | 1 | Brad Hogg | 56.62 | 1 | John Hastings | 21.37 |  |
| 2 | Ben Stokes | 49.67 | 2 | Brett Lee | 52.40 | 2 | Cameron Boyce | 15.37 |  |
| 3 | Chris Lynn | 48.60 | 3 | Jason <br> Behrendorff | 45.85 | 3 | Ashton Turner | 9.29 |  |
| 4 | Tim Ludeman | 45.60 | 4 | Gurinder Sandu | 42.89 | 4 | Jacques Kallis | 8.81 |  |
| 5 | Michael Carberry | 42.70 | 5 | John Hastings | 42.22 | 5 | Ben Laughlin | 8.79 |  |
| 6 | Ben Cutting | 42.64 | 6 | Michael Beer | 41.60 | 6 | Xavier Doherty | 5.18 |  |
| 7 | Jordan Silk | 41.59 | 7 | Lasith Malinga | 32.42 | 7 | Andre Russell | 4.82 |  |
| 8 | Aiden Blizzard | 41.07 | 8 | Muttiah <br> Muralitharan | 32.36 | 8 | Darren Sammy | 4.48 |  |
| 9 | Shaun Marsh | 39.64 | 9 | Shakib Al Hasan | 31.83 | 9 | Yasir Arafat | 4.14 |  |
| 10 | Travis Head | 37.06 | 10 | James Hopes | 31.51 | 10 | Adam Voges | 3.23 |  |

## Thank You

